

# Calculus

W 1 February 2012

RESET THE  
SESSION

SET THE  
PARTICIPANT  
LIST

PLUG IN THE  
RECEIVER

Boxed answers agree with  
TurningPoint answers

Points agree with  
TurningPoint points

Points total to 100

Topics covered are in bounds

QUIZ  
FOLLOWS

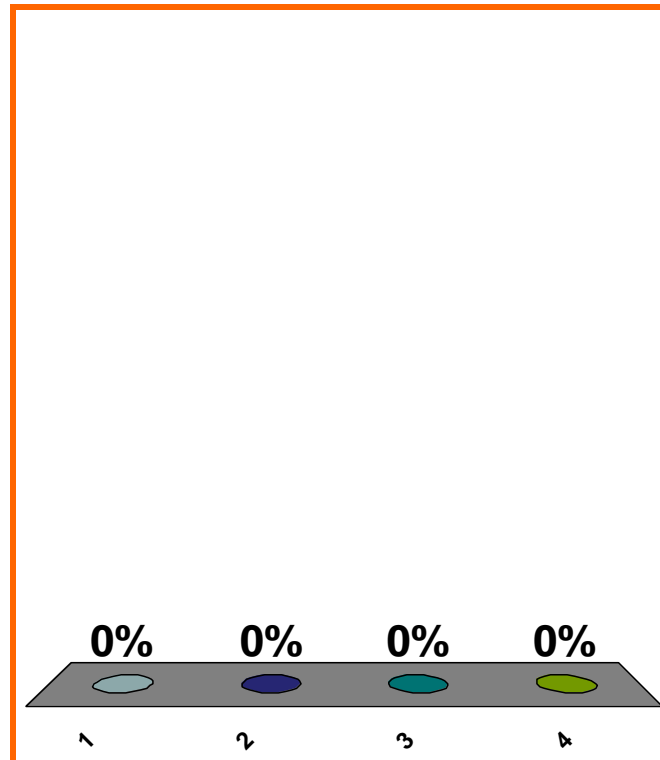
$$\lim_{x \rightarrow \infty} \left[ \frac{3x^4 - x^3 + 2x}{7x^4 + 5x - 1} \right] = ??$$

(a) 3/7

(b) -2

(c) 0

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

0 of 5

Topic 0240

20 pts

5

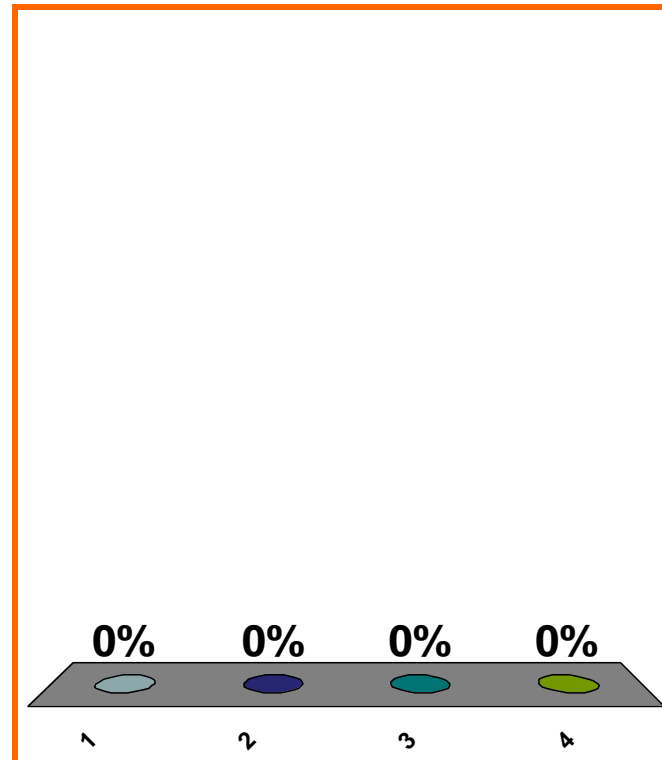
$$\lim_{x \rightarrow 0} \left[ \frac{3x^4 - x^3 + 2x}{7x^4 + 5x - 1} \right] = ??$$

(a) 3/7

(b) -2

(c) 0

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
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Topic 0240

20 pts

6

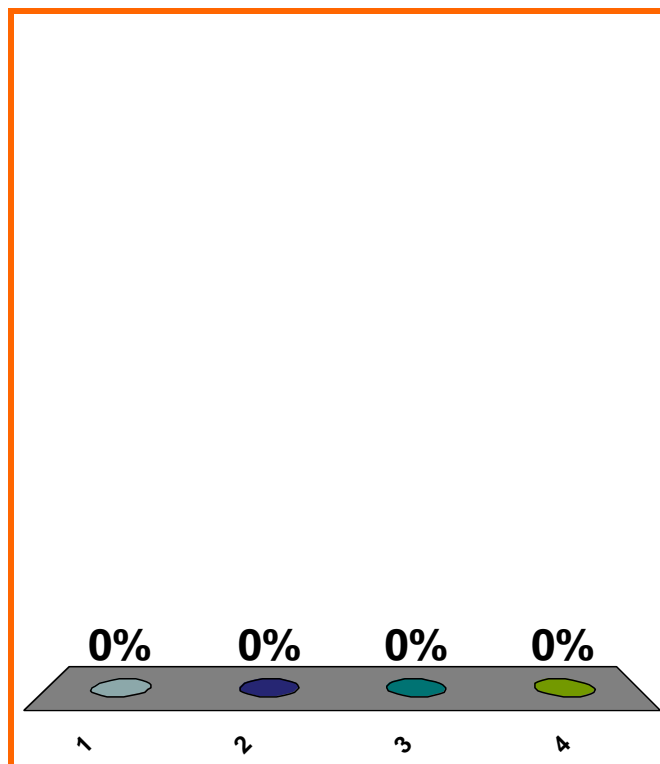
$$\frac{5q^3 - 2q + 4}{2q + 7} + \frac{(q^3 + 4)(2q - 3)}{2q^7 - 9q + 4}$$

(a) a polynomial in  $q$

(b) rational, **nonpolynomial**  
in  $q$

(c) transcendental in  $q$

(d) **none** of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0140

0 pts

7

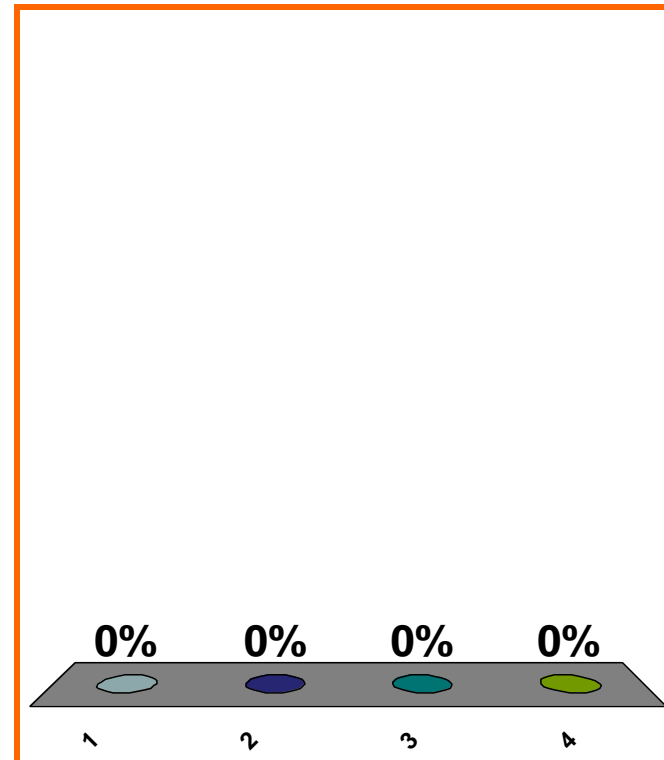
$$x^2 + 3\sqrt{x} + 1 \text{ is ??}$$

(a) a polynomial in  $x$

(b) rational, **nonpolynomial**  
in  $x$

(c) algebraic, **nonrational**  
in  $x$

(d) **none** of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40



distance from  $a$  to  $b$ ?

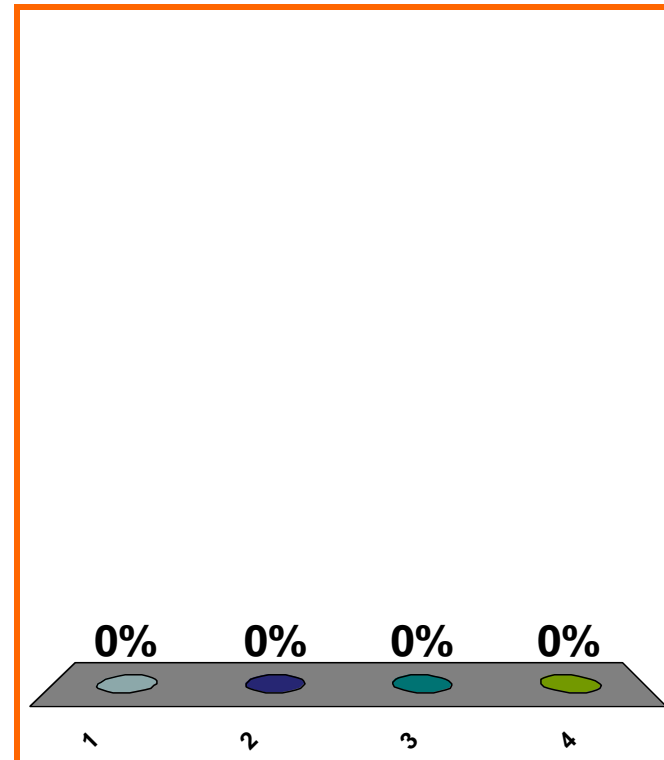
(a)  $a - b$

(b)  $b - a$

(c)  $a + b$

(d) none of the above

Correct answer:  $|a - b|$



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

from position 5 to position 9  
from time 3 to time 11

average velocity = ??

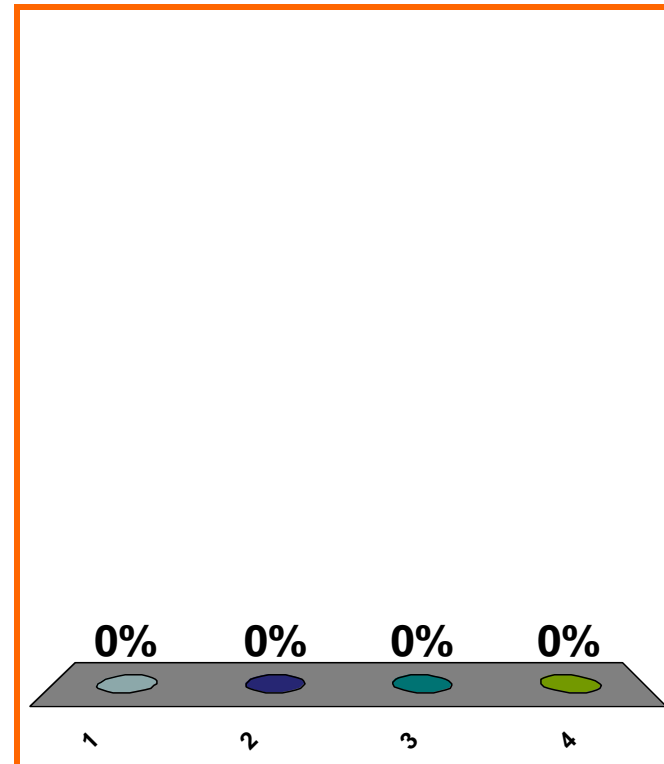
(a) 2

(b) 4

(c) 8

(d) none of the above

Correct answer: 1/2



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

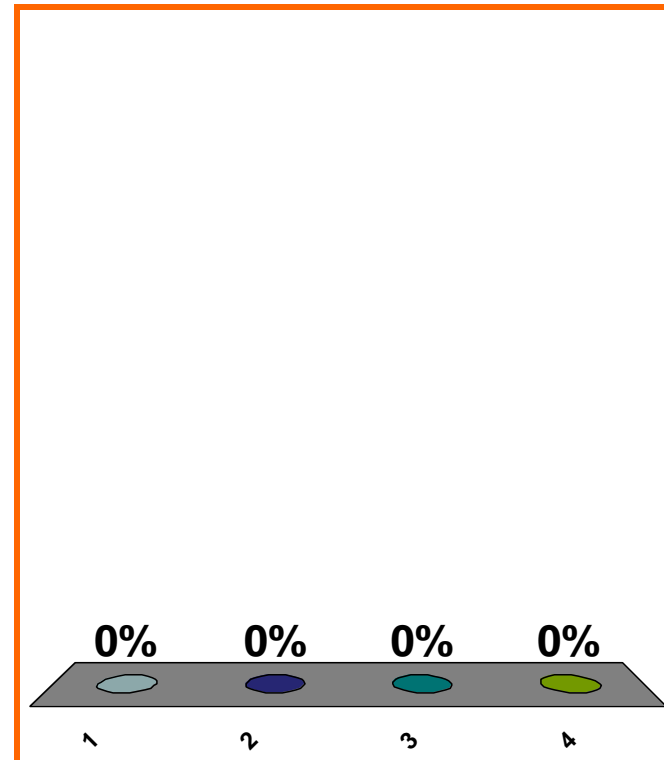
$$\lim_{x \rightarrow 0} \frac{3x^3 + 2x}{x} = ??$$

(a) 0

(b) 2

(c) 3

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0140

0 pts

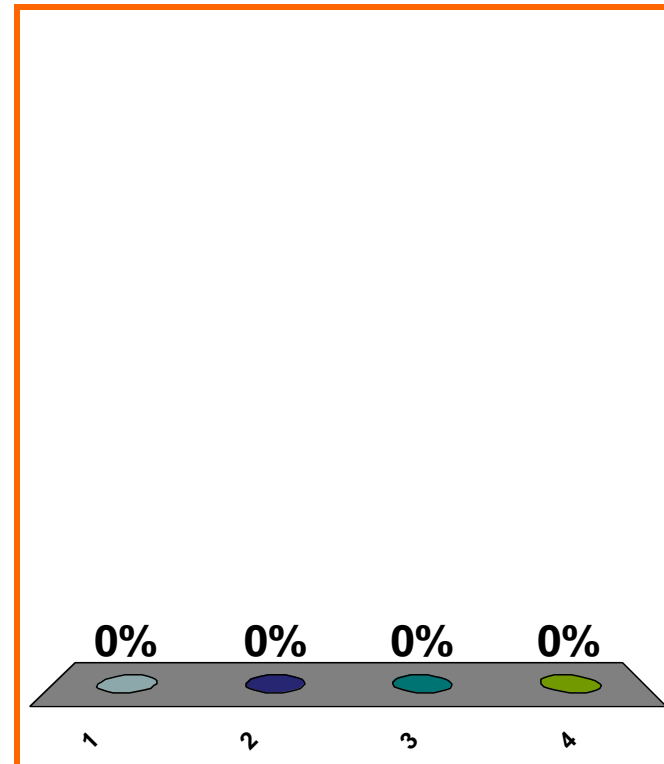
$$\lim_{x \rightarrow 0} \frac{3x^3 + 2x}{\sin x} = ??$$

(a) 0

(b) 2

(c) 3

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

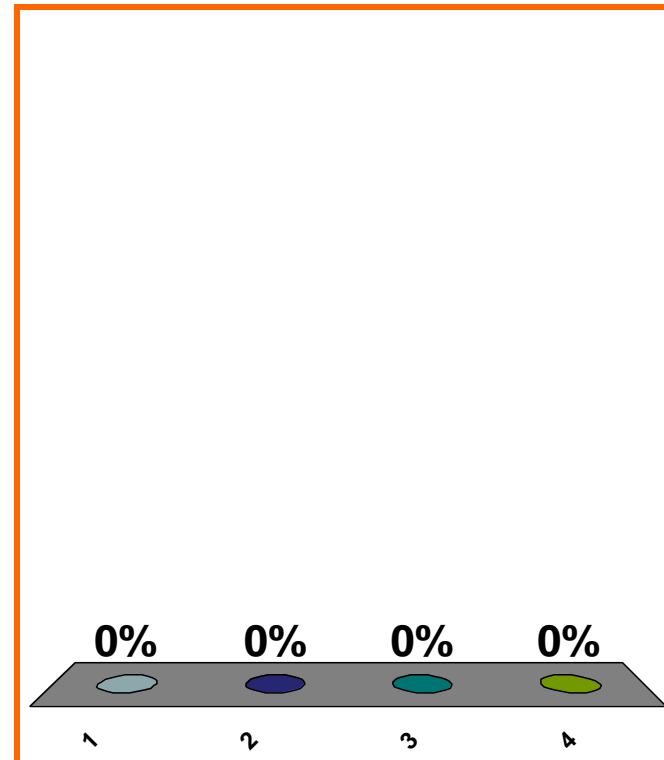
$$\lim_{x \rightarrow 2} \left( (\sin x) + \sqrt{x + 1} \right)$$

(a) DNE

(b)  $-\infty$

(c)  $(\sin 2) + \sqrt{3}$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$P(x) = (x - 3)^7 (x^2 + x + 4)$$

$$Q(x) = (x - 3)^8 (5x^9 + 9x - 7)$$

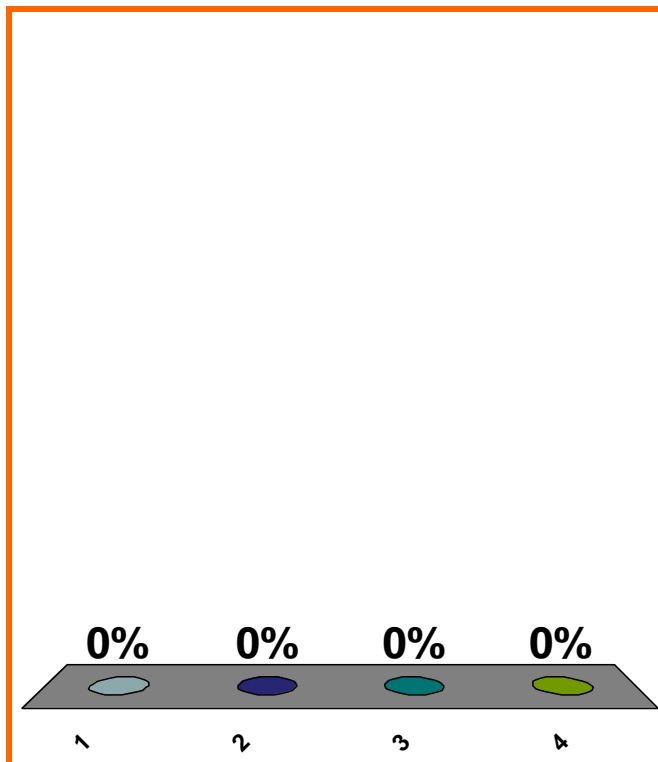
$$\lim_{x \rightarrow 3^+} \frac{P(x)}{Q(x)} = ??$$

(a) 0

(b)  $\infty$

(c)  $-\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
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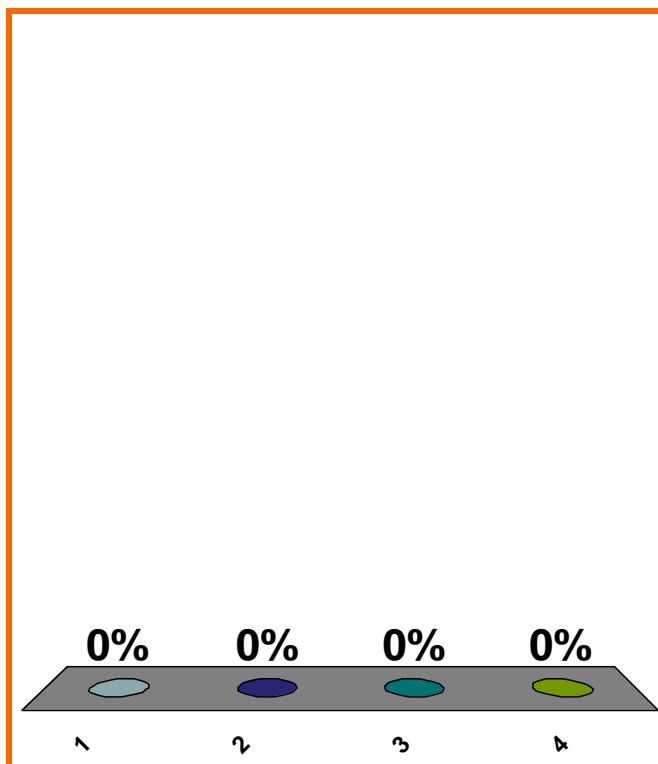
$$\lim_{x \rightarrow -1} \left[ \frac{x^2 + x}{2x + 5} \right]$$

(a) 1/3

(b) 0

(c) DNE

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$\lim_{t \rightarrow 0} \left[ \frac{2t^5 + 8t^4}{t^2(\sin^2 t)} \right]$$

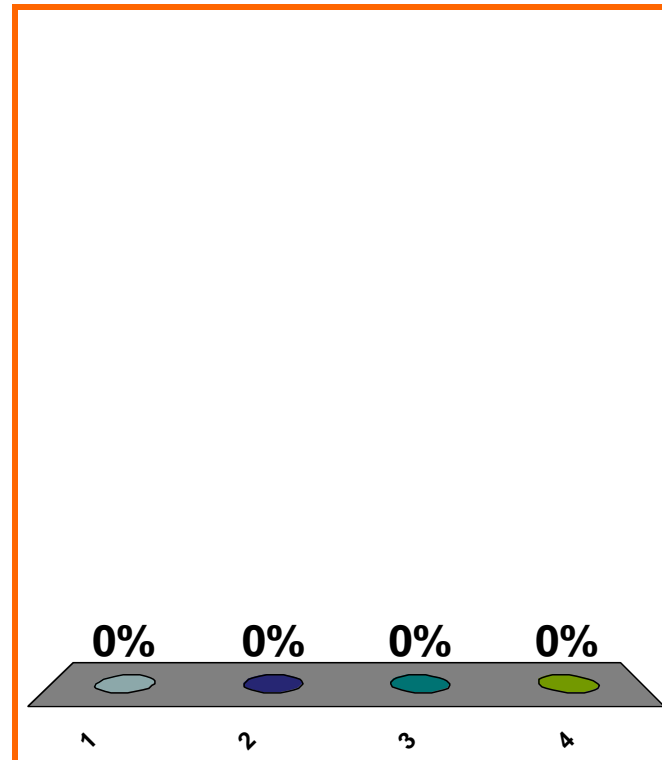
(a) 0

(b)  $\infty$

(c)  $-\infty$

(d) none of the above

Correct answer: 8



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
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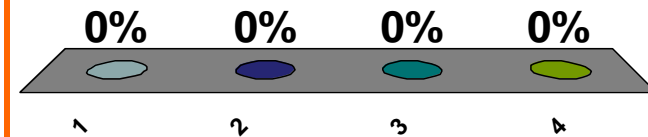
$$\lim_{x \rightarrow 2^-} f(x) = -\infty$$

(a)  $x \approx 2, x \neq 2 \Rightarrow f(x)$  very pos

(b)  $x \approx 2, x \neq 2 \Rightarrow f(x)$  very neg

(c)  $x \approx 2, x < 2 \Rightarrow f(x)$  very neg

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
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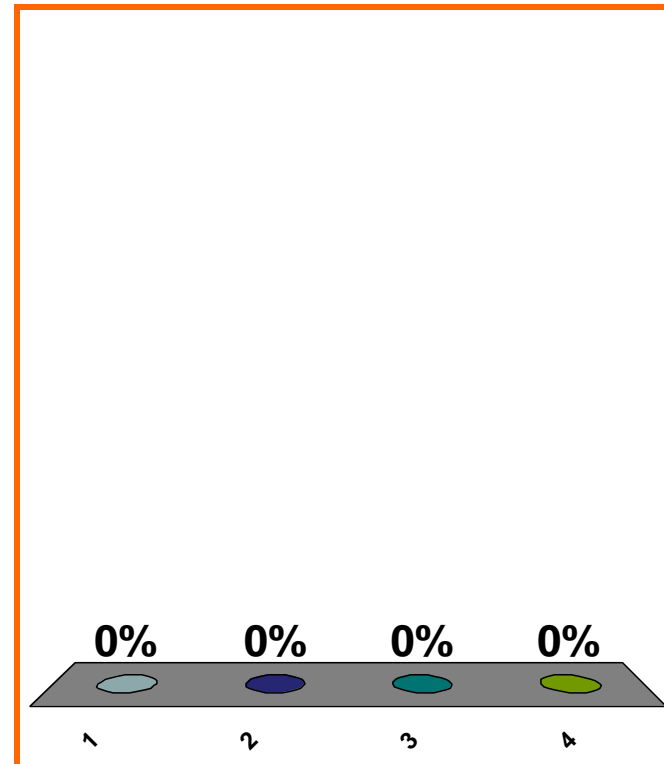
$$6x^5 + 7x^4 - 8x^3 \quad x \rightarrow 0 \quad ??$$

(a)  $6x^5$

(b)  $7x^4$

(c)  $-8x^3$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0240

0 pts

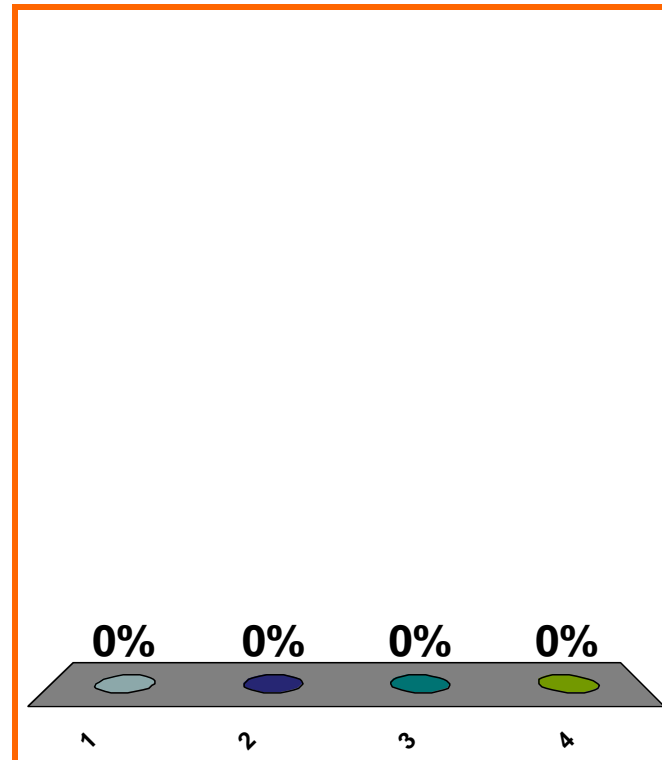
$$6x^5 + 7x^4 - 8x^3 \quad x \rightarrow \infty \quad ??$$

(a)  $6x^5$

(b)  $7x^4$

(c)  $-8x^3$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

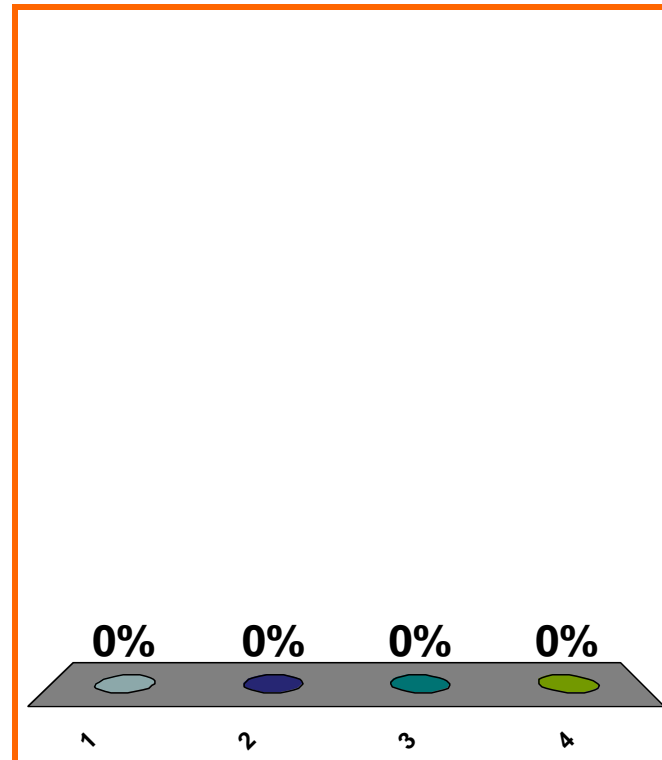
$$\lim_{x \rightarrow 0} \left[ \frac{6x^5 + 7x^4 - 8x^3}{7x^5 - 2x^4 + 9x^3} \right] = ??$$

(a) DNE

(b)  $-8/9$

(c)  $6/7$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0240

0 pts

20

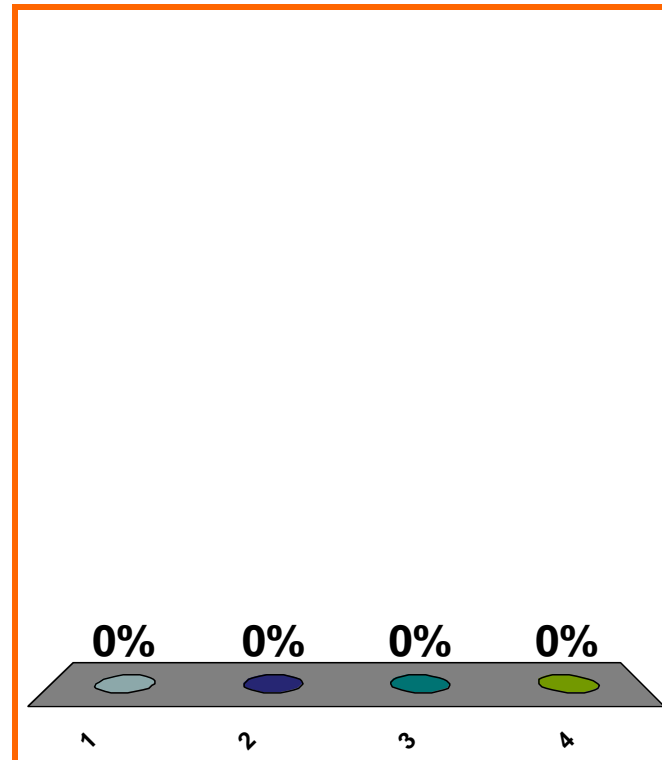
$$\lim_{x \rightarrow \infty} \left[ \frac{6x^5 + 7x^4 - 8x^3}{7x^5 - 2x^4 + 9x^3} \right] = ??$$

(a) DNE

(b)  $-8/9$

(c)  $6/7$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$\lim_{x \rightarrow \infty} \left[ \frac{6x^5 + 7x^4 - 8x^3}{7x^6 - 2x^4 + 9x^3} \right] = ??$$

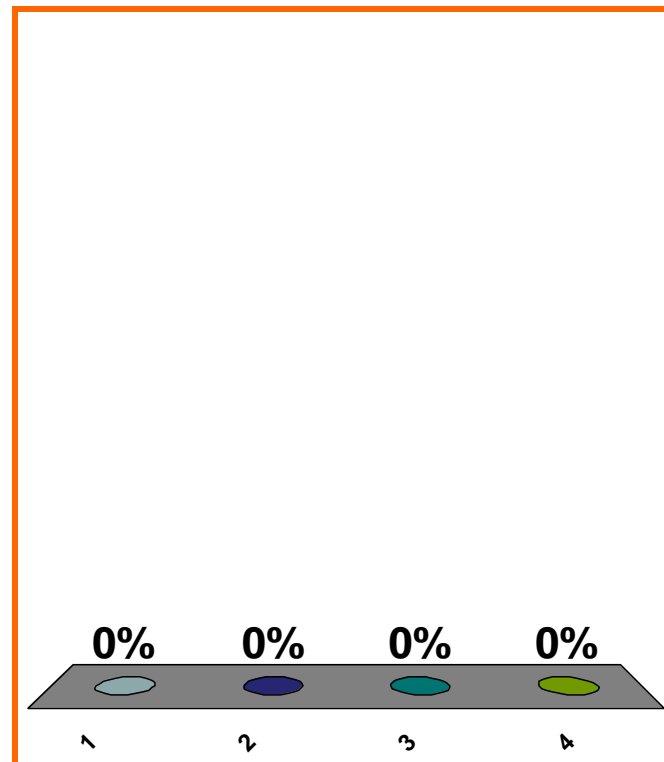
(a) DNE

(b)  $-8/9$

(c)  $6/7$

(d) none of the above

Correct answer: 0



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

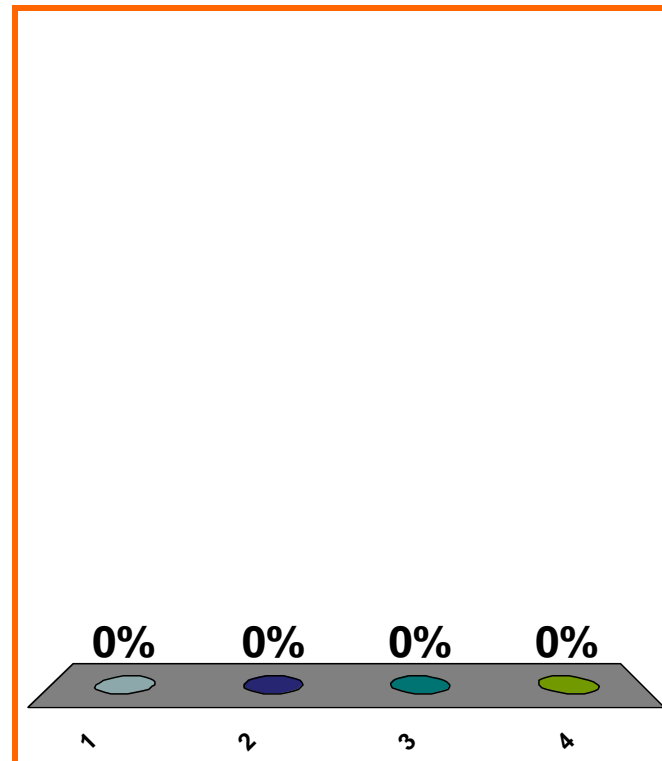
$$\lim_{x \rightarrow 0} \left[ \frac{6x^5 + 7x^4 - 8x^3}{7x^6 - 2x^4 + 9x^3} \right] = ??$$

(a) DNE

(b)  $-8/9$

(c)  $6/7$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0240

0 pts

23

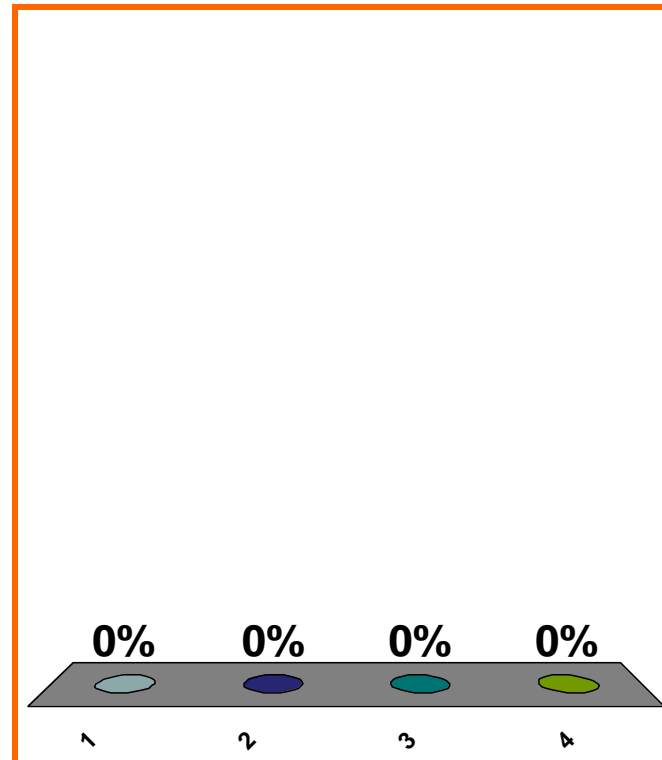
$$\sin x \underset{x \rightarrow 0}{\sim} ??$$

(a)  $x$

(b)  $\cos x$

(c)  $-\cos x$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0230

0 pts

24



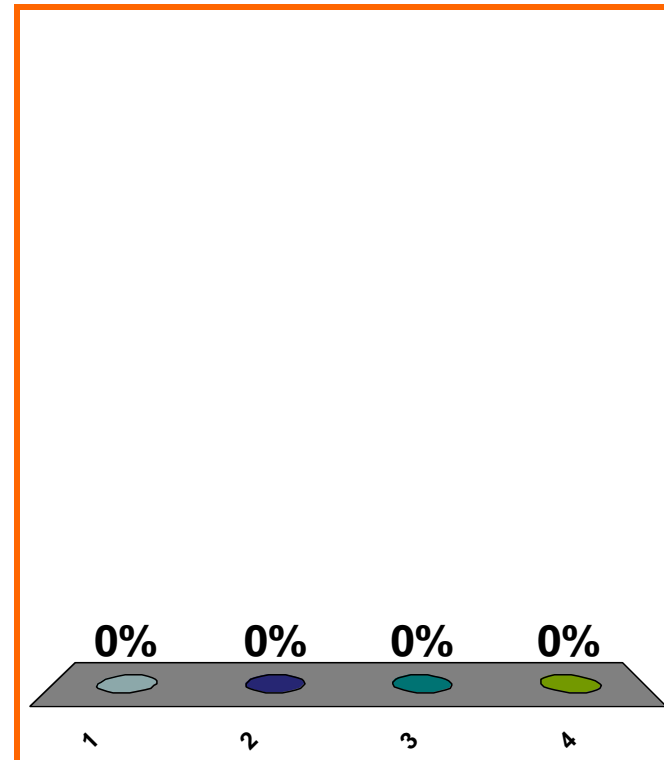
$$3x^3 + 2x \underset{x \rightarrow 0}{\sim} ??$$

(a)  $3x^3$

(b) 0

(c)  $2x$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

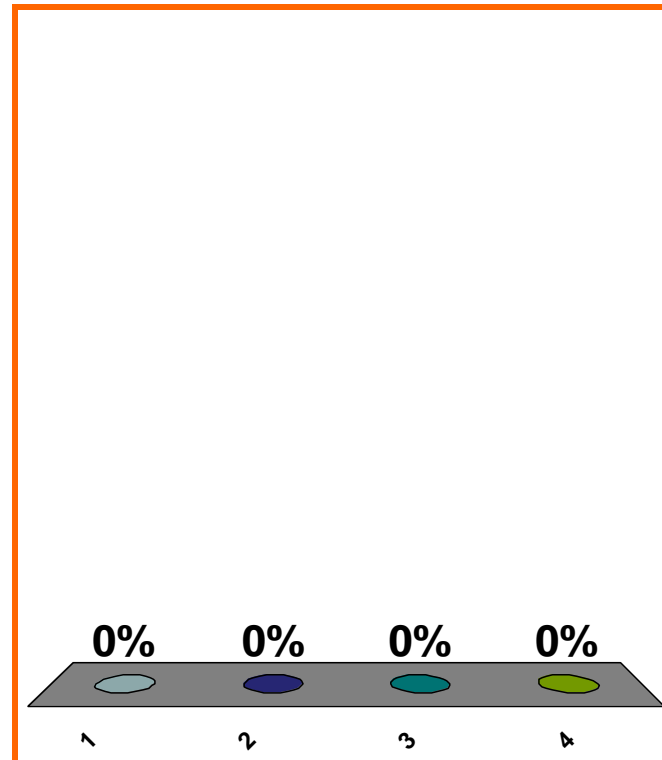
$$\lim_{x \rightarrow 0} \frac{3x^3 + 2x}{\sin x} = ??$$

(a) 0

(b) 2

(c) 3

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0140

0 pts

26

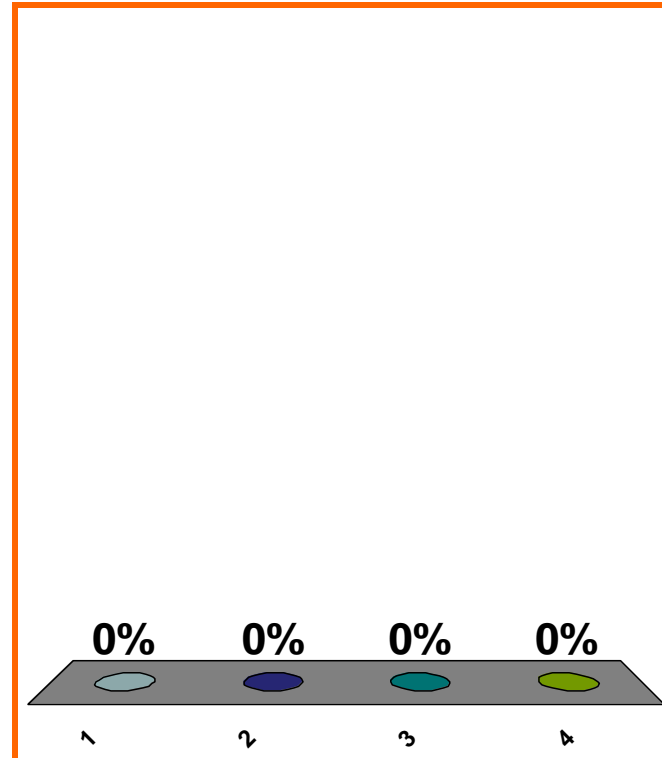
$$3x^3 + 2x \quad x \xrightarrow{\sim} \infty \quad ??$$

(a)  $3x^3$

(b) 0

(c)  $2x$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0230

0 pts

27

# LOOK AHEAD

practice chain rule

two problems with product, quotient, chain  
eq'n of a tangent line

From graph of  $f$  to domain of  $f'$

especially: from graph of  $\ln$  to domain of  $\ln'$

especially: from graph of  $x^{3/2}$  to domain  
of its derivative

continuity vs. continuity on interval

logarithmic derivatives

$$\lim_{h \rightarrow 0} \frac{|h|}{h}$$

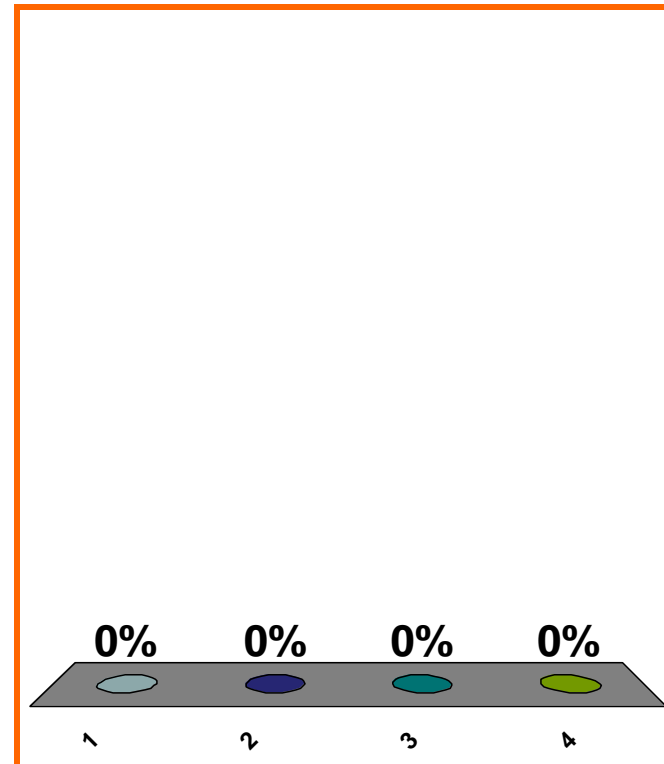
$$\ln(1 + (3/n)) \quad n \rightarrow \infty \quad ??$$

(a)  $1/n^2$

(b) 1

(c)  $3/n$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0420

0 pts

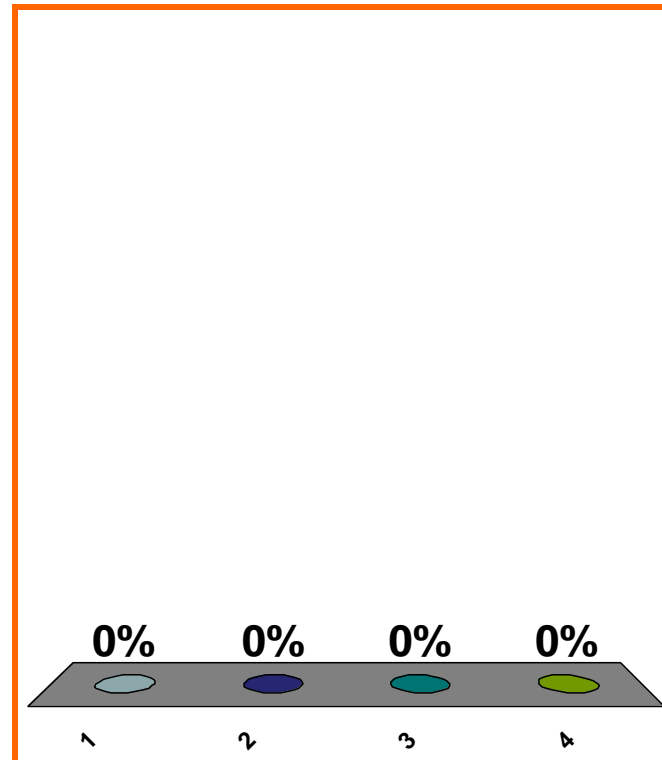
$$\ln(1 + 5x) \quad x \sim 0 \quad ??$$

(a)  $4x^2$

(b)  $5x$

(c) 1

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0420

0 pts

30

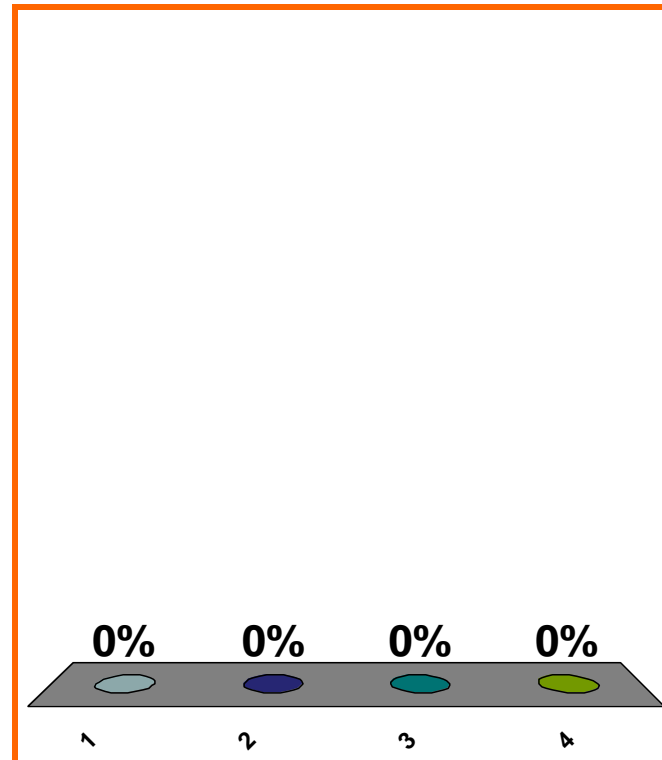
$$\ln(1 + 5x + 4x^2) \quad x \sim 0 \quad ??$$

(a)  $4x^2$

(b)  $5x$

(c) 1

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0420

0 pts

31

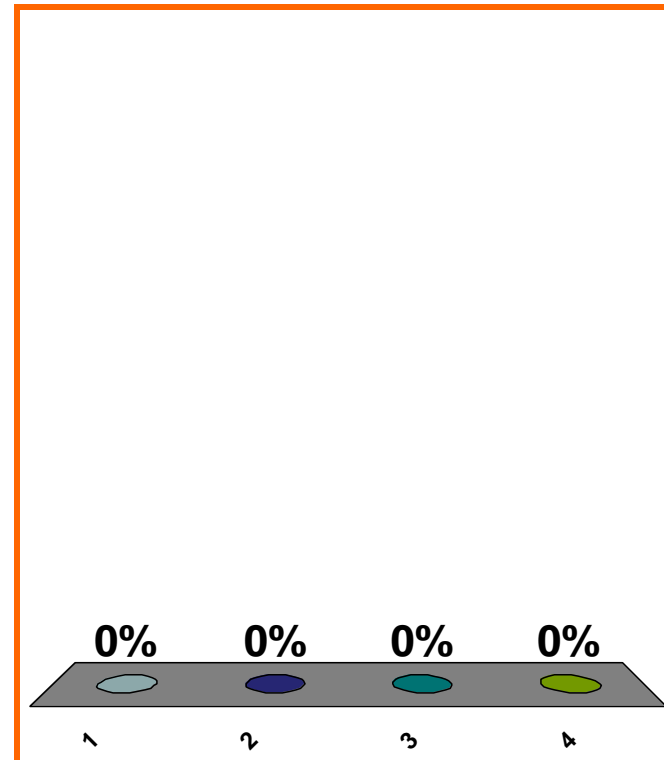
To get graph of  $y + 1 = x^3$ ,  
move graph of  $y = x^3$  ...

(a) right 1

(b) left 1

(c) down 1

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40



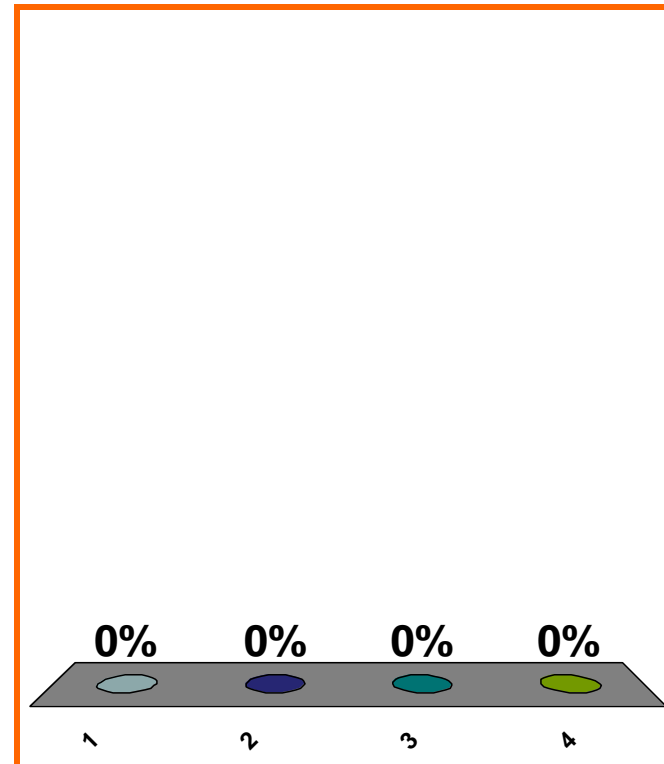
To get graph of  $y^2 = \sin(x + \pi)$ ,  
move graph of  $y^2 = \sin(x)$  ...

(a) right  $\pi$

(b) left  $\pi$

(c) down  $\pi$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0060

0 pts

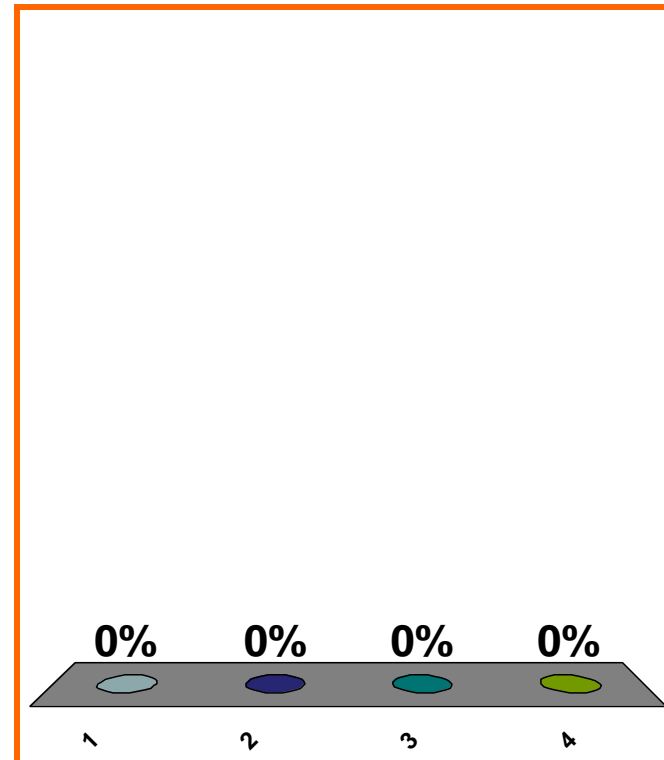
To get graph of  $y^2 = \sin(x - \pi)$ ,  
move graph of  $y^2 = \sin(x)$  ...

(a) right  $\pi$

(b) left  $\pi$

(c) down  $\pi$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

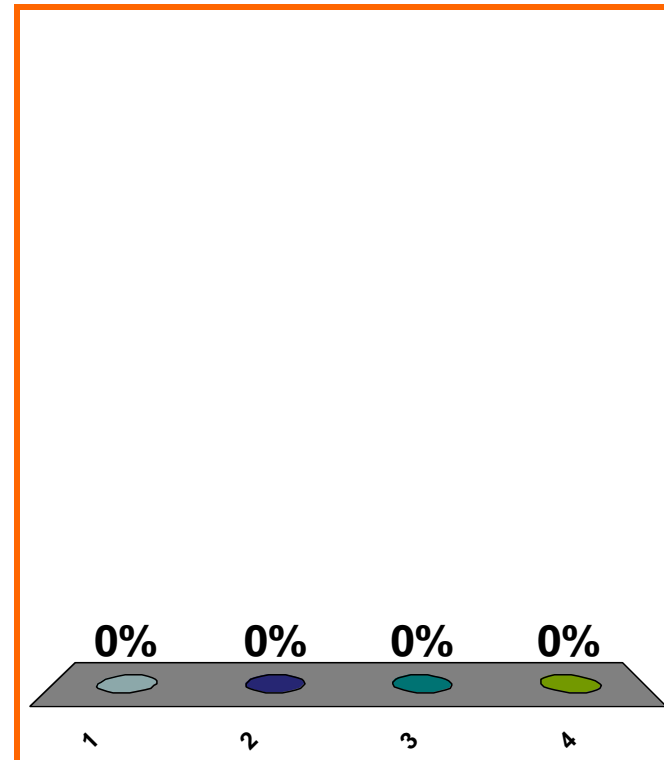
To get graph of  $(y + \pi)^2 = \sin(x)$ ,  
move graph of  $y^2 = \sin(x)$  ...

(a) right  $\pi$

(b) left  $\pi$

(c) down  $\pi$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

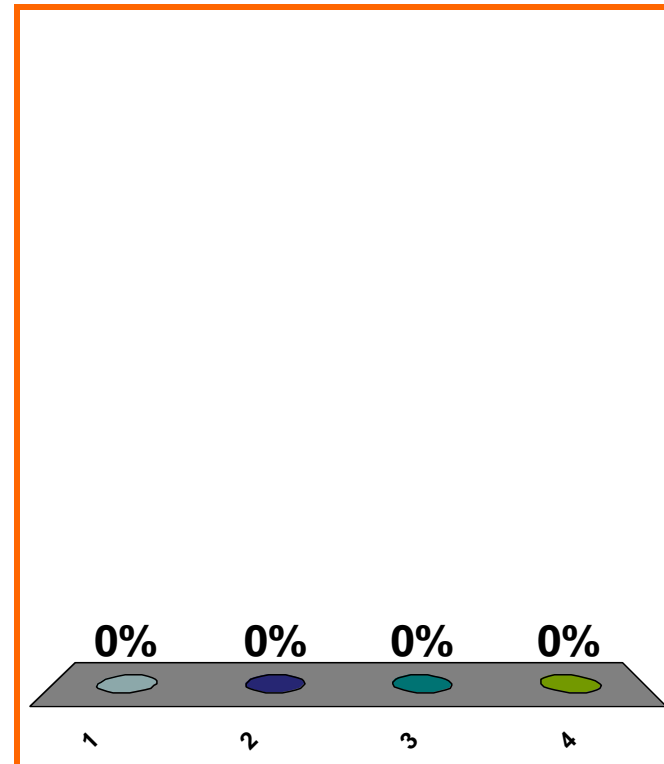
$$\sin(\pi/3) = ??$$

(a)  $\sqrt{2}/2$

(b)  $\sqrt{3}/2$

(c)  $1/2$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0090

0 pts

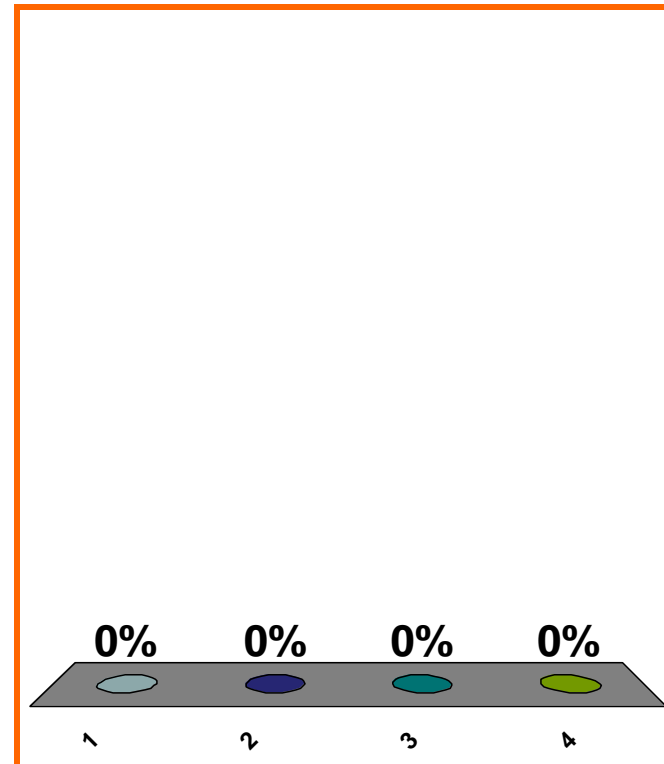
$$\arcsin(\sqrt{3}/2) = ??$$

(a)  $\pi/3$

(b)  $\pi/4$

(c)  $\pi/6$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0110

0 pts

37

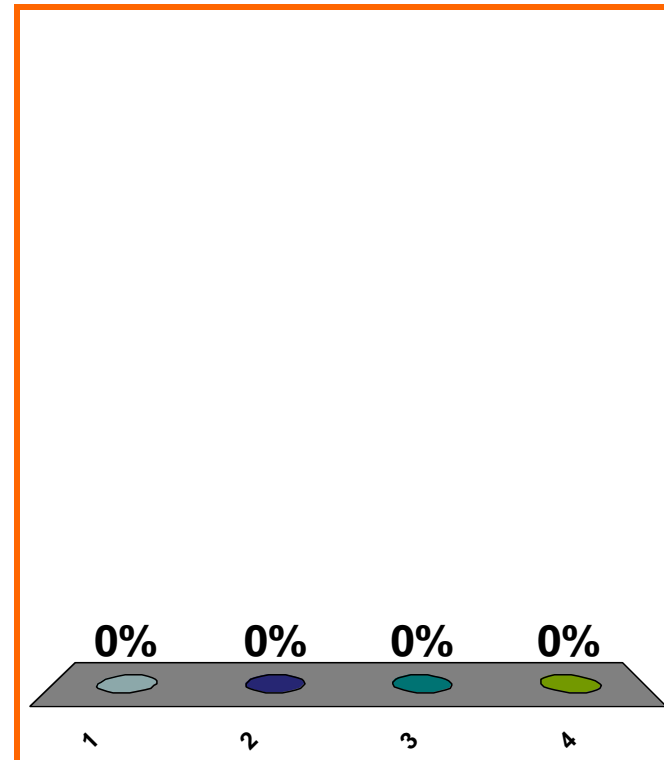
$$\sin(3\pi/4) = ??$$

(a)  $\sqrt{2}/2$

(b)  $-\sqrt{2}/2$

(c)  $1/2$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

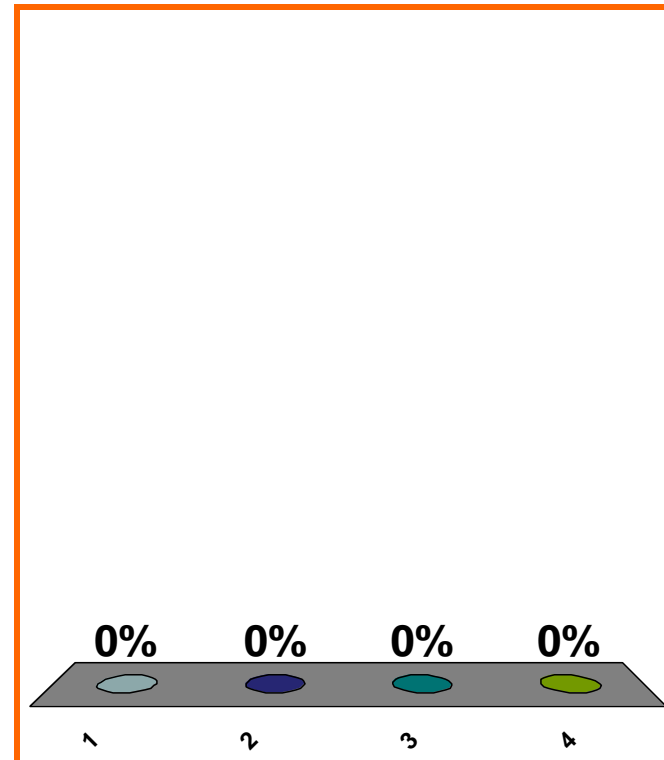
$$\arcsin(\sqrt{2}/2) = ??$$

(a)  $\pi/3$

(b)  $\pi/4$

(c)  $\pi/6$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

0 of 5

Topic 0110

0 pts

39

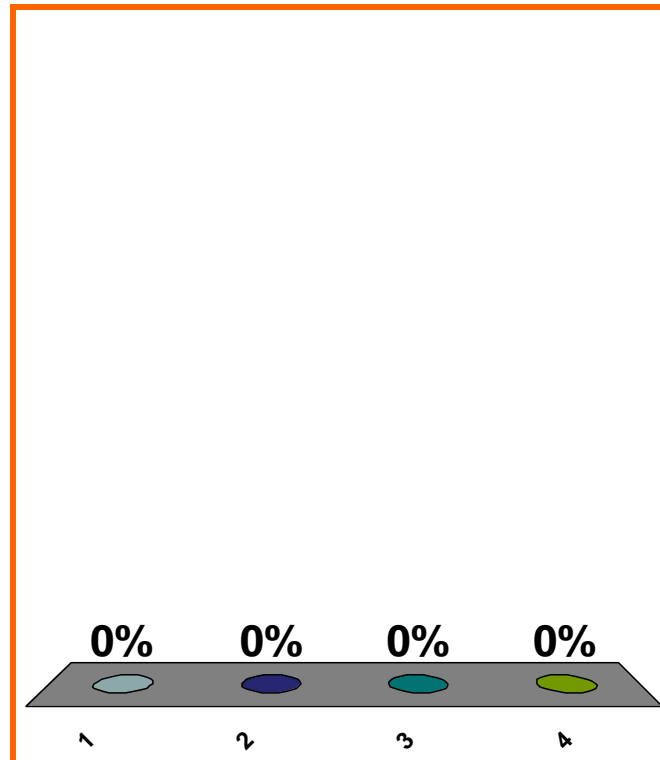
$$\frac{d}{dx} [(x^2)(\sin x)] = ??$$

(a)  $(2x)(\cos x)$

(b)  $(2x)(-\cos x)$

(c)  $(2x)(\sin x) + (x^2)(\cos x)$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0340

0 pts

40



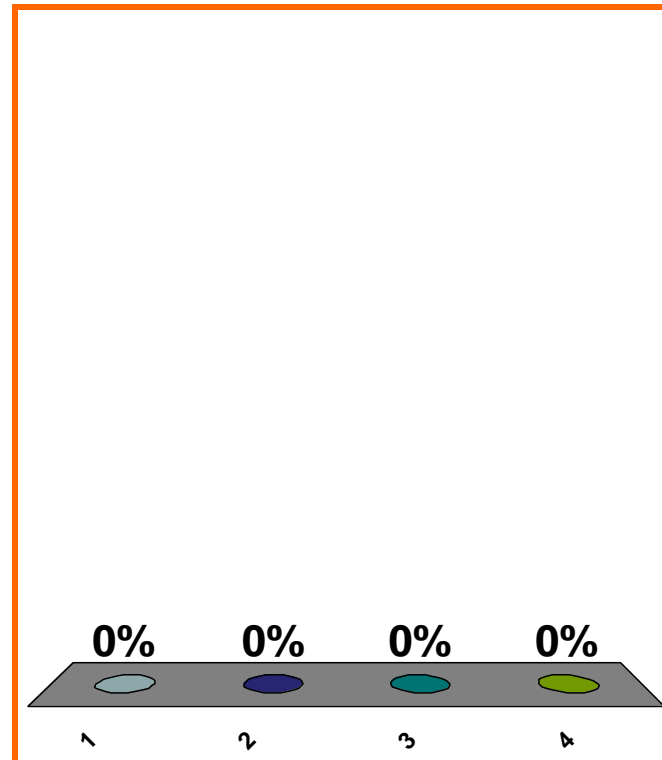
$$\frac{d}{dx} \left[ \frac{\sin x}{x} \right] = ??$$

(a)  $\frac{(\sin x)(1) - (x)(\cos x)}{x}$

(b)  $\frac{(\sin x)(1) - (x)(\cos x)}{x^2}$

(c)  $\frac{(x)(\cos x) - (\sin x)(1)}{x^2}$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0350

0 pts

41

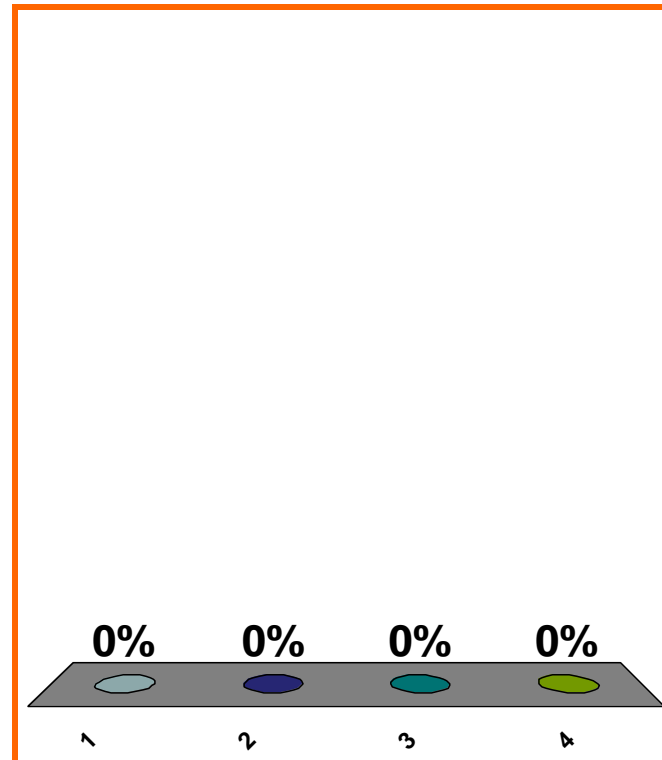
$$\lim_{x \rightarrow 5} (3x^3 - 2x + 8)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

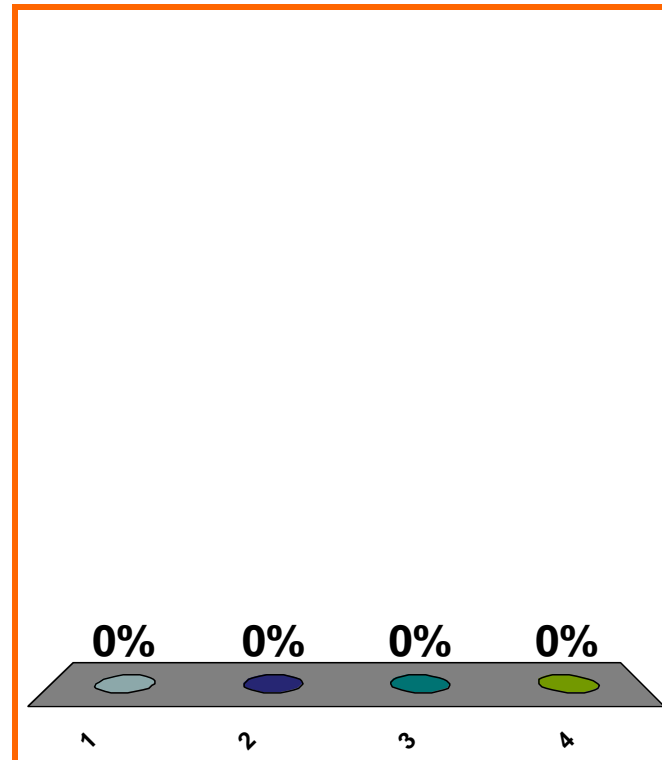
$$\lim_{x \rightarrow 5} \left( \frac{3x^3 - 2x + 8}{x - 4} \right)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

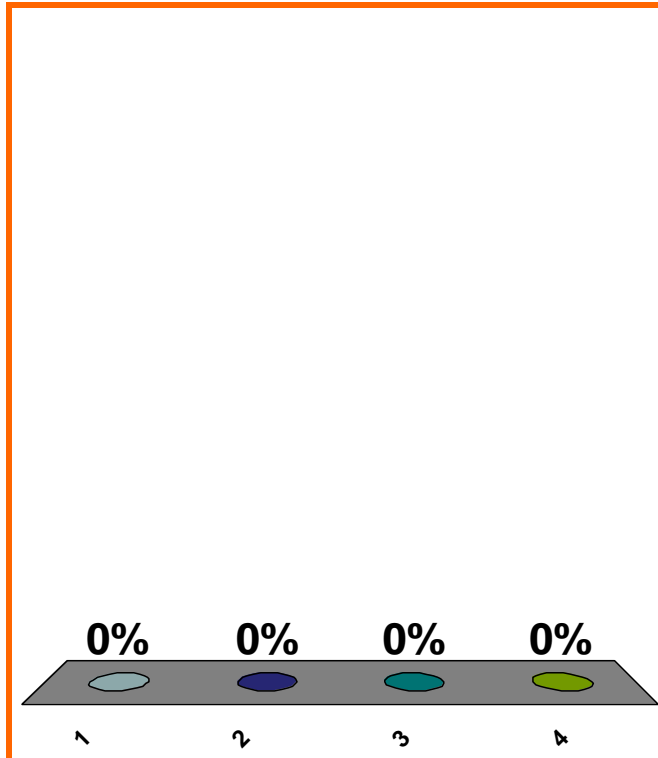
$$\lim_{x \rightarrow 5^+} \left( \frac{3x^3 - 2x + 8}{x - 5} \right)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

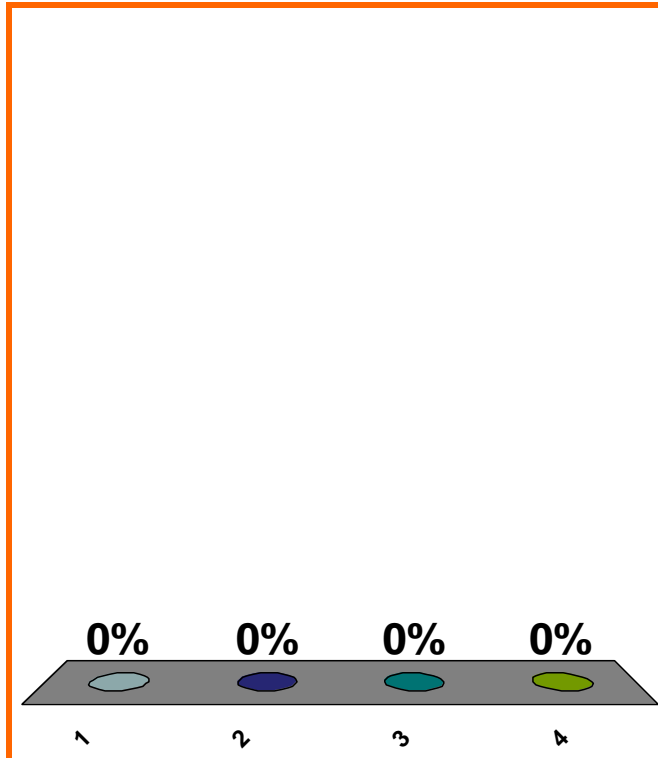
$$\lim_{x \rightarrow 5^-} \left( \frac{3x^3 - 2x + 8}{x - 5} \right)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0250

0 pts

45

$$\lim_{x \rightarrow 5} \left( \frac{3x^3 - 2x + 8}{x - 5} \right)$$

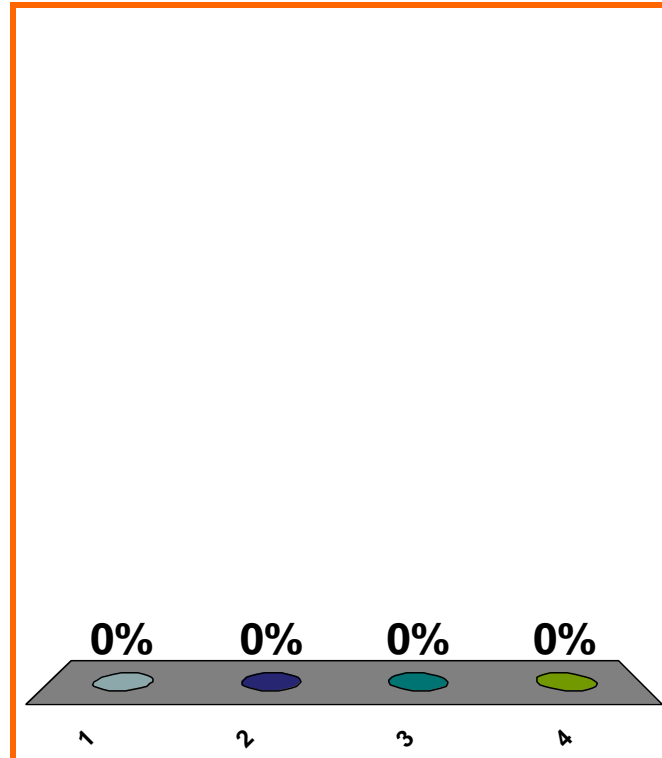
(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above

Correct answer: DNE



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

0170-1. Use the graph of  $f$  given below to find the value of each quantity, if it exists.

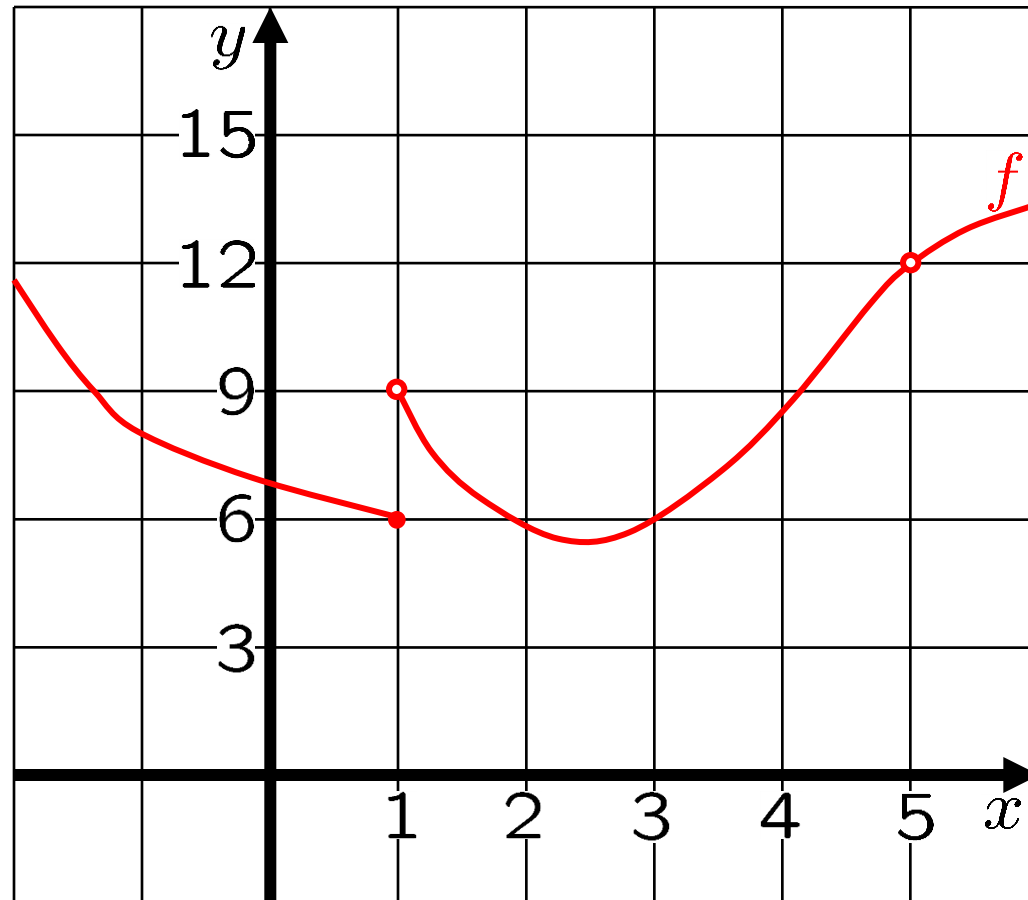
(a)  $\lim_{x \rightarrow 1^-} f(x)$

(b)  $\lim_{x \rightarrow 1^+} f(x)$

(c)  $\lim_{x \rightarrow 1} f(x)$

(d)  $\lim_{x \rightarrow 5} f(x)$

(e)  $f(5)$



0170-2. Use the graph of  $f$  given below to find the value of each quantity, if it exists.

(a)  $\lim_{x \rightarrow 1^-} f(x)$

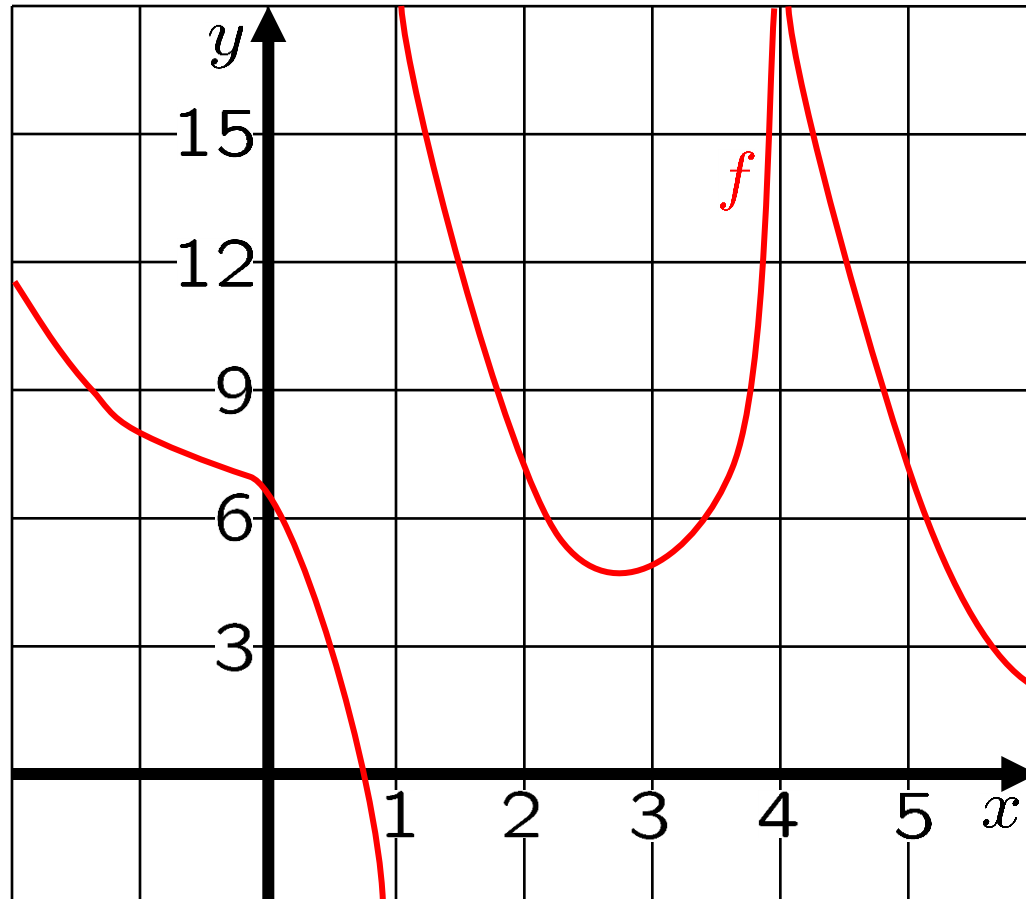
(b)  $\lim_{x \rightarrow 1^+} f(x)$

(c)  $\lim_{x \rightarrow 1} f(x)$

(d)  $\lim_{x \rightarrow 4^-} f(x)$

(e)  $\lim_{x \rightarrow 4^+} f(x)$

(f)  $\lim_{x \rightarrow 4} f(x)$





0170-3. Show a graph of a function  $h$  s.t.

OLD

$$\lim_{x \rightarrow 2^-} h(x) = 7, \quad \lim_{x \rightarrow 2^+} h(x) = 6, \quad h(2) = 5,$$

$$\lim_{x \rightarrow 3} h(x) = -\infty,$$

$$\lim_{x \rightarrow 4^-} h(x) = \infty, \quad \lim_{x \rightarrow 4^+} h(x) = -\infty,$$

$$\lim_{x \rightarrow -\infty} h(x) = -3 \quad \text{and} \quad \lim_{x \rightarrow \infty} h(x) = 1.$$

0170-5. a. Compute  $\lim_{x \rightarrow 1^-} \frac{2x + 3}{x - 1}$ ,

or explain why the limit  
does not exist.

b. Compute  $\lim_{x \rightarrow 1^+} \frac{2x + 3}{x - 1}$ ,

or explain why the limit  
does not exist.

c. Compute  $\lim_{x \rightarrow 1} \frac{2x + 3}{x - 1}$ ,

or explain why the limit  
does not exist.

tangent slopes for  $y = x^3$ , esp. at  $x = 5$ .

$$\lim_{h \rightarrow 0} \frac{(5 + h)^3 - 5^3}{h}$$

$$\lim_{\Delta x \rightarrow 0} \frac{(5 + \Delta x)^3 - 5^3}{\Delta x}$$

## LOOK AHEAD

differentiate polynomials

differentiate all 6 trig functions

$$\lim_{x \rightarrow 0} [\sin(1/x)]$$

$$\lim_{x \rightarrow 0} [x(\sin(1/x))]$$

$$\lim_{x \rightarrow 0} \left[ \frac{2x^3 + x^2}{8x^5 + 3x^4 - 7x^3} \right]$$

SAVE THE  
SESSION  
DATA

RETURN TO  
PRESENTATION