

Schema Refinement and Normal Forms

Chapter 19

Decomposition of a Relation Scheme

- ❖ Suppose that relation R contains attributes $A_1 \dots A_n$. A decomposition of R consists of replacing R by two or more relations such that:
 - Each new relation scheme contains a subset of the attributes of R (and no attributes that do not appear in R), and
 - Every attribute of R appears as an attribute of at least one of the new relations.
- ❖ Intuitively, decomposing R means we will store instances of the relation schemes produced by the decomposition, instead of instances of R.
- ❖ E.g., Can decompose **SNLRWH** into **SNLRH** and **RW**.

Example Decomposition

- ❖ Decompositions should be used only when needed.
 - SNLRWH has FDs $S \rightarrow SNLRWH$ and $R \rightarrow W$
 - Second FD causes violation of 3NF; W values repeatedly associated with R values. Easiest way to fix this is to create a relation RW to store these associations, and to remove W from the main schema:
 - i.e., we decompose SNLRWH into SNLRH and RW
- ❖ The information to be stored consists of SNLRWH tuples. If we just store the projections of these tuples onto SNLRH and RW, *are there any potential problems that we should be aware of?*

Problems with Decompositions

- ❖ There are three potential problems to consider:
 1. Some queries become more expensive.
 - e.g., How much did Joe earn? (salary = $W \cdot H$)
 2. Given instances of the decomposed relations, we may not be able to reconstruct the corresponding instance of the original relation!
 - Fortunately, not in the SNLRWH example.
 3. Checking some dependencies may require joining the instances of the decomposed relations.
 - Fortunately, not in the SNLRWH example.
- ❖ Tradeoff: Must consider these issues vs. redundancy.

Lossless Join Decompositions

- ❖ Decomposition of R into X and Y is lossless-join w.r.t. a set of FDs F if, for every instance r that satisfies F:
 - $\pi_X(r) \bowtie \pi_Y(r) = r$
- ❖ It is always true that $r \subseteq \pi_X(r) \bowtie \pi_Y(r)$
 - In general, the other direction does not hold! If it does, the decomposition is lossless-join.
- ❖ Definition extended to decomposition into 3 or more relations in a straightforward way.
- ❖ *It is essential that all decompositions used to deal with redundancy be lossless! Avoids Problem (2).*

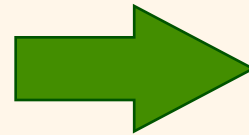
More on Lossless Join

A	B	C
1	2	3
4	5	6
7	2	8



A	B
1	2
4	5
7	2

B	C
2	3
5	6
2	8



A	B	C
1	2	3
4	5	6
7	2	8
1	2	8
7	2	3

- ❖ The decomposition of R into X and Y is **lossless-join wrt F** if and only if the closure of F contains:
 - $X \cap Y \rightarrow X$, or
 - $X \cap Y \rightarrow Y$

Dependency Preserving Decomposition

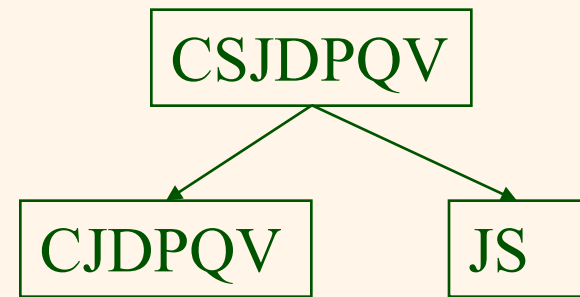
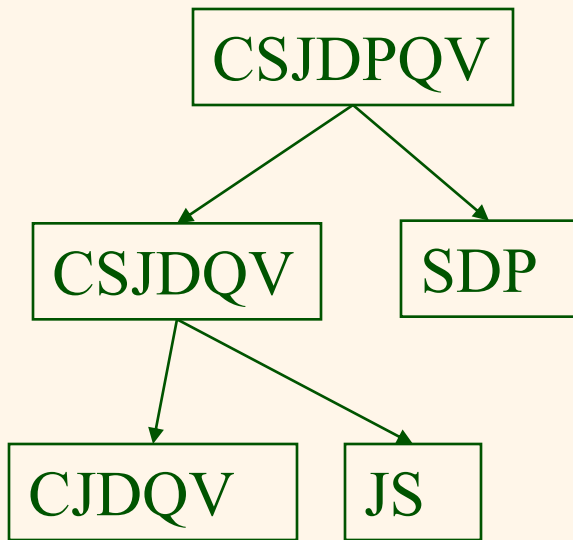
- ❖ Consider CSJDPQV, C is key, $JP \rightarrow C$ and $SD \rightarrow P$.
 - BCNF decomposition: CSJDQV and SDP (lossless-join)
 - Problem: Checking (Enforcing) $JP \rightarrow C$ requires a join!
- ❖ **Dependency preserving decomposition** (Intuitive):
 - If R is decomposed into X, Y and Z, and we enforce the FDs on X, on Y and on Z, (*separately*) then all FDs that were given to hold on R must also hold. (Avoids Problem (3).)

Decomposition into BCNF

- ❖ Consider relation R with FDs F . If $X \rightarrow Y$ violates BCNF, decompose R into $R - Y$ and XY .
 - Repeated application of this idea will give us a collection of relations that are in BCNF; lossless join decomposition, and guaranteed to terminate.

Decomposition into BCNF

- ❖ Example: $CSJDPQV$, key C , $JP \rightarrow C$, $SD \rightarrow P$, $J \rightarrow S$
- ❖ To deal with $SD \rightarrow P$, decompose into SDP , $CSJDQV$.
- ❖ To deal with $J \rightarrow S$, decompose $CSJDQV$ into JS and $CJDQV$



- ❖ In general, several dependencies may cause violation of BCNF. The order in which we “deal with” them could lead to very different sets of relations!

BCNF and Dependency Preservation

- ❖ In general, there may not be a dependency preserving decomposition into BCNF.
 - e.g., $CSZ, CS \rightarrow Z, Z \rightarrow C$
 - Can't decompose while preserving 1st FD; not in BCNF.
- ❖ Similarly, decomposition of $CSJDQV$ into SDP, JS and $CJDQV$ is not dependency preserving (w.r.t. the FDs $JP \rightarrow C, SD \rightarrow P$ and $J \rightarrow S$).
 - However, it is a lossless join decomposition.
 - In this case, adding JPC to the collection of relations gives us a dependency preserving decomposition.
 - JPC tuples stored only for checking FD! (*Redundancy!*)

Decomposition into 3NF

- ❖ Obviously, the algorithm for lossless join decomp into BCNF can be used to obtain a lossless join decomp into 3NF (typically, can stop earlier).
- ❖ To ensure dependency preservation, one idea:
 - If $X \rightarrow Y$ is not preserved, add relation XY .
 - Problem is that XY may violate 3NF! e.g., consider the addition of CJP to 'preserve' $JP \rightarrow C$. What if we also have $J \rightarrow C$?