

MATH 1271 Fall 2013, Midterm #2  
Handout date: Thursday 14 November 2013  
Instructor: Scot Adams

PRINT YOUR NAME:

PRINT YOUR X.500 ID:

PRINT YOUR TA'S NAME:

WHAT RECITATION SECTION ARE YOU IN?

Closed book, closed notes, no calculators/PDAs; no reference materials of any kind. Turn off all handheld devices, including cell phones.

Show work; a correct answer, by itself, may be insufficient for credit. Arithmetic need not be simplified, unless the problem requests it.

I. Multiple choice

A. (5 pts) (no partial credit) Let  $y = x^2 + x$ . Compute  $\Delta y$ , evaluated at  $x = 10$ ,  $\Delta x = 0.1$ . (Hint:  $\Delta(x^2) = 2x(\Delta x) + (\Delta x)^2$ .)

- (a) 2.1
  - (b) 1.2
  - (c) 2.11
  - (d) 1.22
  - (e) NONE OF THE ABOVE
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B. (5 pts) (no partial credit) Let  $f(x) = x^3 + 4x + 3$ . What is the iterative formula of Newton's method used to solve  $f(x) = 0$ ? Circle one of the following answers:

- (a)  $x_{n+1} = x_n - \frac{x_n^3 + 4x_n + 3}{3x_n^2 + 4}$
  - (b)  $x_{n+1} = x_n + \frac{x_n^3 + 4x_n + 3}{3x_n^2 + 4}$
  - (c)  $x_{n+1} = x_n - \frac{3x_n^2 + 4}{x_n^3 + 4x_n + 3}$
  - (d)  $x_{n+1} = x_n + \frac{3x_n^2 + 4}{x_n^3 + 4x_n + 3}$
  - (e) NONE OF THE ABOVE
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C. (5 pts) (no partial credit) Find the logarithmic derivative of  $x^2 + 3x - 8$  w.r.t.  $x$ . Circle one of the following answers:

- (a)  $-\left[\frac{2x + 3}{x^2 + 3x - 8}\right]$
- (b)  $\frac{x^2 + 3x - 8}{2x + 3}$
- (c)  $\frac{2x + 3}{x^2 + 3x - 8}$
- (d)  $(\ln(x^2)) + 3(\ln x) - (\ln 8)$
- (e) NONE OF THE ABOVE

D. (5 pts) (no partial credit) Let  $f$  be a function such that  $f'(x) = 4(\cos(4x))$ . Suppose, also, that  $f(0) = 1$ . Which of the following is an equation of the tangent line to the graph of  $f$  at  $(0, 1)$ . Circle one of the following answers:

- (a)  $y = 4(x - 1)$
  - (b)  $y - 1 = 4(\cos(4x))x$
  - (c)  $y - 1 = 4(\cos 4)x$
  - (d)  $y = -4(\sin(x))(x - 1)$
  - (e) NONE OF THE ABOVE
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E. (5 pts) (no partial credit) Suppose

- $f'(1) = 1, f''(1) = 3,$
- $f'(2) = 0, f''(2) = -2,$
- $f'(3) = 0, f''(3) = 6.$

At which of the numbers 1, 2 and 3 does  $f$  have a local maximum? Circle one of the following answers:

- (a) 1, but not 2, and not 3
  - (b) 2, but not 1, and not 3
  - (c) 3, but not 1, and not 2
  - (d) both 2 and 3, but not 1
  - (e) NONE OF THE ABOVE
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F. (5 pts) (no partial credit) Suppose  $f''(x) = -x^2 + 4x - 3$ . At most one of the following statements is true. If one is, circle it. Otherwise, circle "NONE OF THE ABOVE".

- (a)  $f$  is concave down on  $(-\infty, 1]$ , up on  $[1, 3]$  and down on  $[3, \infty)$ .
- (b)  $f$  is concave up on  $(-\infty, 1]$ , down on  $[1, 3]$  and up on  $[3, \infty)$ .
- (c)  $f$  is concave down on  $(-\infty, -3]$ , up on  $[-3, -1]$  and down on  $[-1, \infty)$ .
- (d)  $f$  is concave up on  $(-\infty, -3]$ , down on  $[-3, -1]$  and up on  $[-1, \infty)$ .
- (e) NONE OF THE ABOVE

II. True or false (no partial credit):

a. (5 pts) Let  $f$  and  $g$  be any two functions such that  $\lim_{x \rightarrow 7} f(x) = \infty$  and  $\lim_{x \rightarrow 7} g(x) = \infty$ . Then  $\lim_{x \rightarrow 7} [1/(f(x))]^{g(x)} = \infty$ .

b. (5 pts) Let  $f, g : \mathbb{R} \rightarrow \mathbb{R}$  be any two differentiable functions such that, for all  $x \in \mathbb{R}$ ,  $f'(x) = g'(x)$ . Then  $f - g$  is a constant.

c. (5 pts) If  $f$  has a local minimum at  $c$ , then  $c$  is a critical number for  $f$ .

d. (5 pts) Let  $f$  be any function such that  $f(x)$  is increasing on  $1 < x < 3$ . Then  $f'(2) > 0$ .

e. (5 pts) Let  $f$  be any function such that  $f(3) = 5$  and such that  $f''(3) = 0$ . Then  $(3, 5)$  is a point of inflection for  $f$ .

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PLEASE DO NOT WRITE BELOW THE LINE

VERSION B

I. A,B,C

I. D,E,F

II. a,b,c,d,e

III. 1.

III. 2.

III. 3.

III. 4.

III. Computations. Show work. Unless otherwise specified, answers must be exactly correct, but can be left in any form easily calculated on a standard calculator.

1. (10 pts) Compute  $d \left[ \frac{e^{-x^2}}{3 - (\cot(x^4))} \right]$ . (Here  $e^{-x^2}$  means  $e^{(-x^2)}$ .)

WARNING: You are asked to find the differential,  $d$ , and *NOT* the derivative,  $d/dx$ .

2. (10 pts) Say  $f'(x) = e^{x^2}$ . (Here  $e^{x^2}$  means  $e^{(x^2)}$ .) Let  $g(x) = f(3x - 5)$ . Find  $g'(1)$ .

3. (15 pts) We must design a cylindrical can with an open top that contains  $27\pi$  cubic feet of volume inside, and which minimizes surface area. Find the height,  $h$ , and the radius,  $r$ , of such a can. (Remember: The surface area includes the side of the can, and the bottom of the can, but the can has no top).

4. (10 pts) Sand is accumulating in a conical pile whose base radius is, at all times, half its height. Sand is being added at 100 cubic feet per hour. At what rate is the height of the pile increasing, at the moment when the height is 5 feet?