

# Calculus

M 6 February 2012

RESET THE  
SESSION

SET THE  
PARTICIPANT  
LIST

PLUG IN THE  
RECEIVER

Boxed answers agree with  
TurningPoint answers

Points agree with  
TurningPoint points

Points total to 100

Topics covered are in bounds

QUIZ  
FOLLOWS

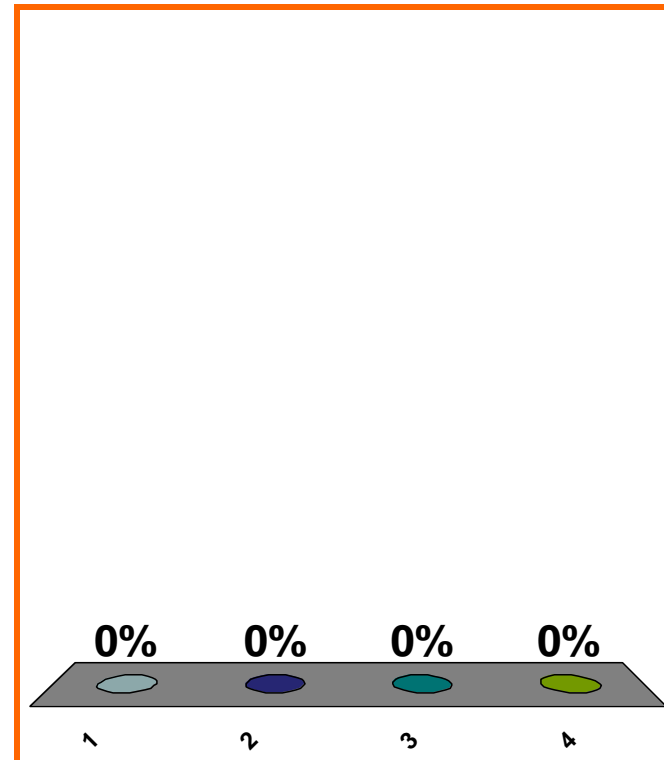
line's slope = 8  
goes through (2, 7)  
equation?

(a)  $x - 7 = 8(y - 2)$

(b)  $y - 7 = 8(x - 2)$

(c)  $y - 8 = 7(x - 2)$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

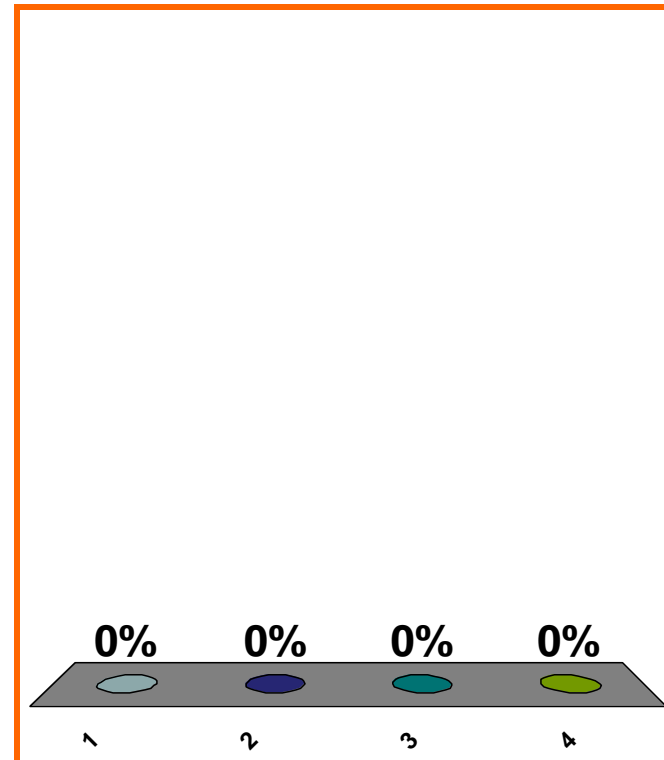
line's slope = 8  
goes through (2, 7)  
equation?

(a)  $x = 7 + 8(y - 2)$

(b)  $y = 7 + 8(x - 2)$

(c)  $y = 8 + 7(x - 2)$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

tangent line to  $y = f(x)$  at  $(2, 7)$

$$y - 7 = 8(x - 2)$$

“linearization” of  $f(x)$  at  $x = 2$ ?

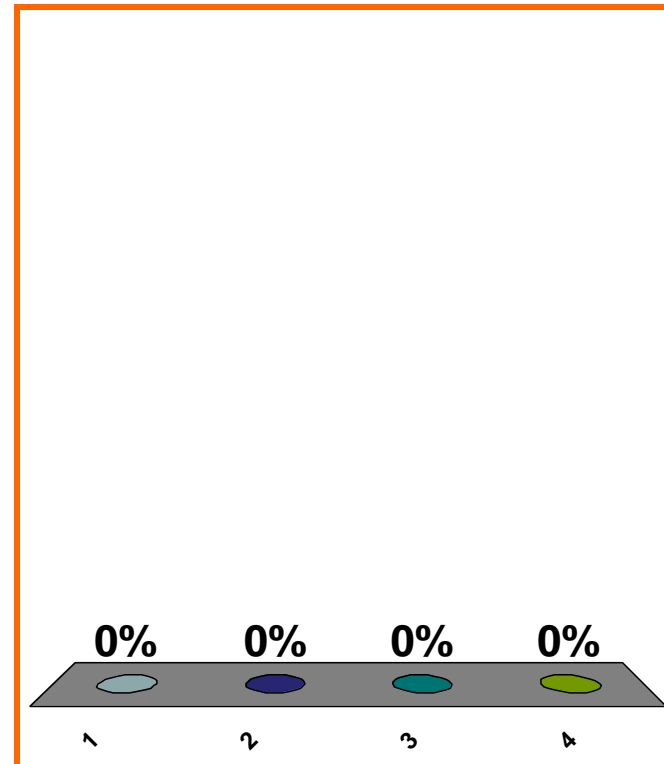
(a) 8

(b) 7

(c)  $8(x - 2)$

(d) none of the above

Correct answer:  $7 + 8(x - 2)$



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
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$$y = \sin x$$

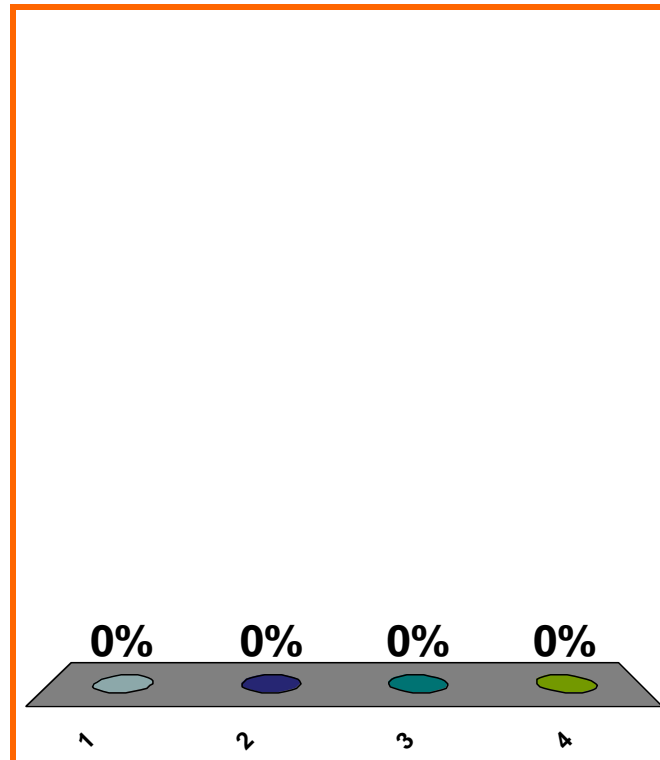
$$\Delta y = ??$$

(a)  $[\sin(x + \Delta x)]$

(b)  $[\sin(x + \Delta x)] - [\sin x]$

(c)  $\frac{[\sin(x + \Delta x)] - [\sin x]}{\Delta x}$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40



$$P(x) = (x - 3)^6(x^2 + x + 4)$$

$$Q(x) = (x - 3)^8(5x^9 + 9x - 7)$$

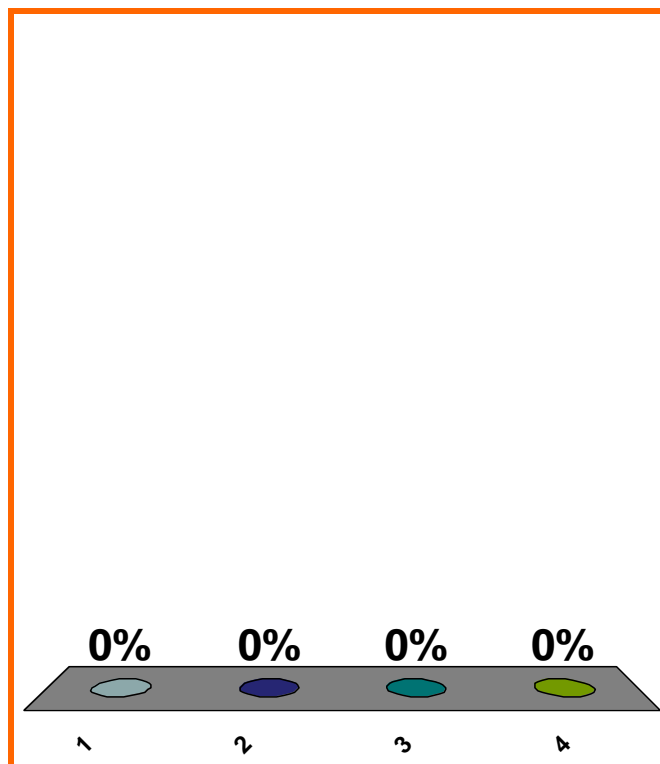
$$\lim_{x \rightarrow 3^-} \frac{P(x)}{Q(x)} = ??$$

(a) 0

(b)  $\infty$

(c)  $-\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0200

10 pts

9

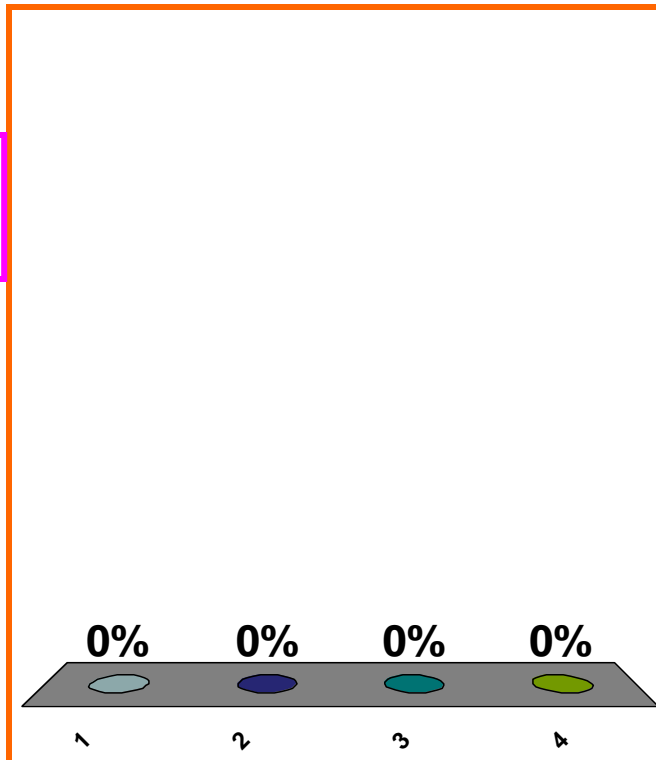
$$\lim_{x \rightarrow 2} f(x) = -\infty$$

(a)  $x \approx 2 \Rightarrow f(x)$  very neg

(b)  $x \approx 2, x \neq 2 \Rightarrow f(x)$  very neg

(c)  $x \approx 2, x < 2 \Rightarrow f(x)$  very neg

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0150

10 pts

10

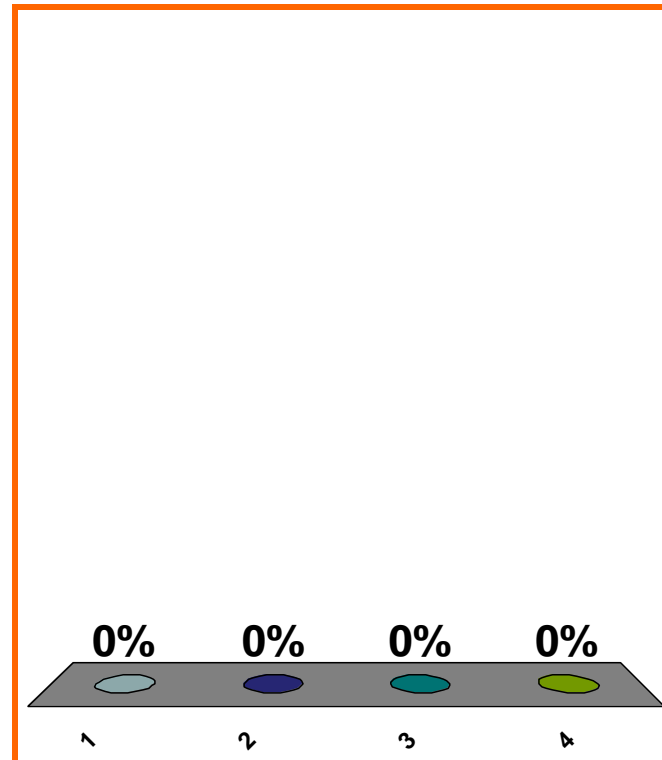
$$\lim_{x \rightarrow 0} \left[ \frac{6x^5 + 7x^4 - 8x^3}{7x^5 - 2x^4 + 9x^3} \right] = ??$$

(a) DNE

(b)  $-8/9$

(c)  $6/7$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0240

10 pts

11

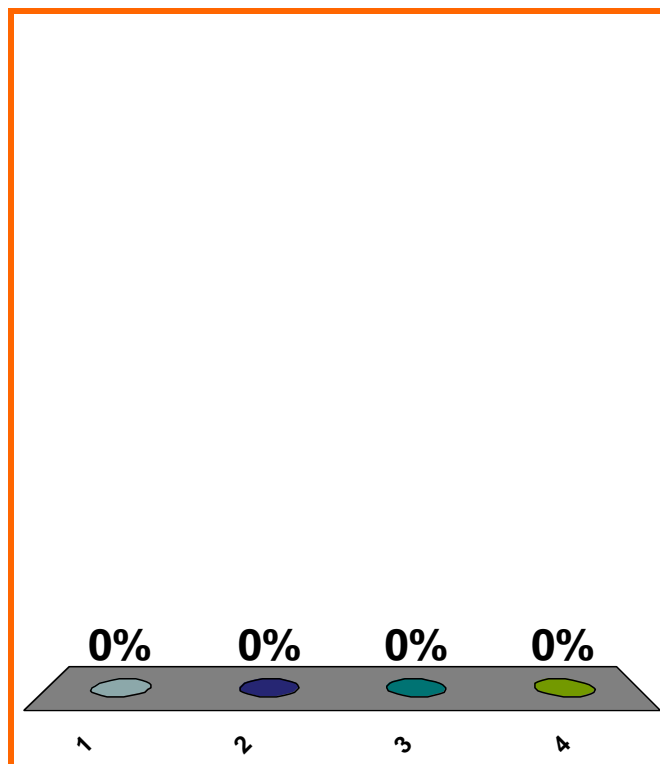
$$\lim_{x \rightarrow \infty} \left[ \frac{6x^5 + 7x^4 - 8x^3}{7x^5 - 2x^4 + 9x^3} \right] = ??$$

(a) DNE

(b)  $-8/9$

(c)  $6/7$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0240

10 pts

12

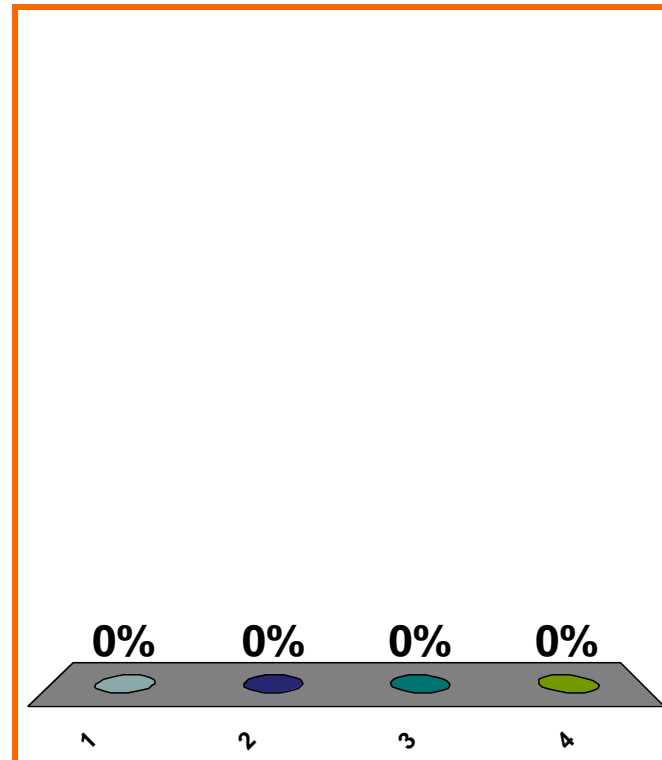
$$\lim_{x \rightarrow 0} \frac{3x^3 + 2x}{\sin x} = ??$$

(a) 0

(b) 2

(c) 3

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0140

10 pts

13

$$\sqrt{x^2 + 1} \sim ??$$

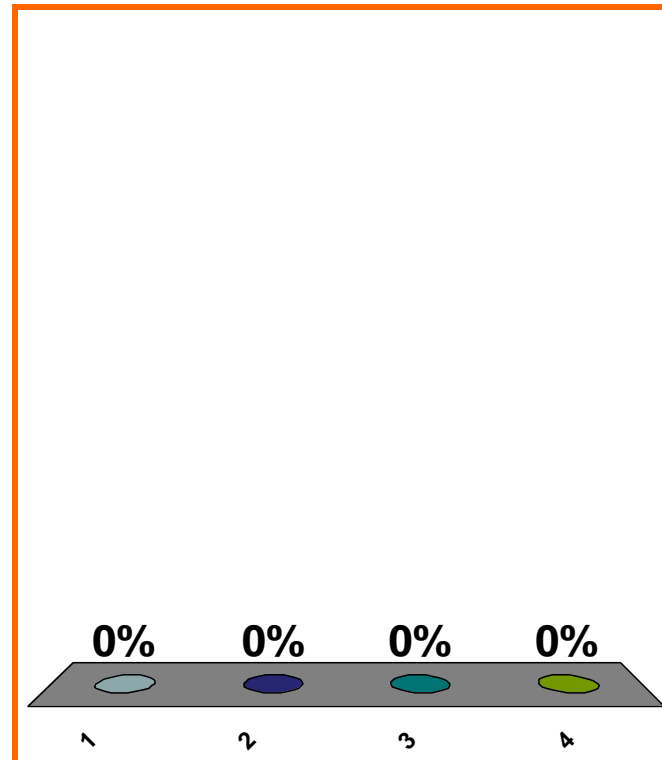
$x \rightarrow \infty$

(a) 1

(b)  $x$

(c)  $-x$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$\sqrt{x^2 + 1} \sim \text{??}$$

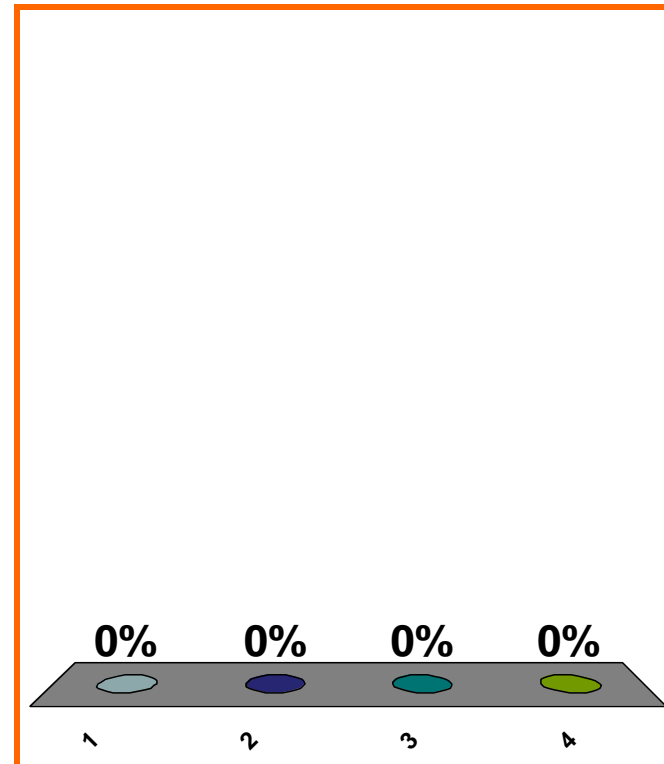
$x \rightarrow -\infty$

(a) 1

(b)  $x$

(c)  $-x$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

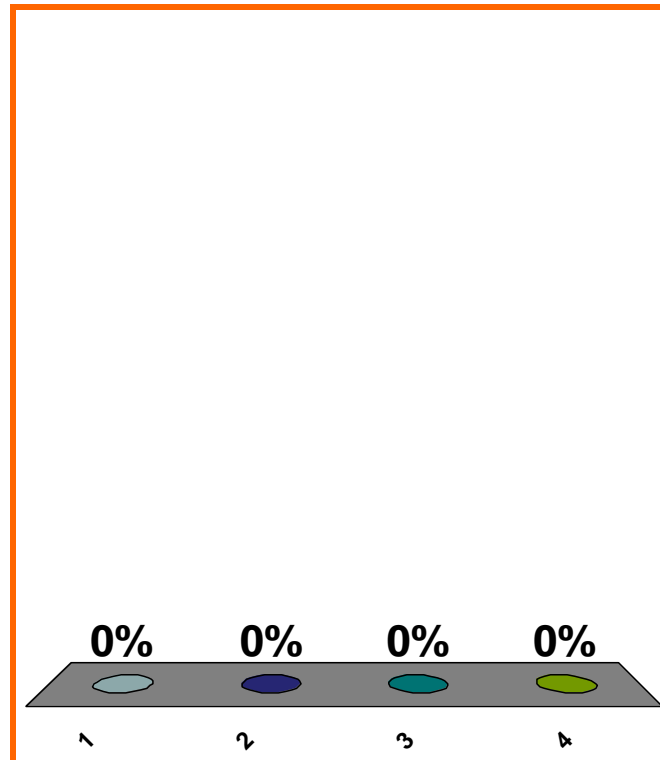
$$\lim_{x \rightarrow \infty} \left[ \frac{\sqrt{x^2 + 1}}{3x} \right] = ??$$

(a) DNE

(b) 1/3

(c) -1/3

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0240

10 pts

16



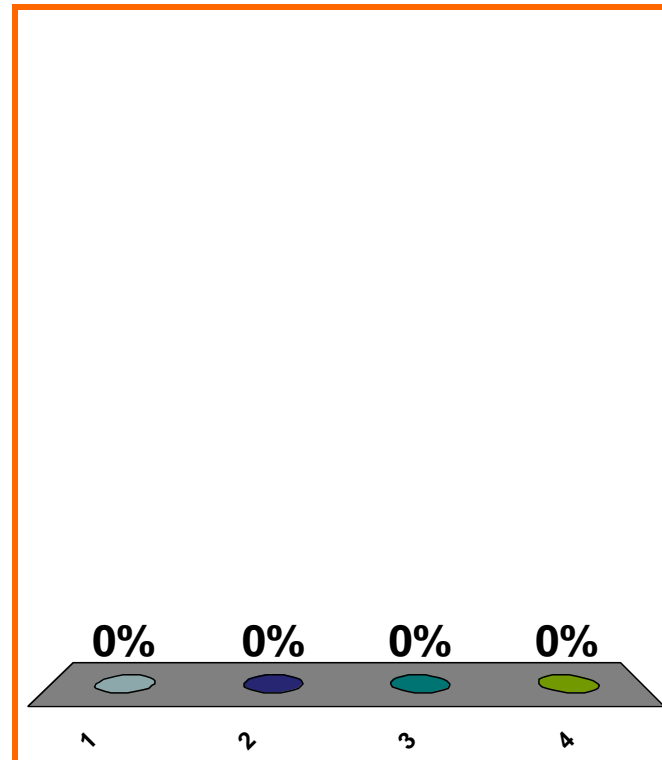
$$\lim_{x \rightarrow -\infty} \left[ \frac{\sqrt{x^2 + 1}}{3x} \right] = ??$$

(a) DNE

(b)  $1/3$

(c)  $-1/3$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

continuity vs. continuity on interval  
differentiability vs. diff. on open interval

## LOOK AHEAD

$(d/dt)(\text{expr of } u, v)$ , etc.

deriv. of inv. trig fn

From graph of  $f$  to domain of  $f'$

especially: from graph of  $\ln$  to domain of  $\ln'$

especially: from graph of  $x^{3/2}$  to domain  
of its derivative

logarithmic derivatives

$$\lim_{h \rightarrow 0} \frac{|h|}{h}$$

$$f(1) = 200$$
$$f(3) = 800$$

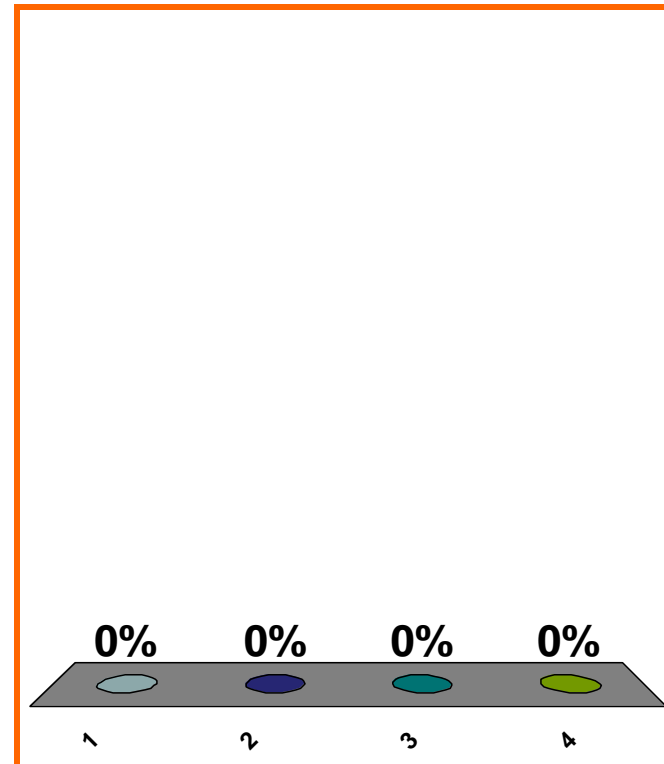
avg rate of change?

(a)  $(800 - 200)/(3 - 1)$

(b)  $(3 - 1)/(800 - 200)$

(c)  $(200 - 800)/(3 - 1)$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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$$f(1) = 200$$

$$f(3) = 800$$

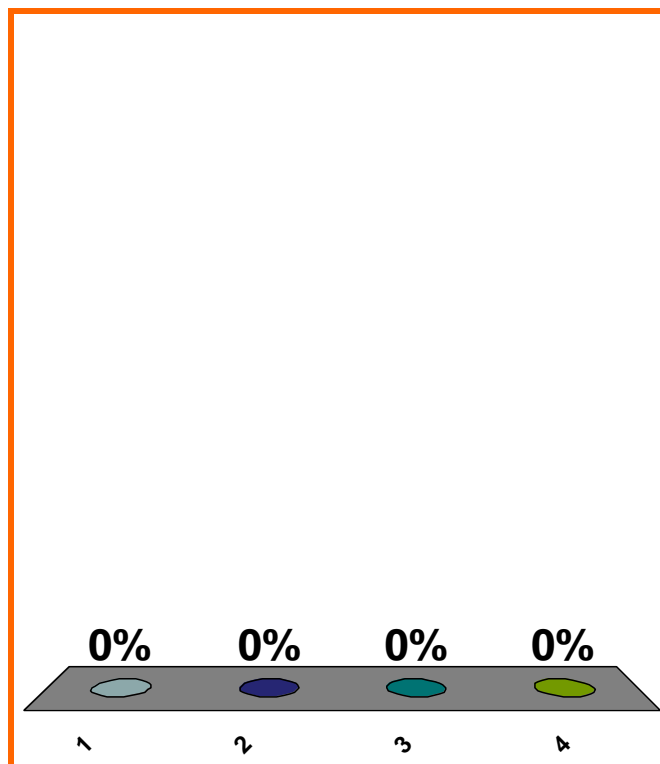
avg rate of change?

(a)  $(200 - 800)/(1 - 3)$

(b)  $(1 - 3)/(200 - 800)$

(c)  $(800 - 200)/(1 - 3)$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$f(x) = x^6/6, \quad f'(x) = x^5$$

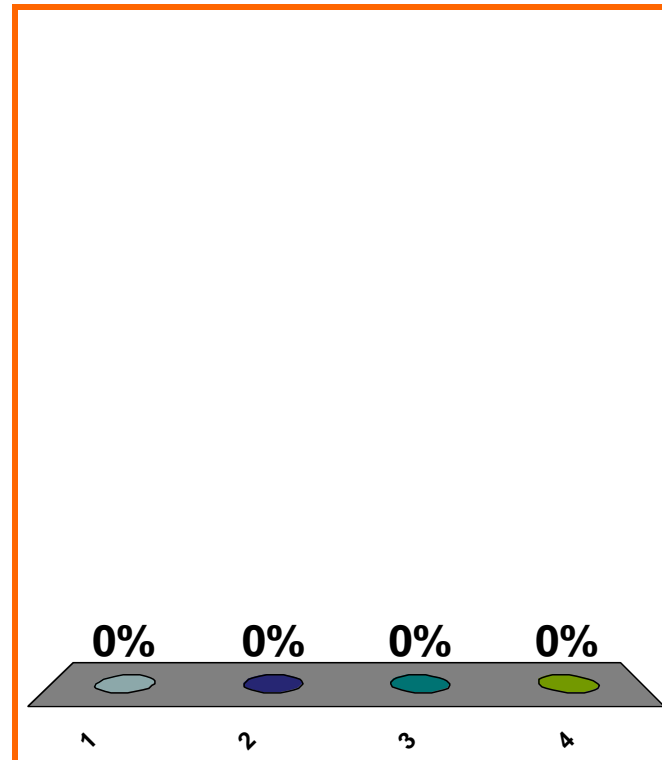
slope of tan. line at  
(2, 2<sup>6</sup>/6)

(a) 2<sup>6</sup>/6

(b) (2<sup>6</sup>/6)<sup>5</sup>

(c) 2<sup>5</sup>

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$\lim_{x \rightarrow \infty} \left[ \frac{100x^3 + 2x - 1}{x^4 - x^3 + x^2 + 1} \right] = ??$$

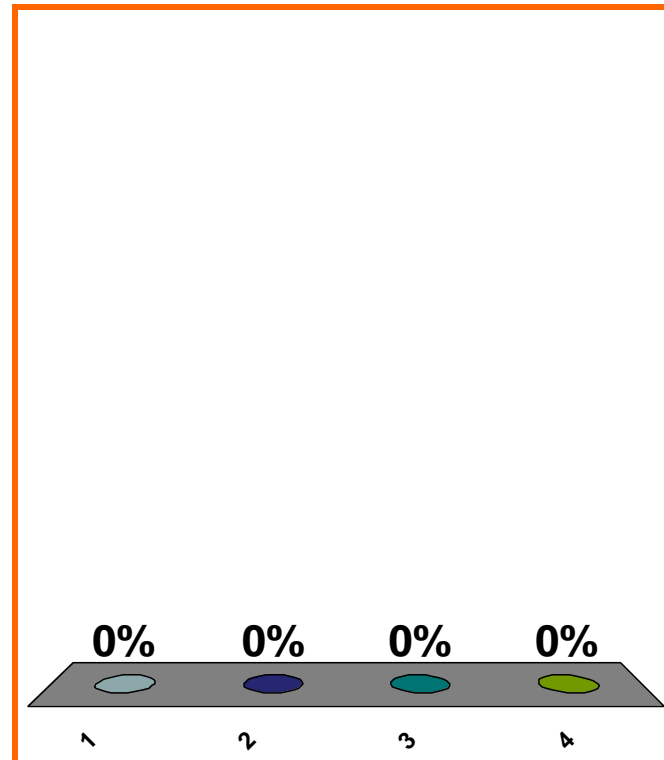
(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above

Correct answer: 0



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$\lim_{x \rightarrow -\infty} \left[ \frac{100x^3 + 2x - 1}{x^4 - x^3 + x^2 + 1} \right] = ??$$

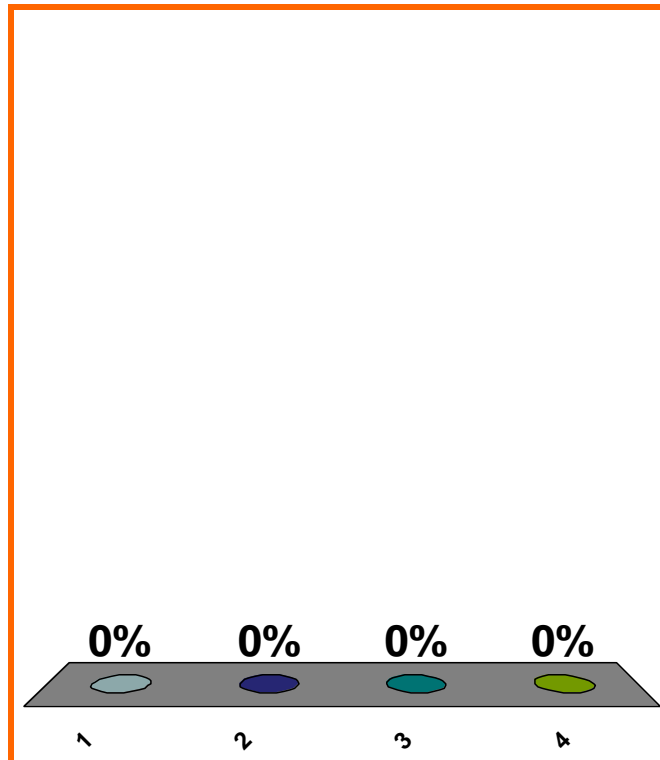
(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above

Correct answer: 0



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

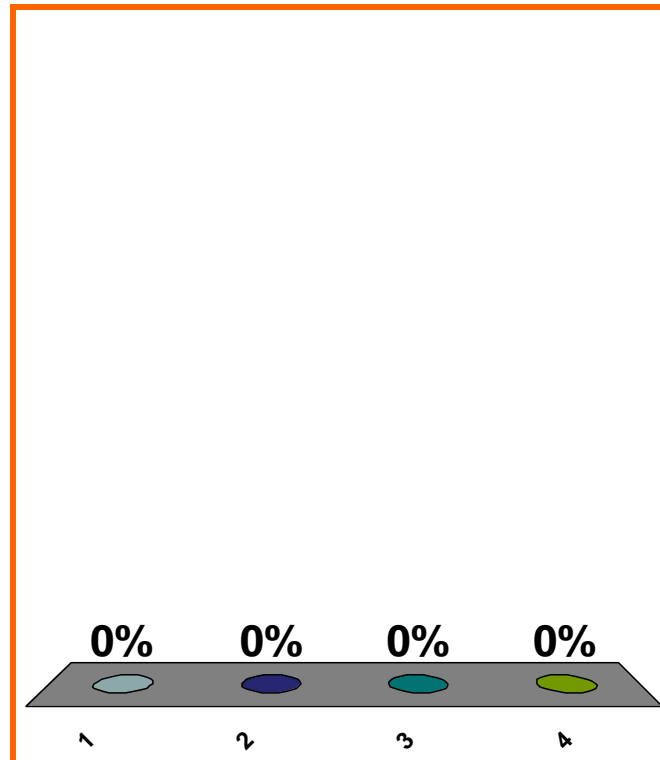
$$\lim_{x \rightarrow -\infty} \left[ \frac{100x^3 + 2x - 1}{x^3 + x^2 + 1} \right] = ??$$

(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40



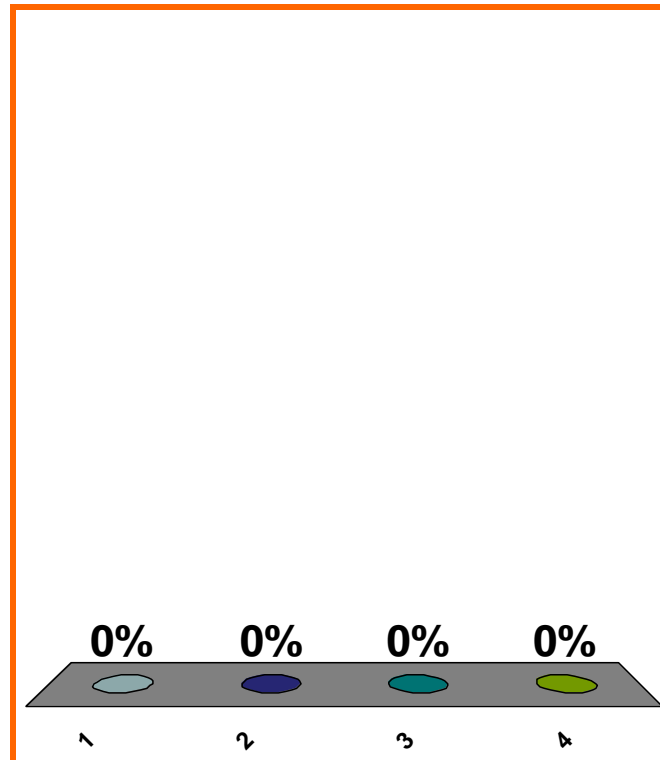
$$\lim_{x \rightarrow \infty} \left[ \frac{100x^3 + 2x - 1}{x^3 + x^2 + 1} \right] = ??$$

(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

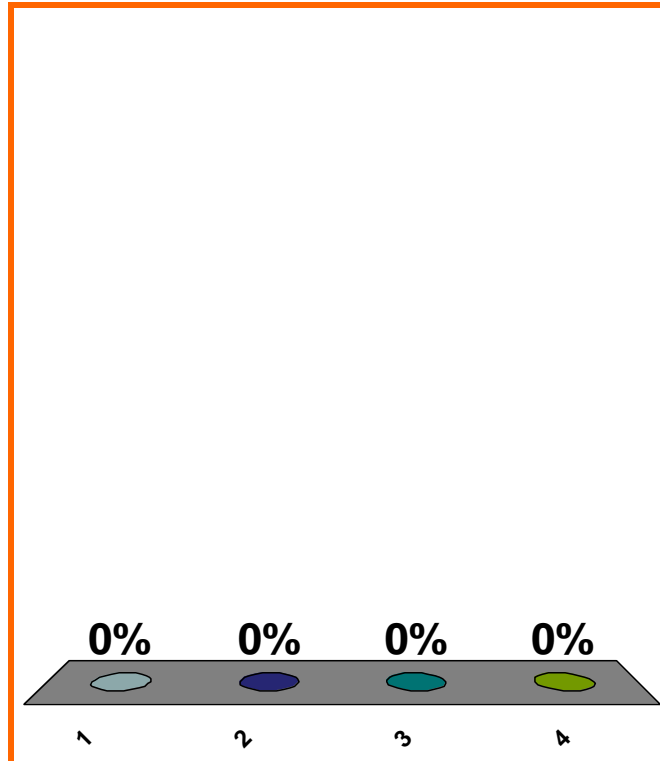
$$\lim_{x \rightarrow \infty} \left[ \frac{100x^3 + 2x - 1}{x^2 + 1} \right] = ??$$

(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

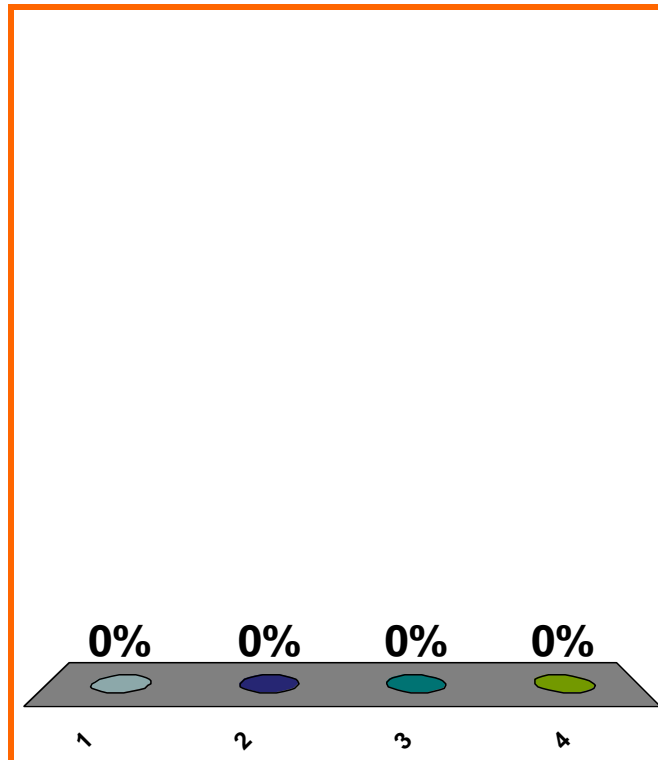
$$\lim_{x \rightarrow -\infty} \left[ \frac{100x^3 + 2x - 1}{x^2 + 1} \right] = ??$$

(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0250

0 pts

27

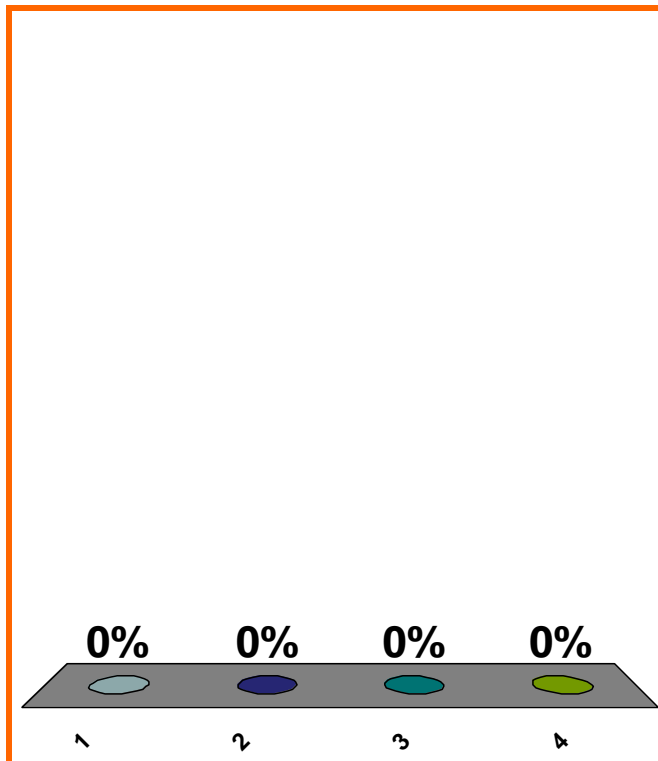
$$\lim_{x \rightarrow -\infty} \left[ \frac{100x^3 + 2x - 1}{x + 1} \right] = ??$$

(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

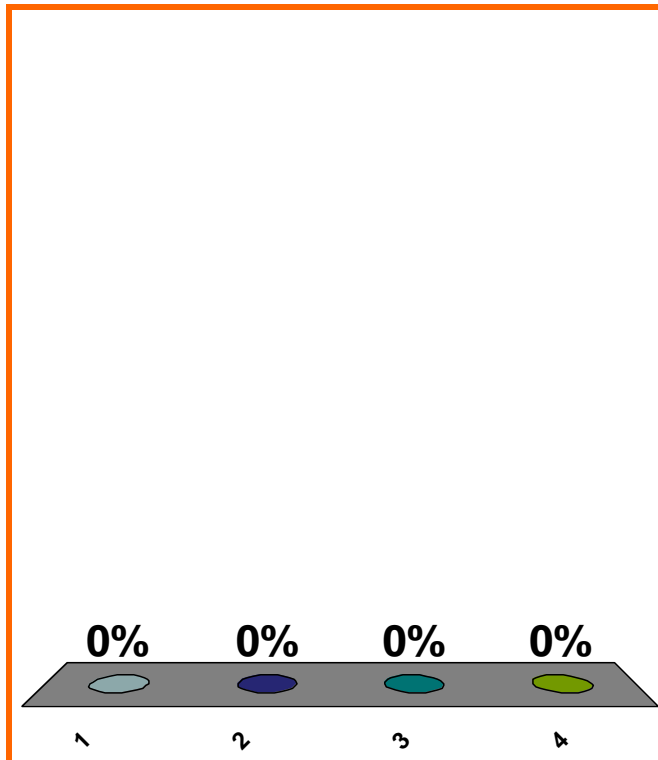
$$\lim_{x \rightarrow \infty} \left[ \frac{100x^3 + 2x - 1}{x + 1} \right] = ??$$

(a)  $\infty$

(b)  $-\infty$

(c) 100

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0250

0 pts

29

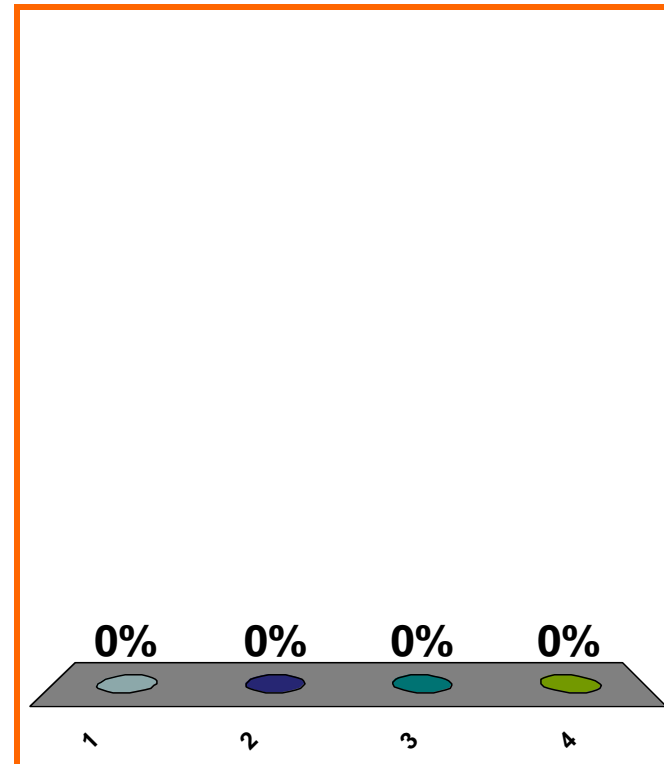
$$\ln(1 + (3/n)) \quad n \rightarrow \infty \quad ??$$

(a)  $1/n^2$

(b) 1

(c)  $3/n$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

$$\ln(1 + 5x) \quad x \sim 0 \quad ??$$

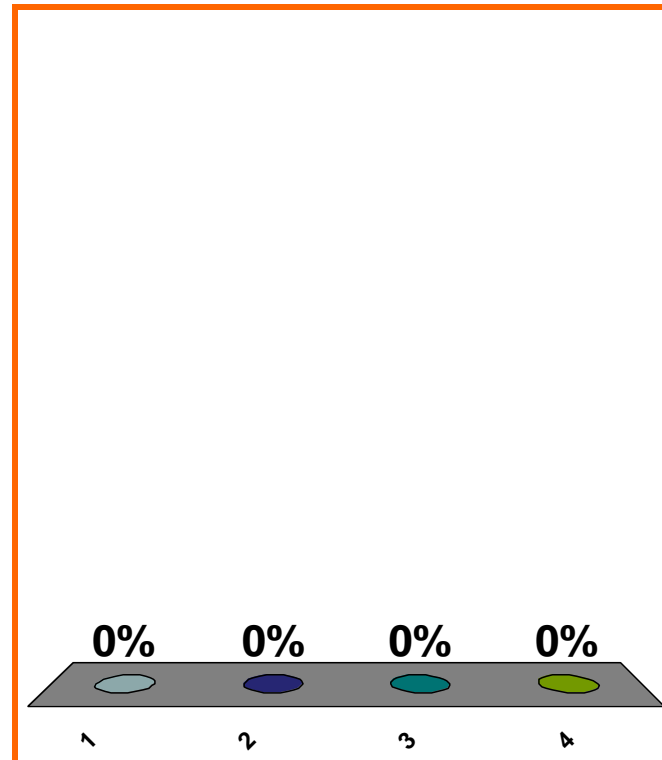
$x \rightarrow 0$

(a)  $4x^2$

(b)  $5x$

(c) 1

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0420

0 pts

31

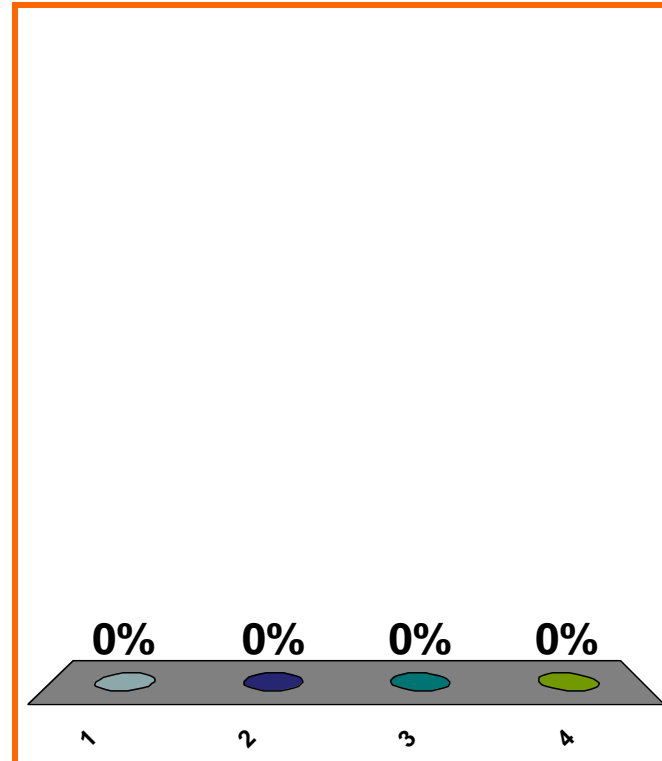
$$\ln(1 + 5x + 4x^2) \quad x \sim 0 \quad ??$$

(a)  $4x^2$

(b)  $5x$

(c) 1

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0420

0 pts

32



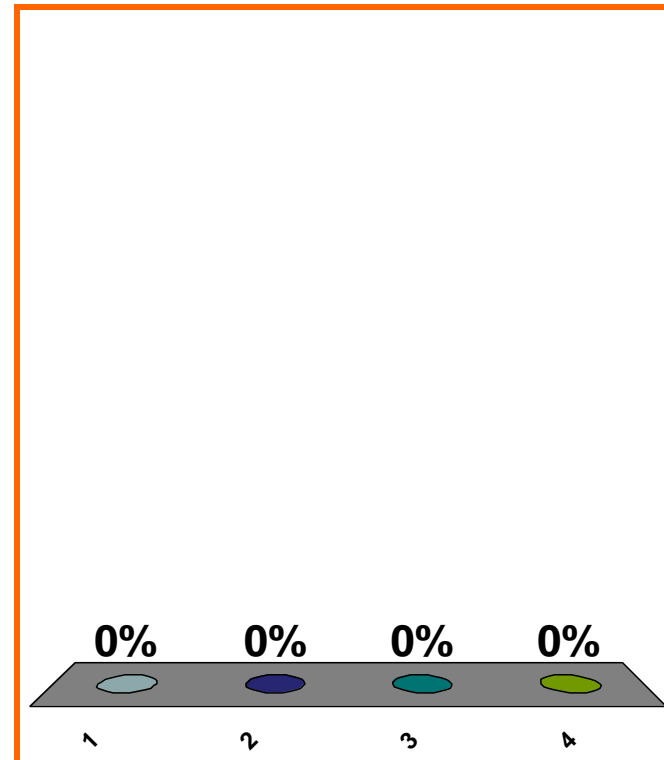
To get graph of  $y + 1 = x^3$ ,  
move graph of  $y = x^3$  ...

(a) right 1

(b) left 1

(c) down 1

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

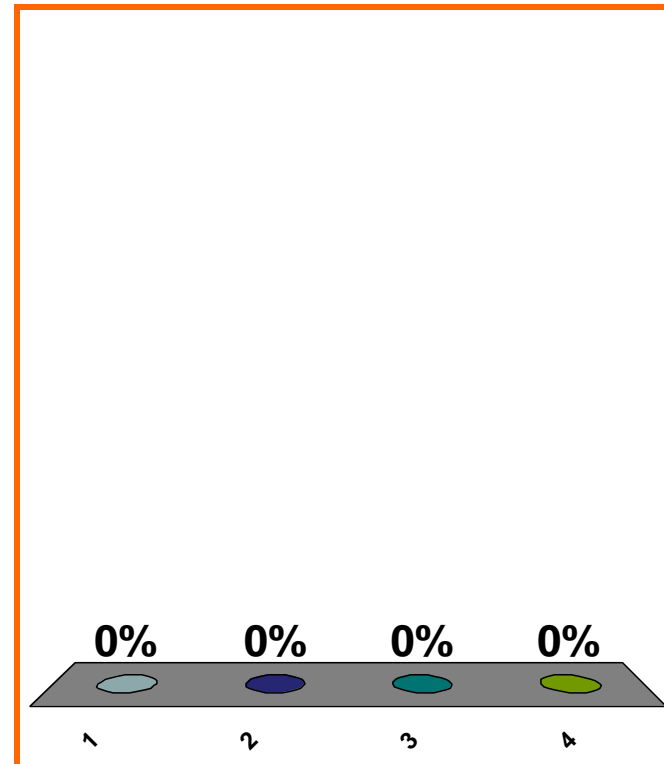
To get graph of  $y^2 = \sin(x + \pi)$ ,  
move graph of  $y^2 = \sin(x)$  ...

(a) right  $\pi$

(b) left  $\pi$

(c) down  $\pi$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0060

0 pts

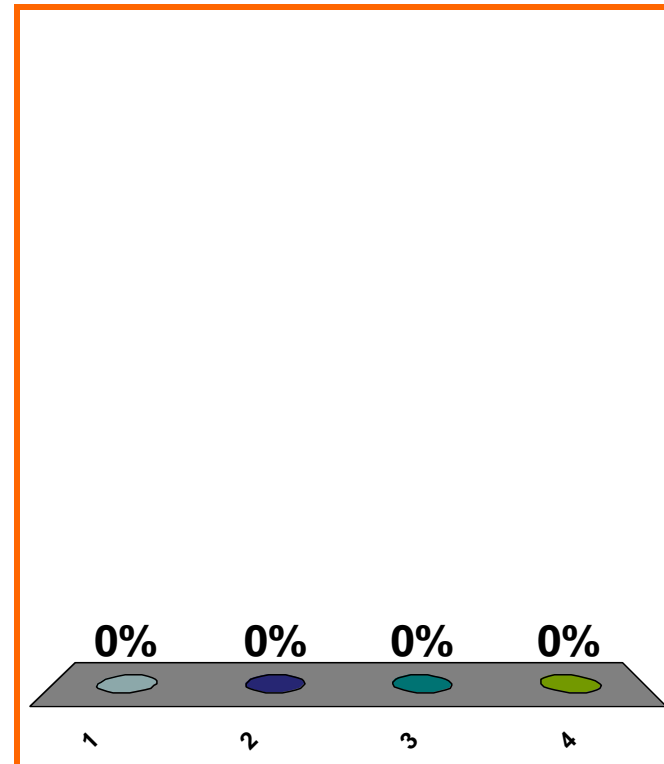
To get graph of  $y^2 = \sin(x - \pi)$ ,  
move graph of  $y^2 = \sin(x)$  ...

(a) right  $\pi$

(b) left  $\pi$

(c) down  $\pi$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

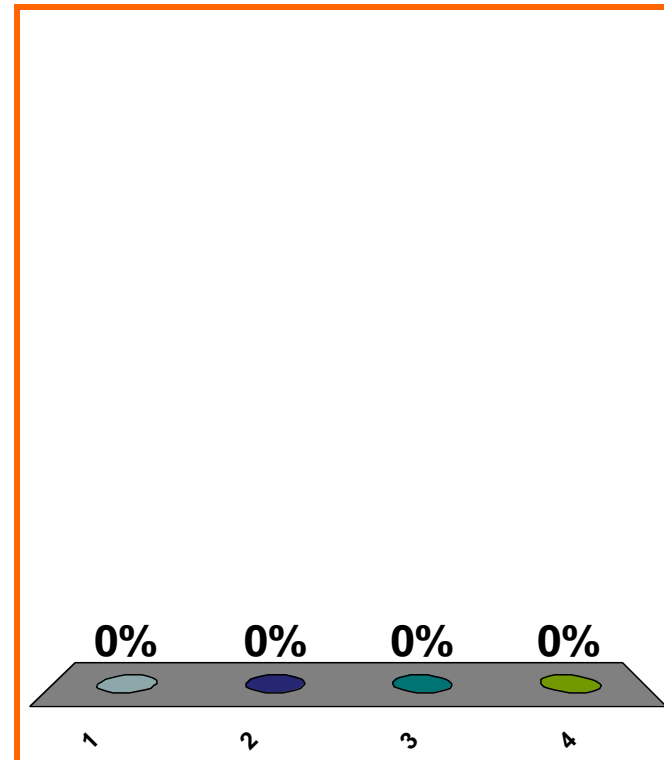
To get graph of  $(y + \pi)^2 = \sin(x)$ ,  
move graph of  $y^2 = \sin(x)$  ...

(a) right  $\pi$

(b) left  $\pi$

(c) down  $\pi$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

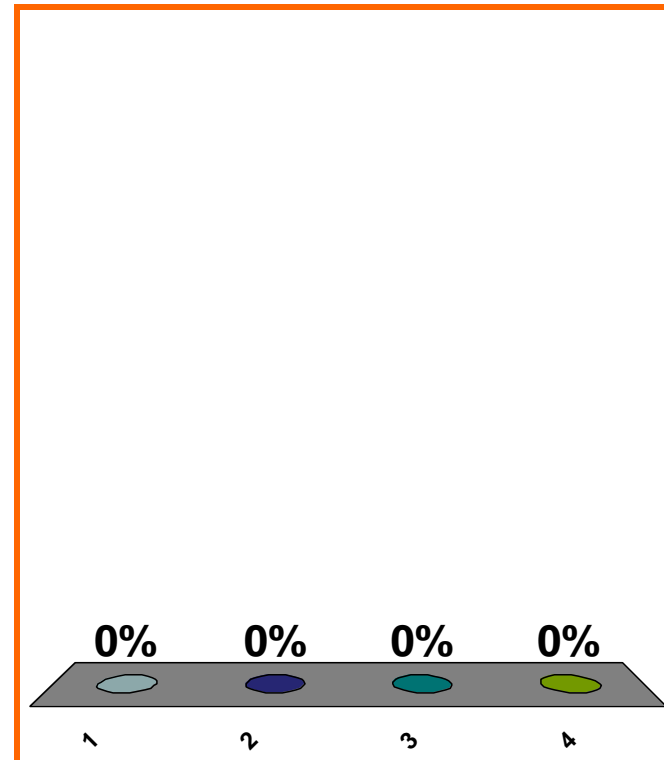
$$\sin(\pi/3) = ??$$

(a)  $\sqrt{2}/2$

(b)  $\sqrt{3}/2$

(c)  $1/2$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

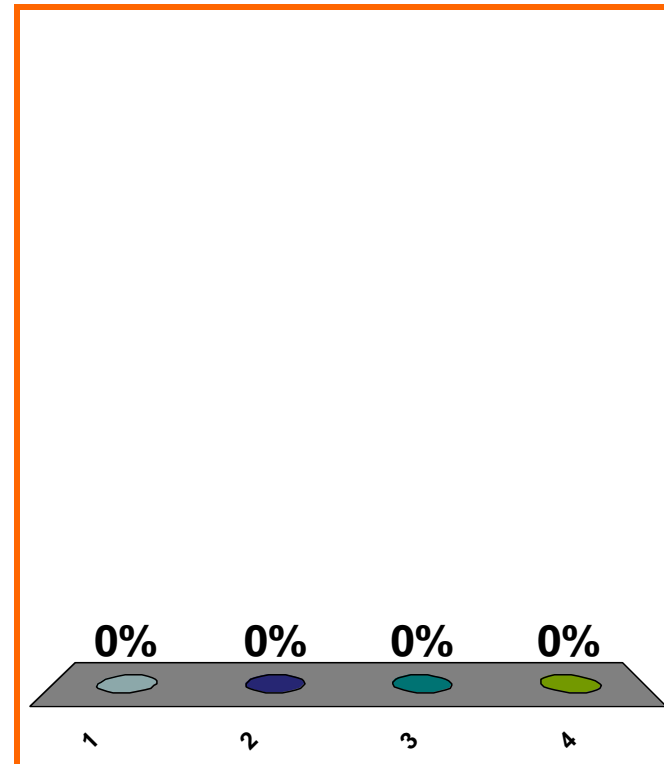
$$\arcsin(\sqrt{3}/2) = ??$$

(a)  $\pi/3$

(b)  $\pi/4$

(c)  $\pi/6$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

0 of 5

Topic 0110

0 pts

38

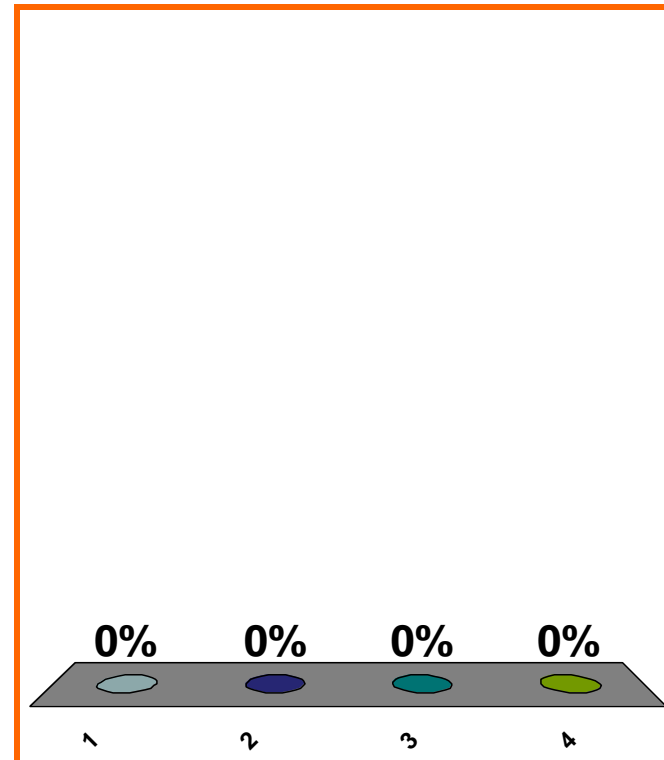
$$\sin(3\pi/4) = ??$$

(a)  $\sqrt{2}/2$

(b)  $-\sqrt{2}/2$

(c)  $1/2$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0090

0 pts

39

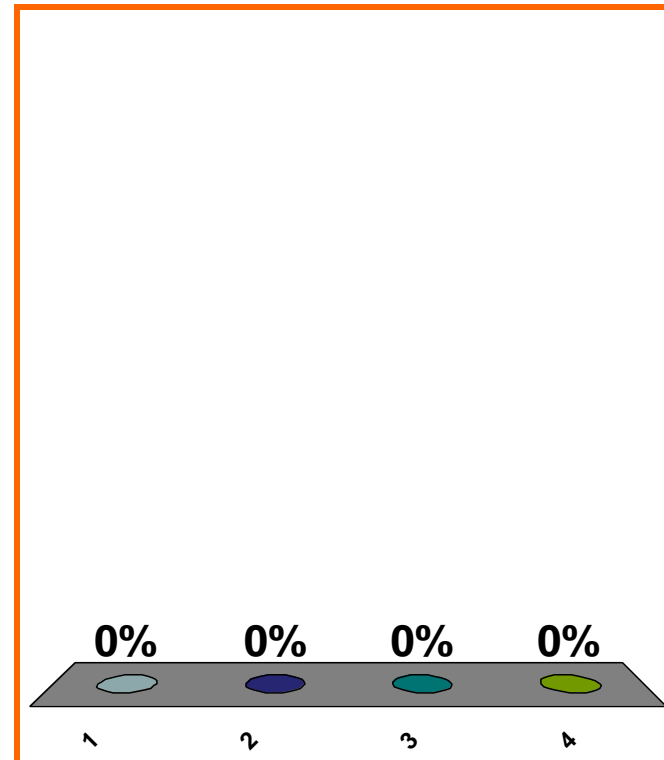
$$\arcsin(\sqrt{2}/2) = ??$$

(a)  $\pi/3$

(b)  $\pi/4$

(c)  $\pi/6$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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Topic 0110

0 pts

40



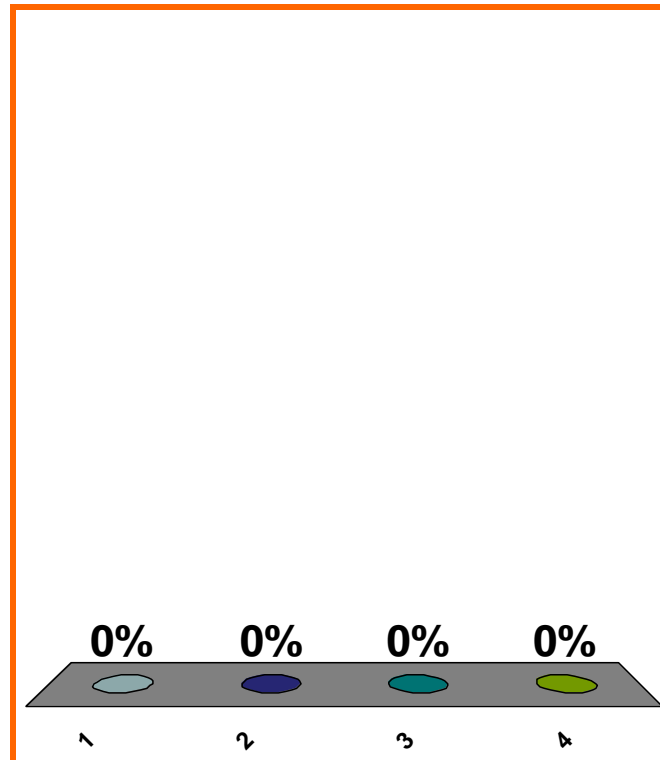
$$\frac{d}{dx} [(x^2)(\sin x)] = ??$$

(a)  $(2x)(\cos x)$

(b)  $(2x)(-\cos x)$

(c)  $(2x)(\sin x) + (x^2)(\cos x)$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0340

0 pts

41

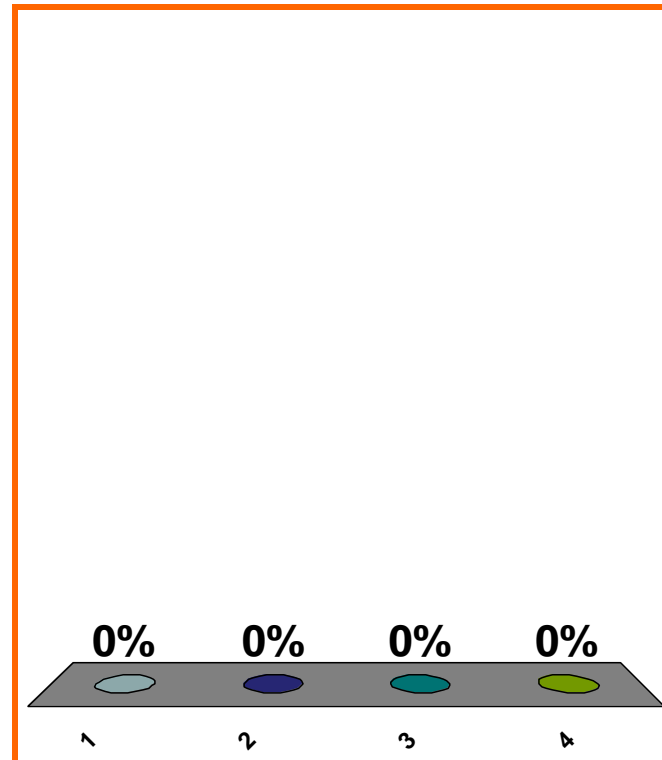
$$\frac{d}{dx} \left[ \frac{\sin x}{x} \right] = ??$$

(a)  $\frac{(\sin x)(1) - (x)(\cos x)}{x}$

(b)  $\frac{(\sin x)(1) - (x)(\cos x)}{x^2}$

(c)  $\frac{(x)(\cos x) - (\sin x)(1)}{x^2}$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0350

0 pts

42

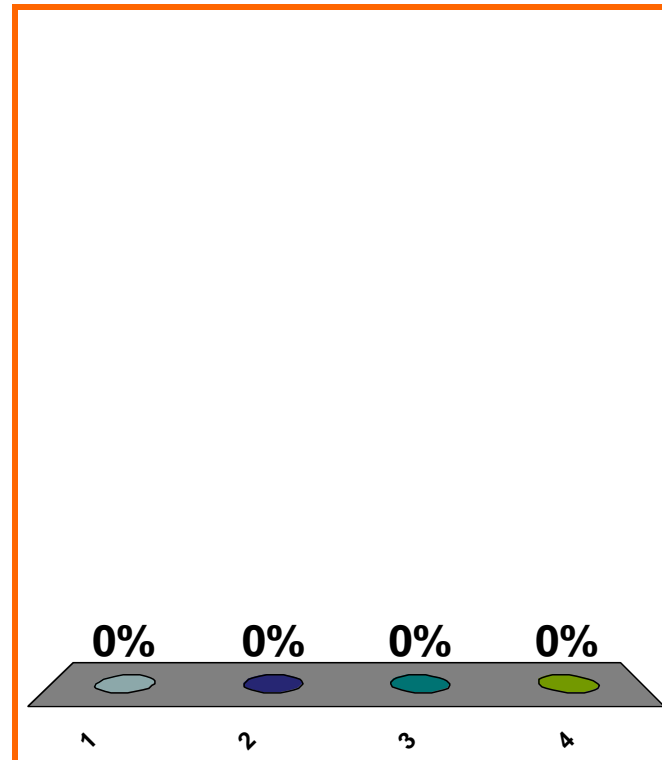
$$\lim_{x \rightarrow 5} (3x^3 - 2x + 8)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

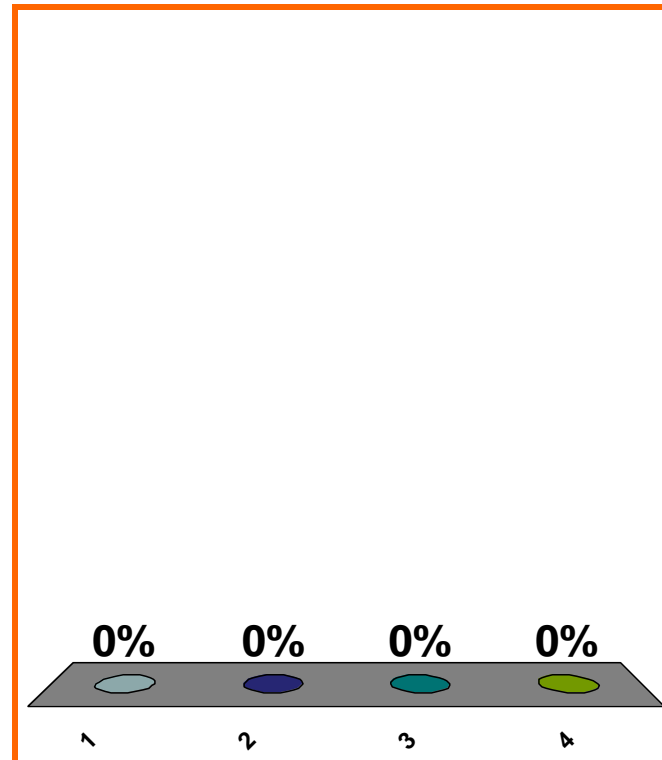
$$\lim_{x \rightarrow 5} \left( \frac{3x^3 - 2x + 8}{x - 4} \right)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

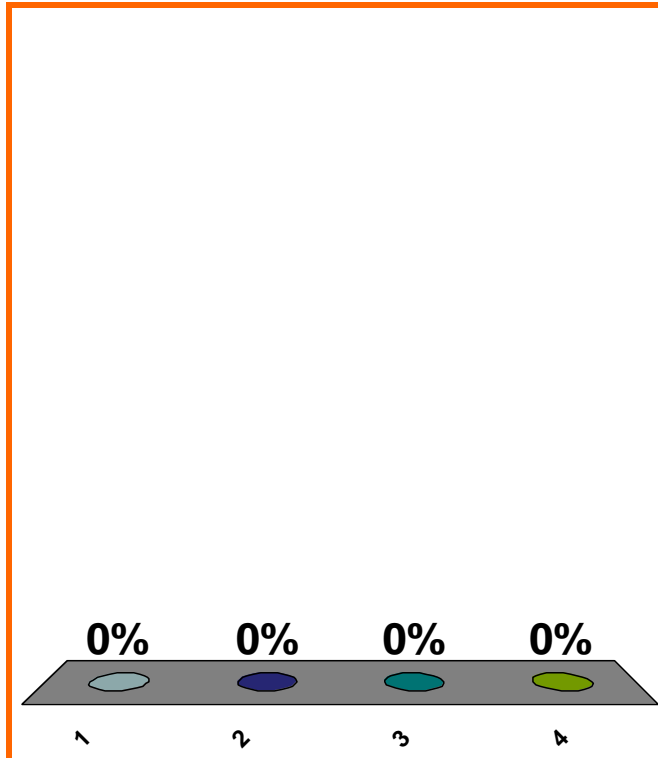
$$\lim_{x \rightarrow 5^+} \left( \frac{3x^3 - 2x + 8}{x - 5} \right)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

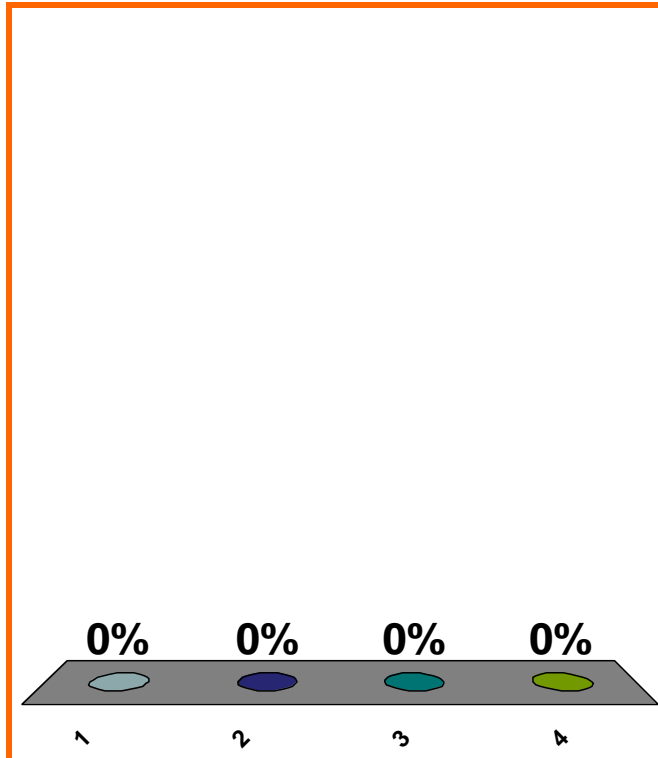
$$\lim_{x \rightarrow 5^-} \left( \frac{3x^3 - 2x + 8}{x - 5} \right)$$

(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0250

0 pts

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$$\lim_{x \rightarrow 5} \left( \frac{3x^3 - 2x + 8}{x - 5} \right)$$

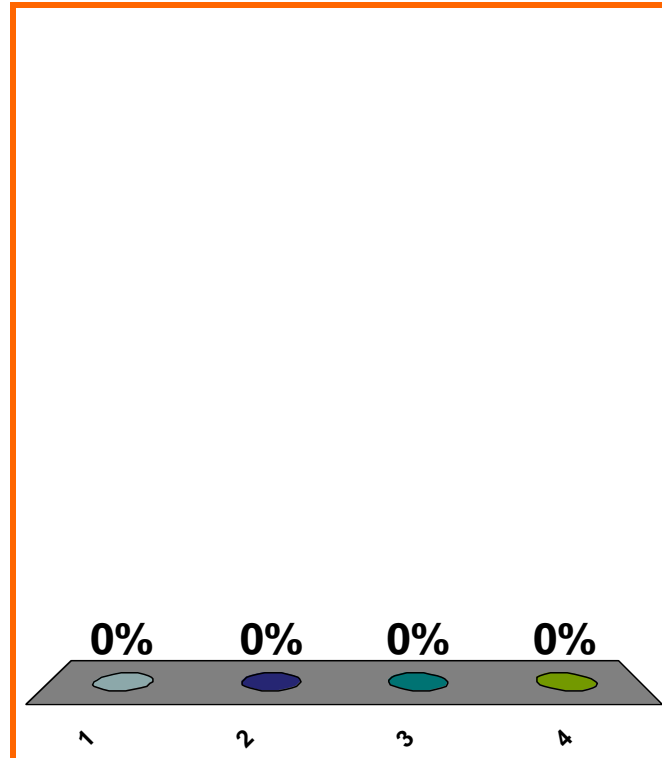
(a)  $(3)(5^3) - (2)(5) + 8$

(b)  $-\infty$

(c)  $\infty$

(d) none of the above

Correct answer: DNE



1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40

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LOOK AHEAD  
Topic 0250

0 pts

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0170-1. Use the graph of  $f$  given below to find the value of each quantity, if it exists.

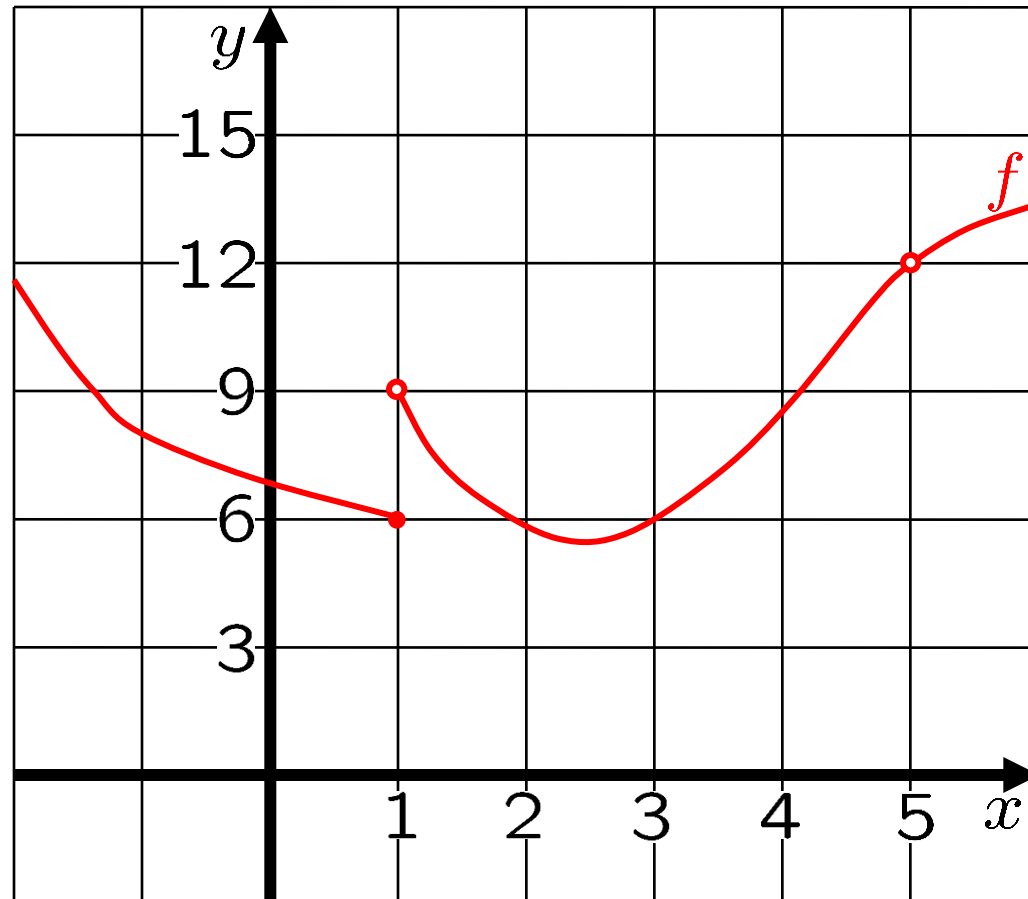
(a)  $\lim_{x \rightarrow 1^-} f(x)$

(b)  $\lim_{x \rightarrow 1^+} f(x)$

(c)  $\lim_{x \rightarrow 1} f(x)$

(d)  $\lim_{x \rightarrow 5} f(x)$

(e)  $f(5)$





0170-2. Use the graph of  $f$  given below to find the value of each quantity, if it exists.

(a)  $\lim_{x \rightarrow 1^-} f(x)$

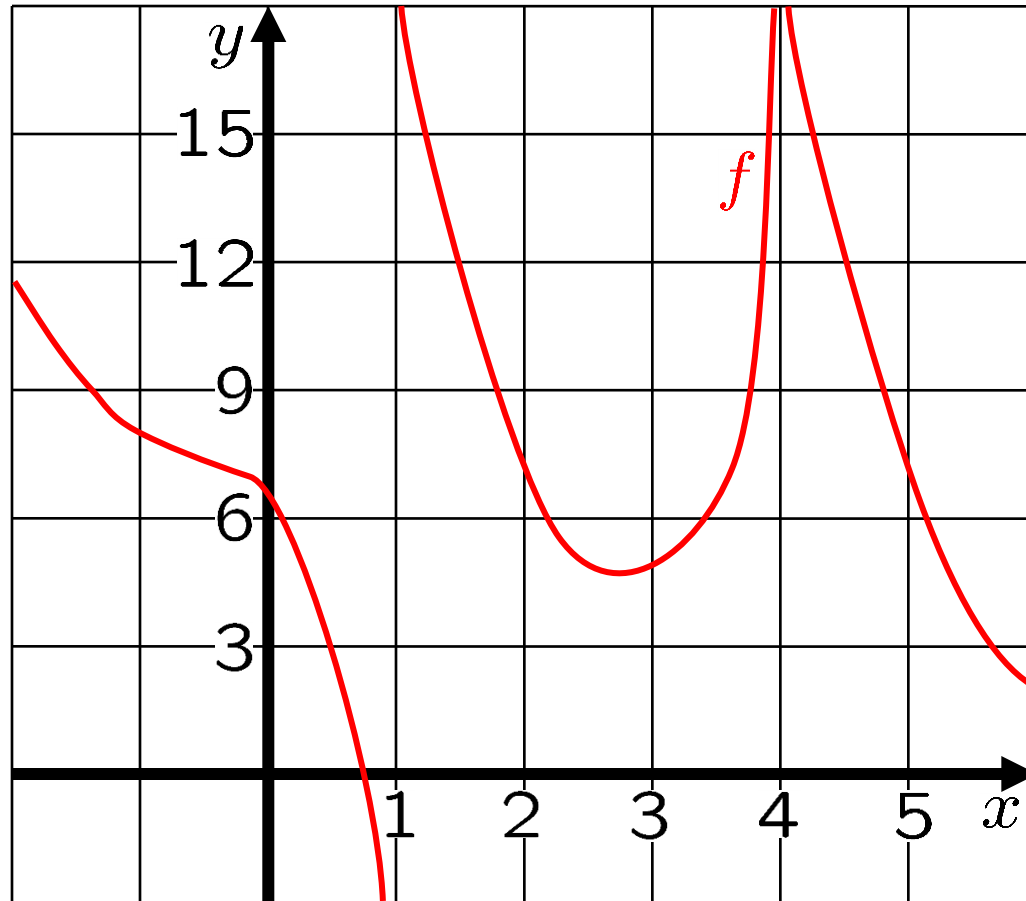
(b)  $\lim_{x \rightarrow 1^+} f(x)$

(c)  $\lim_{x \rightarrow 1} f(x)$

(d)  $\lim_{x \rightarrow 4^-} f(x)$

(e)  $\lim_{x \rightarrow 4^+} f(x)$

(f)  $\lim_{x \rightarrow 4} f(x)$



0170-3. Show a graph of a function  $h$  s.t.

OLD

$$\lim_{x \rightarrow 2^-} h(x) = 7, \quad \lim_{x \rightarrow 2^+} h(x) = 6, \quad h(2) = 5,$$

$$\lim_{x \rightarrow 3} h(x) = -\infty,$$

$$\lim_{x \rightarrow 4^-} h(x) = \infty, \quad \lim_{x \rightarrow 4^+} h(x) = -\infty,$$

$$\lim_{x \rightarrow -\infty} h(x) = -3 \quad \text{and} \quad \lim_{x \rightarrow \infty} h(x) = 1.$$

0170-5. a. Compute  $\lim_{x \rightarrow 1^-} \frac{2x + 3}{x - 1}$ ,

or explain why the limit  
does not exist.

b. Compute  $\lim_{x \rightarrow 1^+} \frac{2x + 3}{x - 1}$ ,

or explain why the limit  
does not exist.

c. Compute  $\lim_{x \rightarrow 1} \frac{2x + 3}{x - 1}$ ,

or explain why the limit  
does not exist.

tangent slopes for  $y = x^3$ , esp. at  $x = 5$ .

$$\lim_{h \rightarrow 0} \frac{(5 + h)^3 - 5^3}{h}$$

$$\lim_{\Delta x \rightarrow 0} \frac{(5 + \Delta x)^3 - 5^3}{\Delta x}$$

## LOOK AHEAD

differentiate polynomials

differentiate all 6 trig functions

$$\lim_{x \rightarrow 0} [\sin(1/x)]$$

$$\lim_{x \rightarrow 0} [x(\sin(1/x))]$$

$$\lim_{x \rightarrow 0} \left[ \frac{2x^3 + x^2}{8x^5 + 3x^4 - 7x^3} \right]$$

$f'(3)$ , when  $f(x) = 1/x$

derivative of ln

product, quotient, chain rules

SAVE THE  
SESSION  
DATA

RETURN TO  
PRESENTATION