

CALCULUS  
Linear approximation  
OLD2

0540-1. Find the linearization of  
OLD2

$$f(x) = 5x^3 - 2x$$

at  $x = 3$ .

That is, find  $m$  and  $a$  s.t. the linear function

$$L(x) = a + m(x - 3)$$

has the same 1-jet at  $x = 3$  as does  $f(x)$ .

That is, find  $m$  and  $a$  s.t. the linear function

$$L(x) = a + m(x - 3)$$

satisfies:  $L(3) = f(3)$  and  $L'(3) = f'(3)$ .

0540-2. Find the linearization of  
OLD2

$$f(x) = \tan x$$

at  $x = \pi/4$ .

That is, find  $m$  and  $a$  s.t. the linear function

$$L(x) = a + m(x - (\pi/4))$$

has the same 1-jet at  $x = \pi/4$  as does  $f(x)$ .

That is, find  $m$  and  $a$  s.t. the linear function

$$L(x) = a + m(x - (\pi/4))$$

satisfies:  $L(\pi/4) = f(\pi/4)$

and  $L'(\pi/4) = f'(\pi/4)$ .

0540-3. Let  $y = \frac{e^x \cos x}{2x^2 + 3x - 5}$ .

Compute  $\Delta y$  and  $dy$ .

0540-4. Let  $w = \frac{u + 4}{\sin(2u + 8)}$ .

Compute  $\Delta w$  and  $dw$ .

0540-5. Let  $z = \frac{e^{3h^2 + 2h}}{\cos(h + 5)}$ .

a. Compute  $[\Delta z]_{h: \rightarrow 0, \Delta h: \rightarrow 0.0002}$ .

b. Compute  $[dz]_{h: \rightarrow 0, dh: \rightarrow 0.0002}$ .

0540-6. a. Compute  $(3.0002)^7$ .

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b. Approx.  $(3.0002)^7$  by differentials.

c. Let  $L(x)$  be the linearization  
of  $f(x) = x^7$  at  $x = 3$ .

Compute  $L(3.0002)$ .

0540-7. Let  $\theta$  be the number of  
radians in  $59.9^\circ$ .

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Approximate  $\cos \theta$  by differentials.

0540-8. Approx.  $e^{0.004}$  by differentials.

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0540-9. We need to paint a ball whose  
radius is 10 meters.

OLD2

The coat of paint is to be 0.001 meters thick,  
so, after painting, the radius will be  
10.001 meters.

a. Let  $V = \frac{4}{3}\pi r^3$ . Compute  $\Delta V$  and  $dV$ .

b. Using  $\Delta V$ , compute the exact volume of  
paint that will be needed.

c. Using  $dV$ , estimate the volume of  
paint that will be needed.

d. Compute 0.001 times the surface area  
of a ball of radius 10 meters.

0540-10. A square based pyramid whose sides are equilateral triangles is called a  $J_1$  (**Johnson<sub>1</sub>**) **solid**; its edges all have the same length. **If** that length is  $s$ , **then** its volume is  $\frac{\sqrt{2}}{6}s^3$ .

Pharaoh asks us to build a pyramid in the shape of a  $J_1$  solid, whose edge length is  $500 \pm 1$  feet.

Up to some error, its volume will be  $\frac{\sqrt{2}}{6}(500)^3$  cubic feet.

Using differentials, **estimate** that error.