MATH 1271 Spring 2012, Midterm #2
Handout date: Thursday 29 March 2012

PRINT YOUR NAME:

PRINT YOUR TA'S NAME:

WHAT RECITATION SECTION ARE YOU IN?

Closed book, closed notes, no calculators/PDAs; no reference materials of any kind. Turn off all handheld devices, including cell phones.

Show work; a correct answer, by itself, may be insufficient for credit. Arithmetic need not be simplified, unless the problem requests it.

I understand the above, and I understand that cheating has severe consequences, from a failing grade to expulsion.

SIGN YOUR NAME:

I. Multiple choice

A. (5 pts) (no partial credit) Suppose $f''(x) = -x^2 + 4x - 3$. At most one of the following statements is true. If one is, circle it. Otherwise, circle "NONE OF THE ABOVE".

(a) f is concave up on $(-\infty, 1]$, down on $[1, 3]$ and up on $[3, \infty)$.

(b) f is concave down on $(-\infty, 1]$, up on $[1, 3]$ and down on $[3, \infty)$.

(c) f is concave up on $(-\infty, -3]$, down on $[-3, -1]$ and up on $[-1, \infty)$.

(d) f is concave down on $(-\infty, -3]$, up on $[-3, -1]$ and down on $[-1, \infty)$.

(e) NONE OF THE ABOVE

B. (5 pts) (no partial credit) Find the logarithmic derivative of $x^2 + 7x - 8$ w.r.t. x.

(a) $\dfrac{x^2 + 7x - 8}{2x + 7}$

(b) $(\ln(x^2)) + 7(\ln x) - (\ln 8)$

(c) $\ln(2x + 7)$

(d) $\dfrac{2x + 7}{x^2 + 7x - 8}$

(e) NONE OF THE ABOVE

C. (5 pts) (no partial credit) Find an equation of the tangent line to $4x^2y - 2y^3 = 2$ at the point $(1, 1)$.

(a) $y - 1 = x - 1$

(b) $y - 1 = 2(x - 1)$

(c) $y - 1 = 3(x - 1)$

(d) $y - 1 = 4(x - 1)$

(e) NONE OF THE ABOVE

D. (5 pts) (no partial credit) Find the logarithmic derivative of $(2+x^4)^{\cos x}$ w.r.t. x.

(a) $(\cos x)(\ln(2+x^4)) + (-\sin x)(4x^3/(2+x^4))$

(b) $(-\sin x)(4x^3/(2+x^4))$

(c) $(-\sin x)(\ln(2+x^4)) + (\cos x)(4x^3/(2+x^4))$

(d) $(\cos x)(\ln(2+x^4))$

(e) NONE OF THE ABOVE

E. (5 pts) (no partial credit) Find the derivative of $(2+x^4)^{\cos x}$ w.r.t. x.

(a) $[(2+x^4)^{\cos x}][(\cos x)(\ln(2+x^4)) + (-\sin x)(4x^3/(2+x^4))]$

(b) $[(2+x^4)^{\cos x}][(-\sin x)(4x^3/(2+x^4))]$

(c) $[(2+x^4)^{\cos x}][(-\sin x)(\ln(2+x^4)) + (\cos x)(4x^3/(2+x^4))]$

(d) $[(2+x^4)^{\cos x}][(\cos x)(\ln(2+x^4))]$

(e) NONE OF THE ABOVE

F. (5 pts) (no partial credit) Compute $[d/dx][\sin(\cos(e^x+3))]$.

(a) $\cos(\cos(e^x+3))$

(b) $[\cos(\cos(e^x+3))][\cos(e^x+3)][e^x+3]$

(c) $[\cos(\cos(e^x+3))][-\sin(e^x+3)][e^x+3]$

(d) 0

(e) NONE OF THE ABOVE

II. True or false (no partial credit):

a. (5 pts) If $f'(7) = 0$ and $f''(7) > 0$, then f has a local maximum at 7.

b. (5 pts) Assume that $\lim_{x\to a}[f(x)] = 0$ and that $\lim_{x\to a}[g(x)] = 0$. Assume also that $\lim_{x\to a}\frac{f'(x)}{g'(x)}$ does not exist. Then $\lim_{x\to a}\frac{f(x)}{g(x)}$ does not exist.

c. (5 pts) Every local extremum occurs at a critical number.

d. (5 pts) If f is concave up on an interval I, then $f'' > 0$ on I.

e. (5 pts) If two functions have the same derivative, then they are equal.

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PLEASE DO NOT WRITE BELOW THE LINE

VERSION B

I. A,B,C

I. D,E,F

II. a,b,c,d,e

III. 1ab.

III. 2.

III. 3,4.

III. 5.

III. Computations. Show work. Unless otherwise specified, answers must be exactly correct, but can be left in any form easily calculated on a standard calculator.

1. a. (5 pts) Compute $\frac{d}{dx}\left[\frac{2x^3-8}{6+(\arctan(2x))}\right]$.

b. (5 pts) Compute $\frac{d}{dx}\left[(4-\sin x)^x\right]$.

2. (10 pts) Using implicit differentiation, find $y' = dy/dx$, assuming that $(x - y^2)^5 = x$.

3. (5 pts) Let $f(x) = 4x + 4x^5$. Then f is a one-to-one function. Let $g := f^{-1}$. Then $f(1) = 8$, so $g(8) = 1$. Compute $g'(8)$.

4. (10 pts) Find the maximal intervals of concavity for $f(x) = -3x^5 + 20x^4 + 4x - 8$. For each interval, state clearly whether f is concave up or concave down on that interval.

5. (10 pts) Compute $\lim_{x \to 1} \left[\dfrac{\ln x}{\cos(\pi x/2)} \right]$.