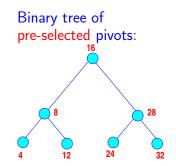
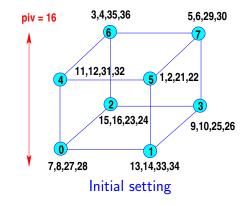
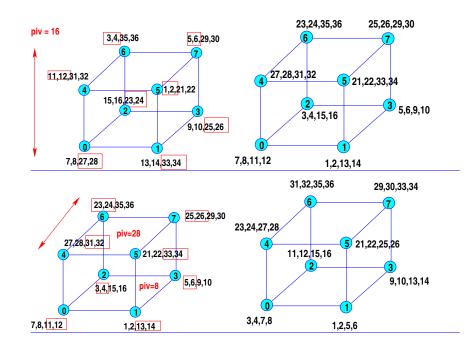
## An Illustration: hypercube Quicksort

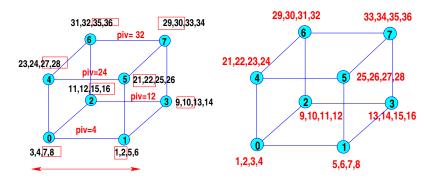
- ➤ Goal: to sort *n* numbers with parallel version of Quicksort.
- **Example:** The sequence of numbers is: 1,2 ..., 16, 21, 22,..., 36











# COMMUNICATION OPERATIONS AND MESSAGE PASSING

- Introduction to programming with message passing
- A preview of MPI interface
- Broadcast operations
- All-to-all broadcast and reduction operations
- Scatter and Gather operations
- All-to-all personalized communication

8-3 \_\_\_\_\_\_ - HQ

## Introduction to message-passing

➤ Need to explicitly code the exchange of messages [data, control,..]

**Example:** Revisit the sum example seen earlier

#### Parallel Sum of $m{n}$ numbers

```
for (j=0; j<p; j++) { // Parallel Loop
    tmp[j]=0;
//----- compute partial sums
    for (i=j*m; i<(j+1)*m; i++)
    tmp[j] += + x[i];
}
//----- sum-up partial sums
s=0;
for (j=0; j<p; j++) // Sequential loop
    s+=tmp[j];</pre>
```

8-5 — comm

8-5

ightharpoonup REDUCE(sum, tmp, 'ADD') adds 'tmp' from each PE into 'sum'

- ➤ Can do reductions with add, multiply, max, min, etc..
- More on reductions later.
- Next: we will see some of the common communication fucntions used –
- On occasion we will see their implementation with MPI
- MPI will be covered in more detail later

Let "root" = 'master' node where the sum ends up. Recall: m=n/p

#### Parallel sum with communication

```
{     ...
     if (myid == root) {
        read/ generate array x ;
        for (j=0; j
```

8-6 — comm

8-

#### Communication 'kernels'

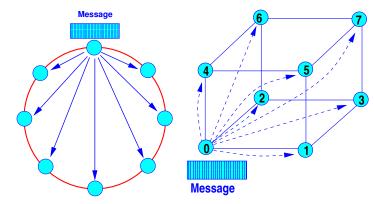
### Typical questions addressed:

- 1. Identify the important communication operations
- 2. Find effective algorithms for performing these on distributed memory computers
- 3. Analyze their cost
- ➤ A by-product: some framework for generic algorithms

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### Example: Broadcast operation

➤ Sending a message from a 'root' node to all nodes is a Broadcast

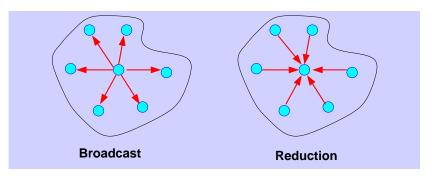


**Questions:** Best way to broadcast a message from a root node to all others in a ring? In hypercube?

- In parallel sum example, could replace the sends of x(j\*m:(j+1)\*m-1) from root to all others by a broadcast of all x from root of the vector x. Lines 1-6 replaced by:
  - 1. broadcast(x, root)
- Note however that each PE will get the whole vector.
- Corresponding MPI code provided in class web-site

### Standard broadcast and reduction operations

- ➤ Reduction does a global operation (e.g. a sum) on items located on all processors onto a 'root' processor
- ➤ Can be viewed as a sort of inverse of the broadcast

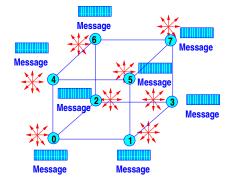


8-10 \_\_\_\_\_\_ — comm

8-10

## All-to-all broadcast and reduction

- ➤ All-to-all broadcast can be viewed as **p** broadcasts, one from each node.
- Similarly: All-to-all reduction is a reduction to each node (different for each node).



*Note:* All-reduce ( $\neq$  all-to-all reduce) is a reduction operation in which the result of reduction is available in each processor

➤ All-reduce achievable by a reduce followed by a broadcast [not best way]

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- comm

➤ Important application of all-reduce: testing if an algorithm has "converged".

**Example:** Test would be something like:

if 
$$\displaystyle \max_{i=0,...,p-1} |x_k^i - x_{k+1}^i| <$$
 then stop

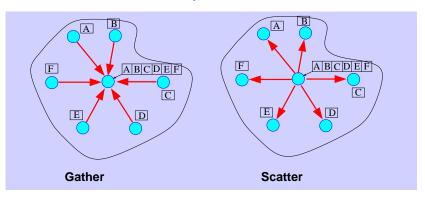
- lacksquare Variable i= processor, variable k= iteration number
- lacksquare Need to know  $\max_i |x_k^i x_{k+1}^i|$  in each processor.
- > See text for algorithms on linear array, ring, and hypercubes

8-13 \_\_\_\_\_\_ - comm

8-13

Gather and scatter operations

- ➤ Scatter is similar to a broadcast but a different item is sent to each processor -
- Gather does the inverse operation.

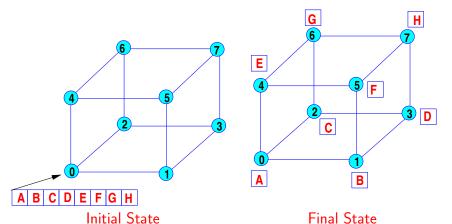


- comm

8-14

∠
Mow would you implement a Scatter operation on a hypercube?

**∠** Cost?



Example:

For the parallel sum example – we can "scatter" the subvectors to be summed up in each processors.

➤ In parallel sum algorithm, the lines

```
for(j=0; j
```

are replaced by

```
scatter(x)
```

-15 - comm

8-16

# $All\-to\-All\ personalized\ communication$

Can be viewed as a scatter from each node: each node sends a distinct message to every other node.

$P_0 oxedownows A_0 oxedownows A_1 oxedownows A_2 oxedownows A_3$	$P_0$	$oxed{A_0 B_0 C_0 D_0}$
$P_1 oxedsymbol{B_0} oxedsymbol{B_1} oxedsymbol{B_2} oxedsymbol{B_3}$	$P_1$	$oxed{A_1 B_1 C_1 D_1}$
$P_2 oxedownowbell C_0 oxedownowbell C_1 oxedownowbell C_2 oxedownowbell C_3$	$ ightharpoonup_2$	$oxed{A_2 B_2 C_2 D_2}$
$P_3  \overline{D_0}  \overline{D_1}  \overline{D_2}  \overline{D_3} $	$P_3$	$oxed{A_3 B_3 C_3 D_3}$

- > Equivalent to *p* gathers too (0ne to each node)
- ightharpoonup Notice : operation amounts to transposing a  $p \times p$  array!

How would you code an all-to-all communication on a hypercube?

8-17 — comr

8-17