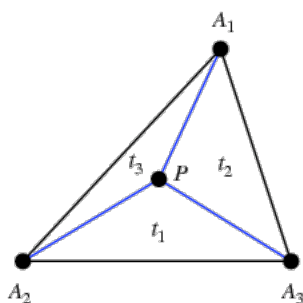


Next week we're learn about *barycentric coordinates*. Given any triangle  $\triangle ABC$ , it turns out you can write any point  $X \in \mathbb{R}^2$  as a unique linear combination of the vertices:

$$X = rA + sB + tC.$$

where  $r$ ,  $s$  and  $t$  satisfy the condition  $r + s + t = 1$ . These numbers are the *barycentric coordinates of  $X$  based on  $\triangle ABC$* , and we'll sometimes write  $X = (r, s, t)^{\triangle ABC}$ .

In class we'll talk about *why* we might care about this, but for now this lab will let you experiment with another interpretation of barycentric coordinates. As illustrated in this diagram from Mathworld, if  $P = t_1A_1 + t_2A_2 + t_3A_3$ , where  $P$  is inside the triangle and  $t_1 + t_2 + t_3 = 1$ , then  $t_1$  represents the area of triangle  $PA_2A_3$  as a percentage of the area of the whole triangle. Similarly,  $t_2$  represents the area of the triangle  $PA_1A_3$  as a percentage of the whole triangle, and  $t_3$  represents the percentage of  $PA_1A_2$ .



GEOGEBRA CONSTRUCTION

- (1) Open a new GeoGebra window. Define a triangle with vertices  $A = (-1, 1)$ ,  $B = (2, -1)$  and  $C = (3, 3)$ . If this is the first thing you've done, GeoGebra will also show a dependent object called `poly1` which represents the area of this triangle. Right click on the name (or the interior of the triangle) and rename it `totalArea`.
- (2) Define a point  $P$  somewhere inside the triangle (e.g.  $(1, 1)$ ).
- (3) Define the triangle `ta = Polygon[P, B, C]`; you can either enter this command in the Input Field below, or choose the Polygon tool and click on those points. (You can then rename the Polygon to `ta` in that case.) Define triangles `tb` and `tc` as appropriate. You should now see the triangle  $ABC$  split into three smaller triangles which meet at  $P$ , similar to the picture above.
- (4) You are now ready to define the barycentric coordinates of your point  $P$ . In the input field below, enter

$$\mathbf{r} = \mathbf{ta} / \mathbf{totalArea}$$

followed by appropriate definitions for  $\mathbf{s}$  and  $\mathbf{t}$ .

- (5) To check your coordinates, defined a point  $Q$  by typing `Q = r*A + s*B + t*C` in the input field. The new point  $Q$  should be superimposed on the point  $P$  if you've done everything correctly.
- (6) Test your construction by moving the points  $A$ ,  $B$ ,  $C$ , and  $P$ . What happens when you move  $P$  outside of the triangle? On Monday we'll learn about the "quadrants" of the barycentric plane, after which you might be able to see why  $Q$  is in the wrong place.

To receive credit for this assignment, save your file as `lastname-5335-lab3.ggb` and email it to me as an attachment by the beginning of class on Wednesday, 10/28/15. Before you send it to me, you should spend a bit of time right-clicking on unnecessary labels and hiding them, etc., to make everything look nice!