

CALCULUS
Derivatives of inverse functions
(The Inverse Function Theorem)
OLD

0440-1. Differentiate $y = \arctan(e^x + \sqrt[3]{x})$.

0440-2. Differentiate $F(t) = [e^{3t+4}] [\arcsin(t^2)]$.

0440-3. Differentiate $f(x) = \sin(\arctan x)$.

0440-4. Differentiate $v(s) = \operatorname{arccot} \left[\sqrt{\frac{2-s}{2+s}} \right]$.

0440-5. **Draw** a graph of a 1-1 function f
which passes through $(4, 5)$
and whose tangent line at $(4, 5)$ has slope $2/3$.

In the same picture,
draw that tangent line.

In the same picture,
draw a right triangle whose
hypotenuse is on the tangent line
and whose legs have lengths 2 and 3.

In a separate picture, **reflect**,
through the 45° line,
everything in the previous picture.

Let $g := f^{-1}$.

What are the values of $f(4)$ and $f'(4)$?

What are the values of $g(5)$ and $g'(5)$?