

Exam 2 covers the material from the first midterm until this week – Chapters 7 through 11, as described below. You don't need to know the material from Chapter 12 that we covered on Wednesday.

As far as the type of problem, you can expect a mixture similar to the first exam. Most will be very similar to homework problems and/or propositions or theorems which we devoted a lot of class time to. Somewhere on the exam you might be asked to prove things we haven't done in class. *Don't freak out and think "I've never seen this!"* That's the point: to check if you understand the definitions and techniques well enough to apply them in a slightly different setting. If you're comfortable with the material from class, you'll be well equipped to figure out anything on the exam.

In general, I'm much more interested in whether you can explain concepts than regurgitate facts. I couldn't care less if you've memorized a long formula for the circumcenter of $\triangle ABC$. But I'm very interested in whether you can use what you know about perpendicular bisectors to explain how you know the perpendicular bisectors of the sides of $\triangle ABC$ must meet in a point.

As before, the exam is closed book, closed notes, closed calculator, etc. Don't trivialize a problem, meaning if I ask you to prove a result from class, you shouldn't just cite the theorem.

Don't forget about the various handouts and activities I've asked you to work on in class! If you need new copies, you can get them on the webpage.

A few words of advice, by chapter:

Chapter 7: In addition to the basic definitions in the chapter, you should know what medians, altitudes, perpendicular bisectors and angle bisectors are, and where they meet. There are various "concurrency" theorems and formulas. Proving the perpendicular bisectors are concurrent (and explaining why the circumcenter is the center of the circumcircle) is pretty reasonable for an exam. Same for the angle bisectors and incenter. Proving the medians are concurrent is a cute little application of parametric lines, but I'm not so interested in whether you can memorize a bunch of expressions with $1/2$'s, $1/3$'s and $2/3$'s. I'd probably be more interested in applications of the median, like the homework problem that showed the medians split a triangle into six smaller (not necessarily congruent) triangles which all have area $1/6$ that of the original triangle.

Under no circumstances should you start memorizing the formulas for barycentric coordinates of the feet of the altitudes, the orthocenter, etc. Don't memorize formulas for the circumradius, or inradius. We can be glad somebody has figured those out, but I have other things I can test you on.

Suggested additional review problems: any of the HW, plus 7.34

Chapter 8: Major results like Proposition 8.4 are important; results like Theorem 8.5 or Propositions 8.6 and 8.7 are useful, but rather than memorizing them you could aim to become familiar enough with the methods of this chapter so you could prove them if needed. One suggestion I can make is that you shouldn't be afraid of "vector methods" – i.e. doing calculations involving the vertices of a quadrangle or the vectors between them. [See the proofs we did in class involving parts and (vi) of Proposition 8.4, for example, or the proof of Theorem 8.5.] The parts of the chapter that we skimmed over in class (e.g. much of the material on circles) won't be emphasized on the exam. That doesn't mean circles won't appear, or that you can't use basic facts about circles (radius perpendicular to a tangent line, for example) but you wouldn't ever have to

prove Theorem 8.18, for example.

Suggested additional review problems: any of the HW, plus 8.21, 8.24, 8.25, 8.26, 8.29

Chapter 9: You should know the definitions of conformal affinity and similarity, and be able to do the types of problems involving similar triangles that we did in class. The big (and new) topic in this chapter is circle inversion, which we've also referred to as "reflecting" across a circle. You should be rock-solid with the formula to invert X across a circle of radius ρ centered at the origin, as well as the geometric definition – $X' = \mathcal{I}(X)$ is the point on $\overrightarrow{OX}$ such that $|\overrightarrow{OX}| \cdot |\overrightarrow{OX'}| = \rho^2$. You should be able to use both of those definitions to find the reflection of any line or circle in the plane. Finally, you should be able to do all of that (definitions, images of lines and circles) if the mirror is centered somewhere other than the origin, as well. You should be aware that circle inversion is conformal, and what that means, but you needn't be able to prove it.

Suggested additional review problems: any of the HW, plus 9.6, 9.11, 9.13, and 9.6 with mirror $(x+1)^2 + y^2 = 4$.

Chapter 10: Do **not** spend time memorizing the axioms in this chapter. If I want you to say anything about an axiom, I'll provide it for you on the exam. The basic definitions and properties of lines and distances in the Poincaré Half Plane comprise the important material in this chapter. You don't need to memorize the formulas 10.6 and 10.7 on page 171. If I want you to use those, I'll provide them – or it will be a situation where you can figure out ω and ρ with other methods. You should be able to find the distance between two points on a Poincaré line.

Suggested additional review problems: 10.32.

Chapter 11: We covered the distance formula in Theorem 11.1 back in Chapter 10, but you don't need to memorize it. You should be familiar with Poincaré Direction indicators, but don't need to know the cross ratio formulas to determine whether two Poincaré lines intersect, and don't memorize the formulas we covered for angles. If you have to find angles, the problems will be similar to ones we've done in class, where you can use our knowledge of Euclidean angles to figure out the measure of the Poincaré angle. You should also be familiar with the area of triangles and asymptotic triangles. That doesn't mean you have to memorize Lemma 11.13 and how it's used to find the area of certain kinds of triply or doubly asymptotic triangles. I'm not looking to ask multivariable calculus questions. But knowing how to, say, make use of the formula for area of doubly asymptotic triangles to find the area of a singly asymptotic triangle is important.

Suggested additional review problems: 11.10, 11.24, 11.25

I've included a lot of possible review problems. The goal is not for you to do every single one of them and memorize their solutions. Pick and choose as appropriate; if you're very confident with chapter 8 you don't need to spend much time there. If you're not as sure of chapter 9 you might want to look at a few more of those review problems. (And make sure you review any homework problems and in-class activities first!) As always, please feel free to email me with questions.