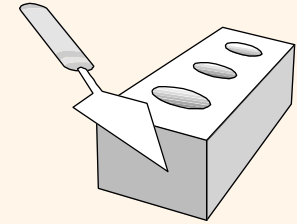


# *Relational Algebra*

## Chapter 4

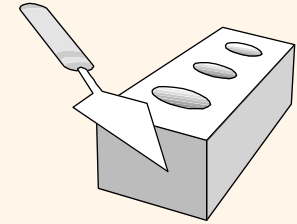


# Division

- ❖ Not supported as a primitive operator, but useful for expressing queries like:

*Find sailors who have reserved all boats.*

- ❖ Let  $A$  have 2 fields,  $x$  and  $y$ ;  $B$  have only field  $y$ :
  - $A/B = \{ \langle x \rangle \mid \exists \langle x, y \rangle \in A \ \forall \langle y \rangle \in B \}$
  - i.e.,  **$A/B$  contains all  $x$  tuples (sailors) such that for every  $y$  tuple (boat) in  $B$ , there is an  $xy$  tuple in  $A$ .**
  - Or: If the set of  $y$  values (boats) associated with an  $x$  value (sailor) in  $A$  contains all  $y$  values in  $B$ , the  $x$  value is in  $A/B$ .
- ❖ In general,  $x$  and  $y$  can be any lists of fields;  $y$  is the list of fields in  $B$ , and  $x \cup y$  is the list of fields of  $A$ .



# Examples of Division A/B

sno	pno
s1	p1
s1	p2
s1	p3
s1	p4
s2	p1
s2	p2
s3	p2
s4	p2
s4	p4

*A*

pno
p2

*B1*

sno
s1
s2
s3
s4

*A/B1*

pno
p2
p4

*B2*

sno
s1
s4

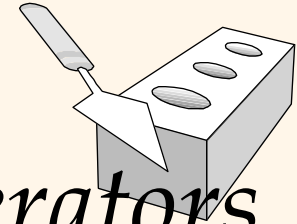
*A/B2*

pno
p1
p2
p4

*B3*

sno
s1

*A/B3*



# Expressing $A/B$ Using Basic Operators

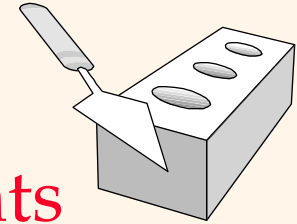
- ❖ Division is not essential op; just a useful shorthand.
  - (Also true of joins, but joins are so common that systems implement joins specially.)
- ❖ *Idea*: For  $A/B$ , compute all  $x$  values that are not 'disqualified' by some  $y$  value in  $B$ .
  - $x$  value is *disqualified* if by attaching  $y$  value from  $B$ , we obtain an  $xy$  tuple that is not in  $A$ .

Disqualified  $x$  values:

$$\pi_x((\pi_x(A) \times B) - A)$$

$$A/B: \quad \pi_x(A) - \text{all disqualified tuples}$$

Find names of sailors who've reserved boat #103



## Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

## Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

## Boats

<u>bid</u>	<u>Color</u>
101	Red
103	Green

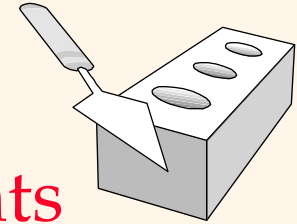
### Solution 1

$$\pi_{sname}(\sigma_{bid=103}(\text{Reserves} \bowtie \text{Sailors}))$$

### Solution 2

$$\pi_{sname}((\sigma_{bid=103} \text{Reserves}) \bowtie \text{Sailors})$$

Find names of sailors who've reserved boat #103



### Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

### Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

### Boats

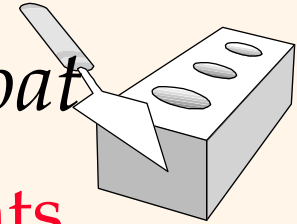
<u>bid</u>	<u>Color</u>
101	Red
103	Green

❖ Solution 3:  $\rho (Temp1, \sigma_{bid=103} Reserves)$

$\rho (Temp2, Temp1 \bowtie Sailors)$

$\pi_{sname} (Temp2)$

Find names of sailors who've reserved a red boat



## Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

## Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

## Boats

<u>bid</u>	<u>Color</u>
101	Red
103	Green

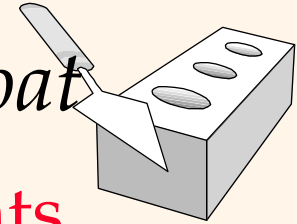
### Solution 1

$$\pi_{sname}(\sigma_{color='red'}(Boats \bowtie Reserves \bowtie Sailors))$$

### Solution 2

$$\pi_{sname}((\sigma_{color='red'} Boats) \bowtie Reserves \bowtie Sailors)$$

Find names of sailors who've reserved a red boat



Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

Boats

<u>bid</u>	<u>Color</u>
101	Red
103	Green

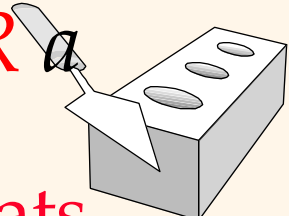
❖ A more efficient solution:

$$\pi_{sname}(\pi_{sid}((\pi_{bid} \sigma_{color='red'} Boats) \bowtie Reserve) \bowtie Sailors)$$

*A query optimizer can find this!*



Find names of sailors who've reserved a red **OR** a green boat



**Sailors**

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

**Reserves**

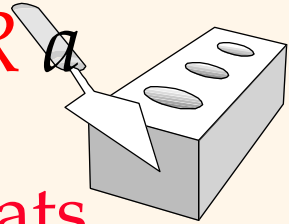
<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

**Boats**

<u>bid</u>	<u>Color</u>
101	Red
103	Green

$\pi_{sname}((\sigma_{col='red' \vee col='green'} Boats) \bowtie Reserves \bowtie Sailors)$

Find names of sailors who've reserved a red **OR** a green boat



Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

Boats

<u>bid</u>	<u>Color</u>
101	Red
103	Green

## ❖ Using Union:

$$\rho(\text{Tempred}, \pi_{\text{sname}}((\sigma_{\text{color}='red'} \text{Boats}) \bowtie \text{Reserves}) \bowtie \text{Sailors}))$$

$$\rho(\text{Tempgreen}, \pi_{\text{sname}}((\sigma_{\text{color}='green'} \text{Boats}) \bowtie \text{Reserves}) \bowtie \text{Sailors}))$$

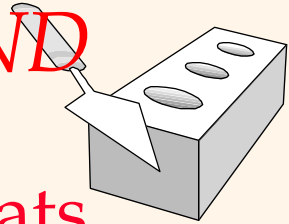
$\text{Tempred} \cup \text{Tempgreen}$

$$\rho(\text{Tempred}, \pi_{\text{sid}}((\sigma_{\text{color}='red'} \text{Boats}) \bowtie \text{Reserves}))$$

$$\rho(\text{Tempgreen}, \pi_{\text{sid}}((\sigma_{\text{color}='green'} \text{Boats}) \bowtie \text{Reserves}))$$

$$\pi_{\text{sname}}((\text{Tempred} \cup \text{Tempgreen}) \bowtie \text{Sailors})$$

Find names of sailors who've reserved a red **AND**  
a green boat



Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

Boats

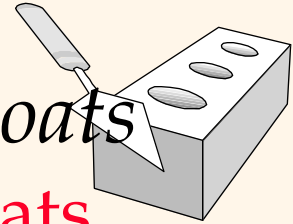
<u>bid</u>	<u>Color</u>
101	Red
103	Green

$$\rho(\text{Tempred}, \pi_{\text{sid}}((\sigma_{\text{color}='red'} \text{Boats}) \bowtie \text{Reserves}))$$

$$\rho(\text{Tempgreen}, \pi_{\text{sid}}((\sigma_{\text{color}='green'} \text{Boats}) \bowtie \text{Reserves}))$$

$$\pi_{\text{sname}}((\text{Tempred} \cap \text{Tempgreen}) \bowtie \text{Sailors})$$

Find the names of sailors who've reserved *all* boats



Sailors

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

Reserves

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

Boats

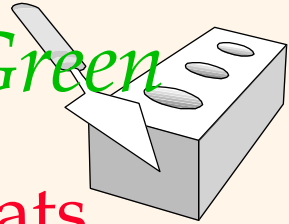
<u>bid</u>	<u>Color</u>
101	Red
103	Green

- ❖ Uses division; schemas of the input relations to / must be carefully chosen:

$$\rho(\text{Tempsids}, (\pi_{\text{sid}, \text{bid}} \text{Reserves}) / (\pi_{\text{bid}} \text{Boats}))$$

$$\pi_{\text{sname}} (\text{Tempsids} \bowtie \text{Sailors})$$

Find the names of sailors who've reserved **all Green** boats



**Sailors**

<u>sid</u>	sname	rating	age
22	dustin	7	45.0
31	lubber	8	55.5
58	rusty	10	35.0

**Reserves**

<u>sid</u>	<u>bid</u>	<u>day</u>
22	101	10/10/96
58	103	11/12/96

**Boats**

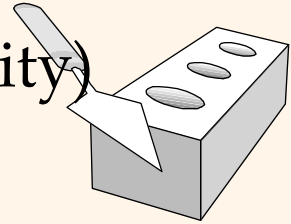
<u>bid</u>	<u>Color</u>
101	Red
103	Green

$$\rho(\text{Tempsids}, (\pi_{\text{sid}, \text{bid}} \text{Reserves}) / (\pi_{\text{bid}} (\sigma_{\text{Color} = \text{'Green'}} \text{Boats})))$$

$$\pi_{\text{sname}} (\text{Tempsids} \bowtie \text{Sailors})$$

*Example*

- ❖ Employee (ID, person\_name, street, city)
- ❖ Works (ID, company\_name, salary)
- ❖ Company (company\_name, city)



- ❖ Find the names of employees who live in Miami

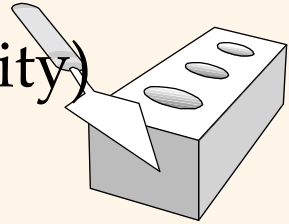
$$\Pi_{person\_name} (\sigma_{city = "Miami"} (employee) )$$

- ❖ Find the names of employees whose salary is more than \$100K

$$\Pi_{person\_name} (\sigma_{salary > 100K} (employee \bowtie_{ID} works) )$$

*Example*

- ❖ Employee (ID, person\_name, street, city)
- ❖ Works (ID, company\_name, salary)
- ❖ Company (company\_name, city)

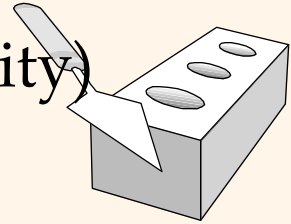


- ❖ Find the names of employees who live in Miami and whose salary is more than \$100K

$$\Pi_{person\_name} (\sigma_{city = \text{“Miami”} \text{ AND } salary > 100K} (employee \bowtie_{ID} works) )$$

*Example*

- ❖ Employee (ID, person\_name, street, city)
- ❖ Works (ID, company\_name, salary)
- ❖ Company (company\_name, city)

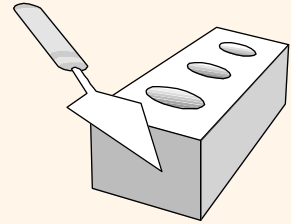


- ❖ Find the ID and name of each employee who does not work for BigBank

$$\Pi_{ID, person\_name} (employee) - \Pi_{ID, person\_name} (employee \bowtie_{ID} (\sigma_{company\_name = \text{BigBank}} (works)))$$



# Summary



- ❖ The relational model has rigorously defined query languages that are simple and powerful.
- ❖ Relational algebra is more operational; useful as internal representation for query evaluation plans.
- ❖ Several ways of expressing a given query; a query optimizer should choose the most efficient version.