

CSci 8980, Fall 2012

Specifying and Reasoning About Computational Systems

Introduction to the Course

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Objectives for the Course

Expose a logic-based approach to the treatment of syntax-directed and rule driven descriptions

In particular, we will gain an understanding of at least the following aspects

- A logic programming approach to encoding rule-based specifications
- A logical approach to capturing the meta-theory of logic programming languages
- Foundational underpinnings of the different logical approaches
- Particular languages and programming systems that realize the above capabilities
- Computational aspects that make the systems work

Motivation for Studying these Topics

Syntax-driven and rule based specifications are commonly used for describing computational notions

For example, the following are typically described in this way

- semantics of programming language constructs
- typing in programming languages
- natural deduction and sequent calculi
- software modelling languages (e.g. π -calculus)

Moreover, these specifications are often used as the basis for (informal) reasoning about the systems

Logics for formalizing such specifications and reasoning can be used to provide computer-based support for these activities

Motivations (Continued)

More specifically, satisfying the agenda will require providing a means to do the following:

- Transparently encoding syntax-based descriptions
 - **succinct, declarative representation of objects treated**
 - **logic-based encoding of all aspects of rules**
- Prototyping based on specifications
 - **Effectively automatable proof search**
 - **Reflection of underlying computational structure**
- Reasoning through specifications
 - **characterizing positive and negative behaviour**
 - **specification properties should reflect actual system properties (adequacy)**

These requirements will guide the construction of the logics we discuss

Motivating Example (Formalizing mini-Lazy ML)

Syntax

$$ty ::= \text{int} \mid ty \rightarrow ty \quad e ::= x \mid e \ e \mid (\text{fn } x : ty \Rightarrow e)$$

Call-by-Name Evaluation ($e \Downarrow v$ means e evaluates to v)

$$\frac{}{(\text{fn } x : a \Rightarrow r) \Downarrow (\text{fn } x : a \Rightarrow r)}$$
$$\frac{m \Downarrow (\text{fn } x : a \Rightarrow r) \quad r[n/x] \Downarrow v}{(m \ n) \Downarrow v}$$

Typing Rules ($\Gamma \vdash e : ty$ means e has type ty relative to Γ)

$$\frac{x : a \in \Gamma}{\Gamma \vdash x : a} \quad \frac{\Gamma \vdash m : a \rightarrow b \quad \Gamma \vdash n : a}{\Gamma \vdash (m \ n) : b}$$
$$\frac{\Gamma, x : a \vdash r : b}{\Gamma \vdash (\text{fn } x : a \Rightarrow r) : a \rightarrow b} \quad x \notin \text{dom}(\Gamma)$$

Motivating Example (Continued)

In the setting of these specifications, we want to be able to provide the following kinds of capabilities:

- An easy to use and transparently correct representation of types and terms
- A formalization of *all* aspects of the different rules, especially the side conditions
- Executability of the formalization
- Reasoning about the formalization
 - E.g. we would want to derive properties such as
 - Determinateness of evaluation
 - Preservation of typing by evaluation
 - Uniqueness of typing
- Transference of the properties to the actual system

Realizing the Desired Capabilities

Our realization of the capabilities we desire will rely on the following logical devices:

- a rich, higher-order logic for logic programming
- the use of lambda terms as data structures
- logics of definitions (with induction and co-induction)
- differentiation between intensional and extensional universal quantification
- two-level logic form of reasoning

We will develop an understanding of these notions at different points in the course