

Financial Mathematics

Basics of processes

3600-1. Let W_t be a Brownian motion.

a. Compute $\mathbb{E}[W_5^7 W_4^9]$.

b. Compute $\mathbb{E} \left[\int_0^6 W_t^4 dt + (e^{W_t} - e^2)_+^2 dW_t \right]$.

That is, compute the expectation of the sum of $\int_0^6 W_t^4 dt$ and $\int_0^6 (e^{W_t} - e^2)_+^2 dW_t$.

c. Compute

$$\mathbb{E} \left[\int_0^5 W_t^8 dt + \sin^2(4W_t - 2) dW_t \right].$$