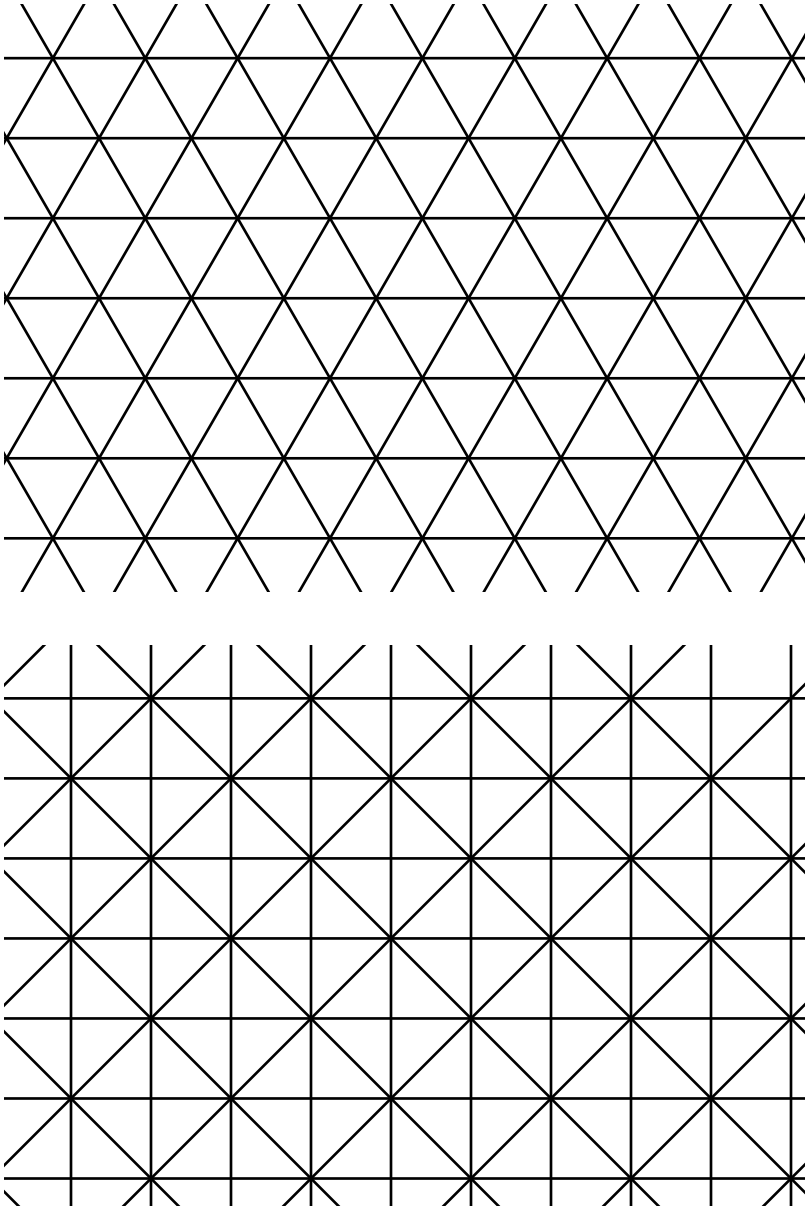

Two affine coxeter complexes: the top is type $\tilde{A}_2$, while the bottom is $\tilde{C}_2$.
In the former, every vertex is special, while in the latter only the vertices with four lines through them are special, the others not.