

What is special about mining spatial data?

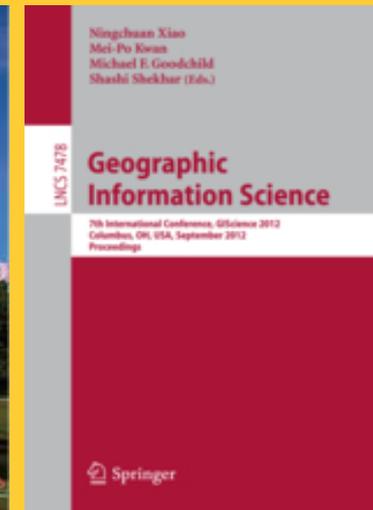
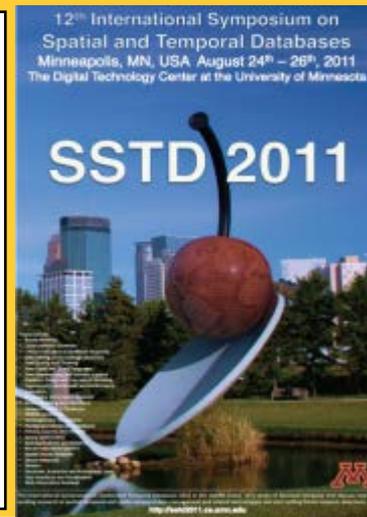
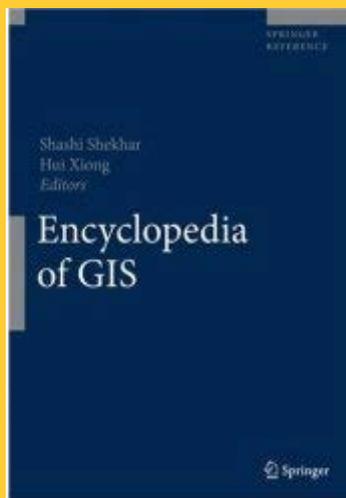
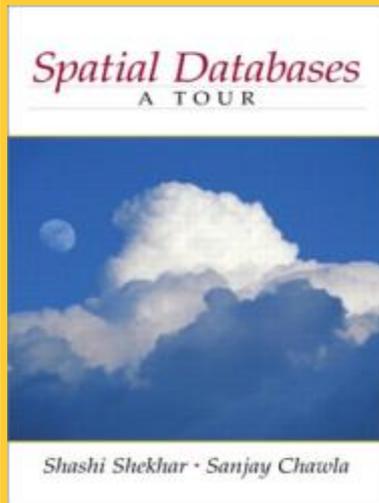
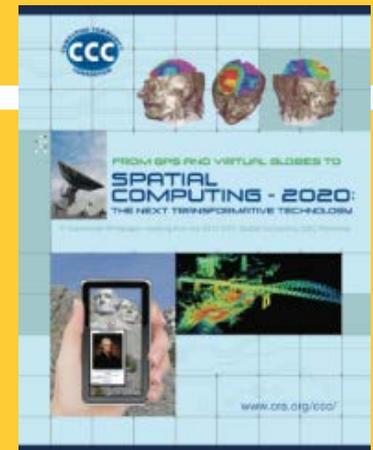
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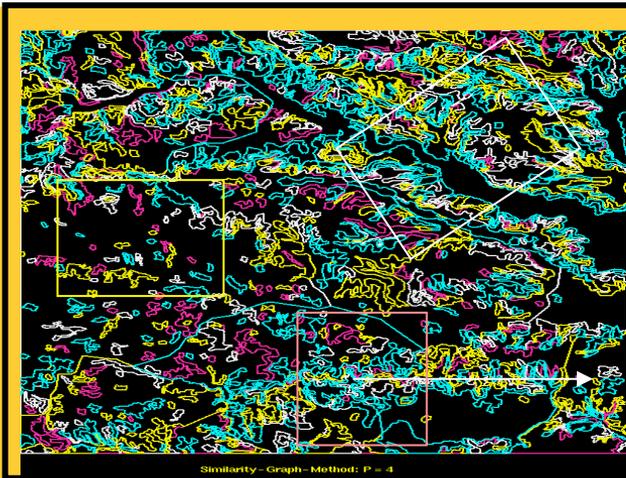


UNIVERSITY OF MINNESOTA

Driven to DiscoverSM

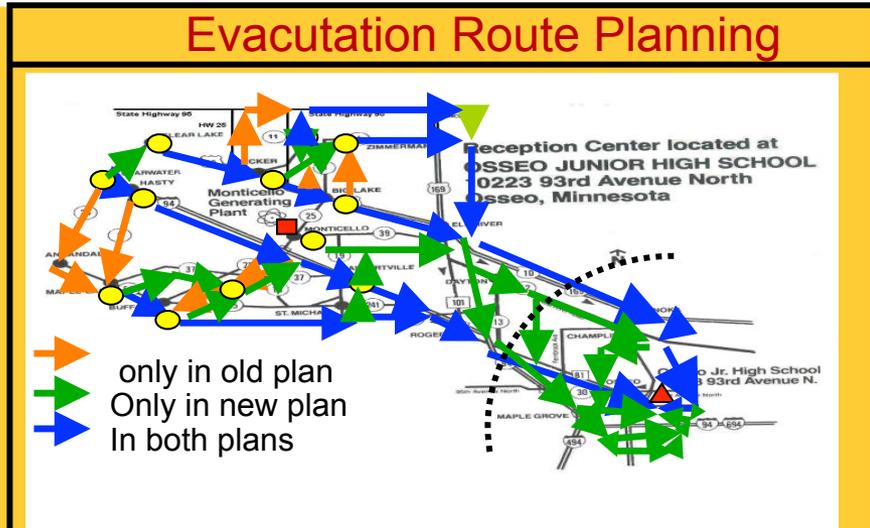
Spatial Databases: Representative Projects

Details: Spatial Databases: Accomplishments and Research Needs, IEEE Transactions on Knowledge and Data Engineering, 11(1), 1999. (and recent update via a technical report)



Parallelize
Range
Queries

Evacuation Route Planning



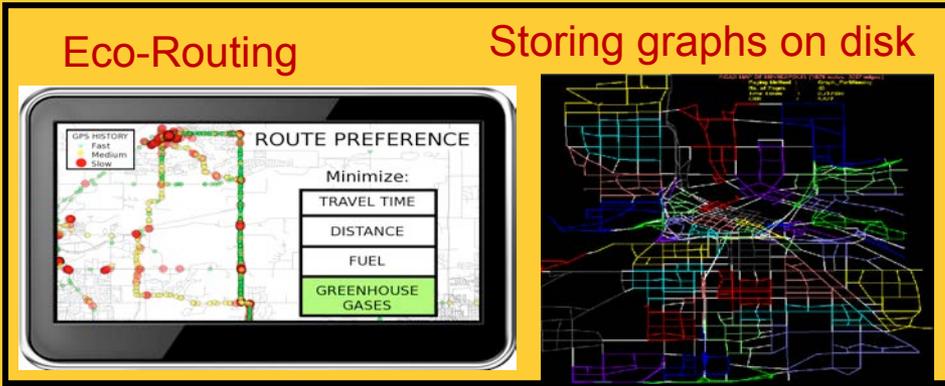
Reception Center located at
OSSEO JUNIOR HIGH SCHOOL
0223 93rd Avenue North
Osseo, Minnesota

Monticello Generating Plant

Legend:
Orange arrow: only in old plan
Green arrow: Only in new plan
Blue arrow: In both plans

Eco-Routing

Storing graphs on disk



ROUTE PREFERENCE

Minimize:

- TRAVEL TIME
- DISTANCE
- FUEL
- GREENHOUSE GASES

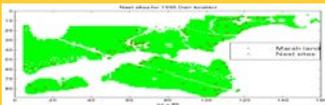


Spatial Data Mining: Example Projects

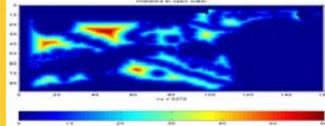
Details: Identifying patterns in spatial information: a survey of methods, Wiley Interdisc.
Reviews: Data Mining and Know. Discovery , 1(3):193-214, May/June 2011

Location prediction: nesting sites

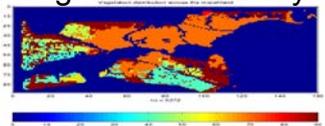
Nest locations



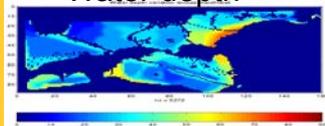
Distance to open water



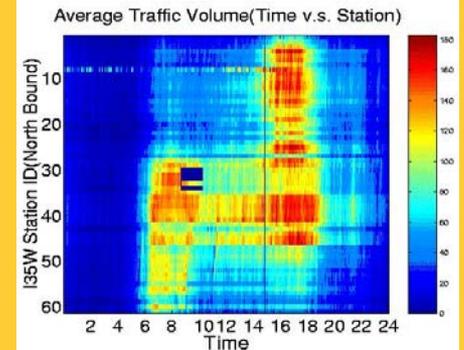
Vegetation durability



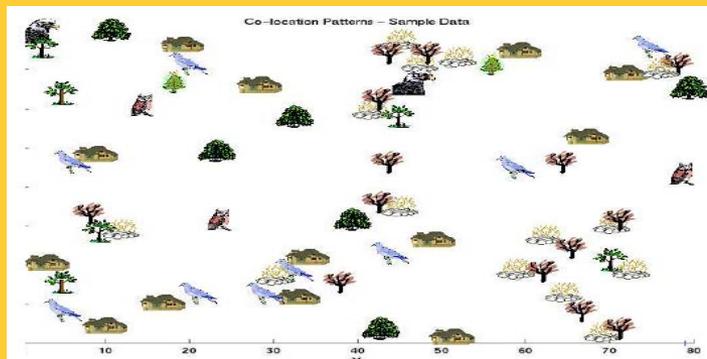
Water depth



Spatial outliers: sensor (#9) on I-35



Co-location Patterns



Spatial Network Activity Summarization



Input: k = 4, 43 fatalities



Network Distance



Euclidean Distance



KMR

Outline

- Motivation
 - Use cases
 - Pattern families
- Spatial Data Types
- Spatial Statistical Foundations
- Spatial Data Mining
- Conclusions



Why Data Mining?

- Holy Grail - Informed Decision Making
- Sensors & Databases **increased** rate of Data Collection
 - Transactions, Web logs, GPS-track, Remote sensing, ...
- Challenges:
 - Volume (data) >> number of human analysts
 - Some automation needed
- Approaches
 - Database Querying, e.g., SQL3/OGIS
 - Data Mining for Patterns
 - ...

Data Mining vs. Database Querying

- Database Querying (e.g., SQL3/OGIS)
 - Does not answer questions about items not in the database!
 - Ex. Predict tomorrow's weather or credit-worthiness of a new customer
 - Does not efficiently answer complex questions beyond joins
 - Ex. What are natural groups of customers?
 - Ex. Which subsets of items are bought together?
- Data Mining may help with above questions!
 - Prediction Models
 - Clustering, Associations, ...

Spatial Data Mining (SDM)

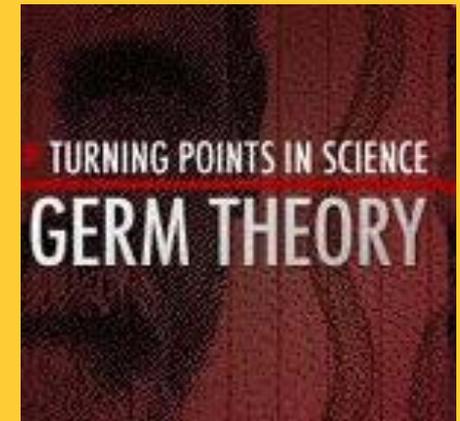
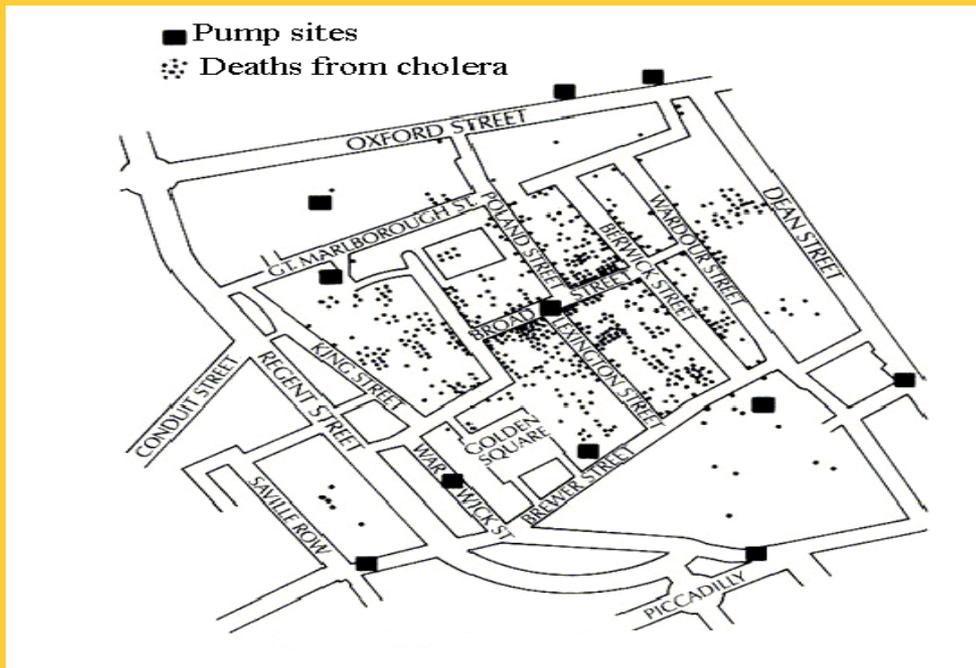
- The process of discovering
 - interesting, useful, non-trivial **patterns**
 - patterns: non-specialist
 - exception to patterns: specialist
 - from large **spatial** datasets

- Spatial pattern families
 - Hotspots, Spatial clusters
 - Spatial outlier, discontinuities
 - Co-locations, co-occurrences
 - Location prediction models
 - ...



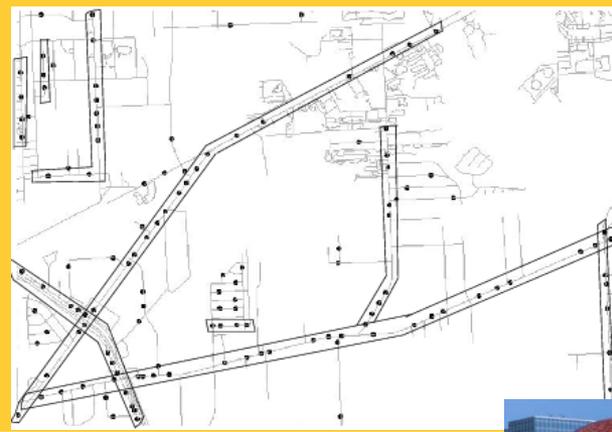
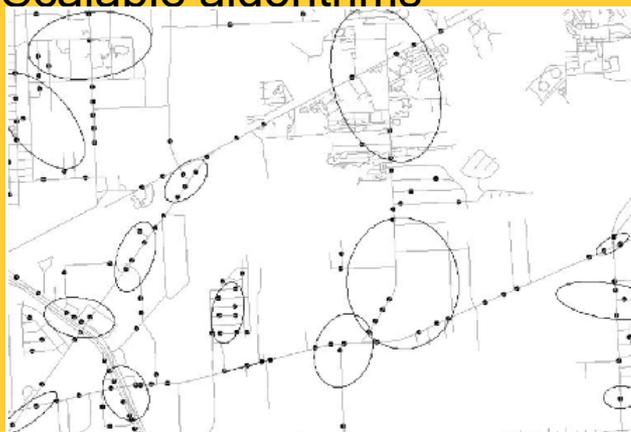
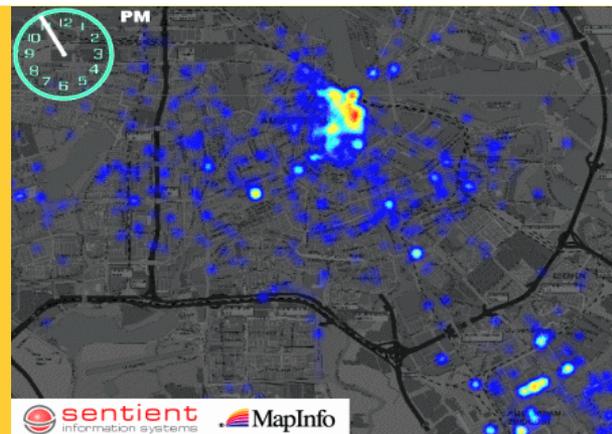
Pattern Family 1: Hotspots, Spatial Cluster

- The 1854 Asiatic Cholera in London
 - Near Broad St. water pump except a brewery



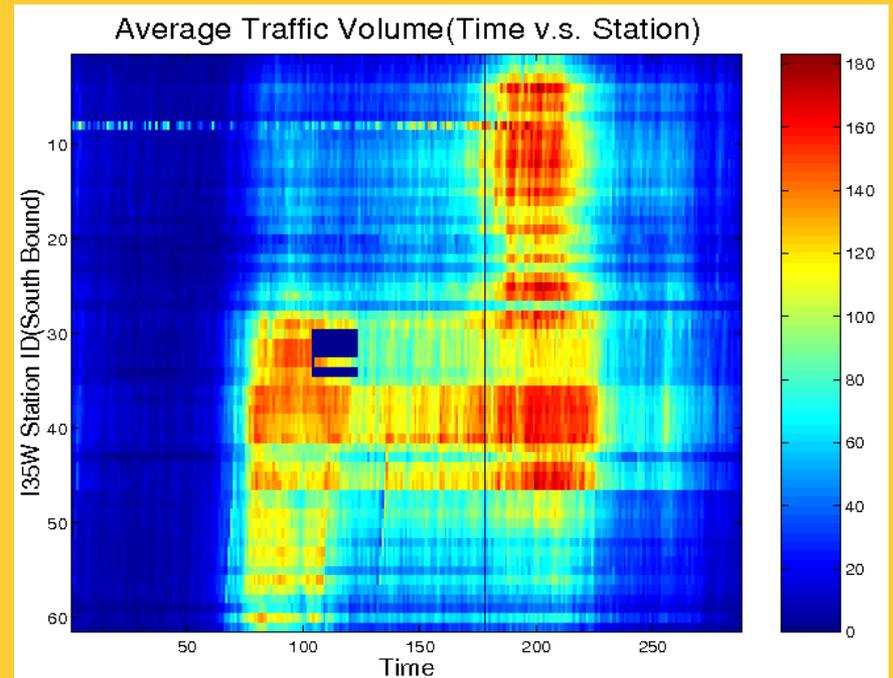
Complicated Hotspots

- Complication Dimensions
 - Time
 - Spatial Networks
- Challenges: **Trade-off** b/w
 - Semantic richness and
 - Scalable algorithms



Pattern Family 2: Spatial Outliers

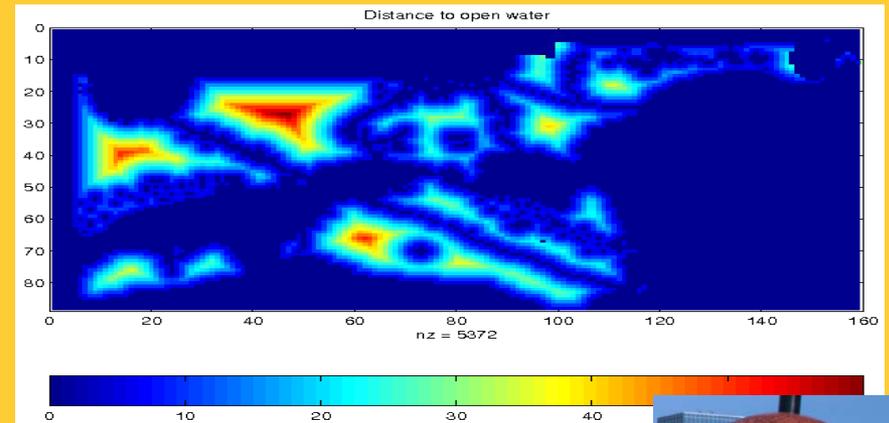
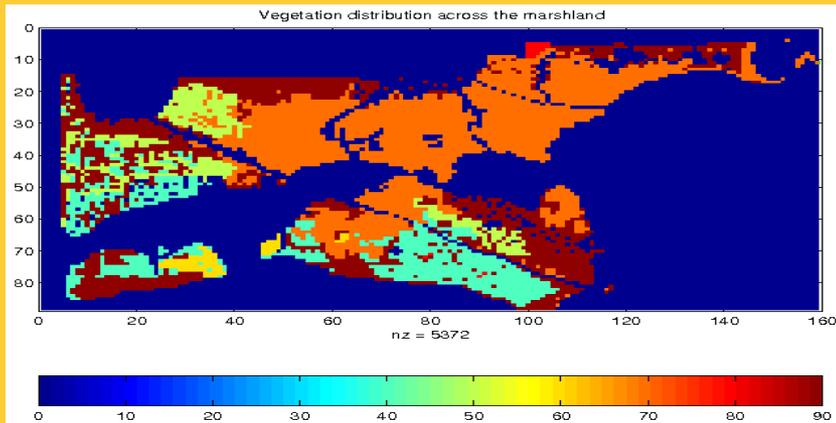
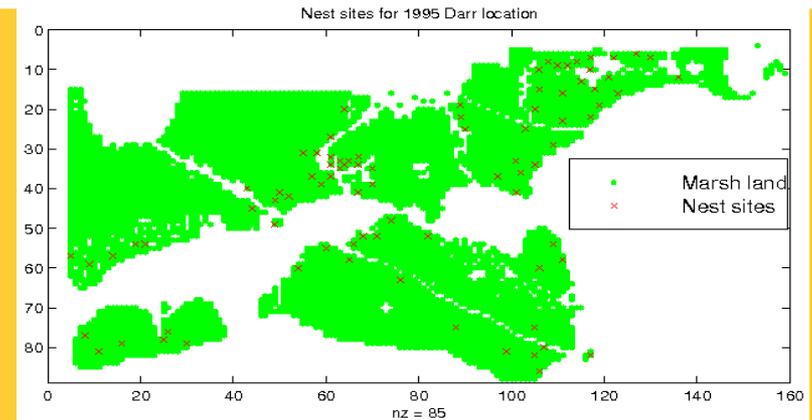
- Spatial Outliers, Anomalies, Discontinuities
 - Traffic Data in Twin Cities
 - Abnormal Sensor Detections
 - Spatial and Temporal Outliers



Source: A Unified Approach to Detecting Spatial Outliers, *Geoinformatica*, 7(2), Springer, June 2003.
(A Summary in Proc. ACM SIGKDD 2001) with C.-T. Lu, P. Zhang.

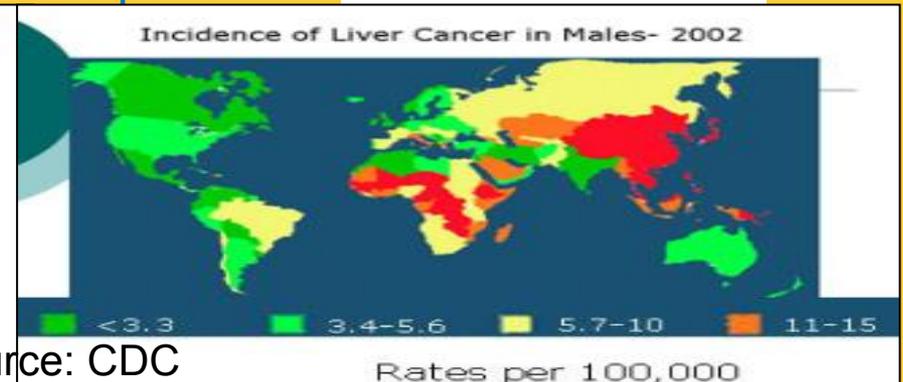
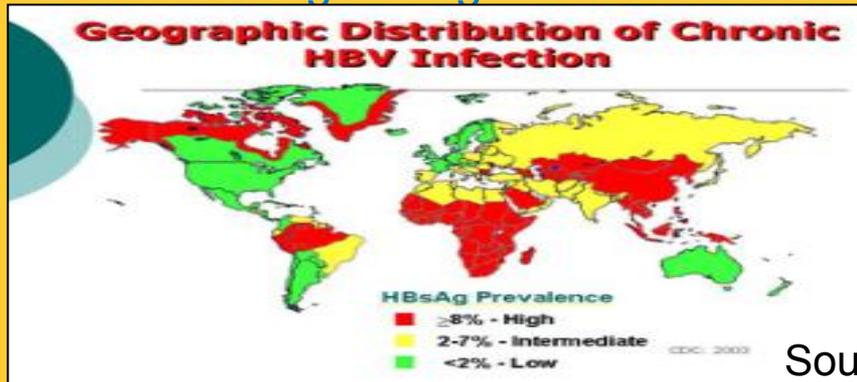
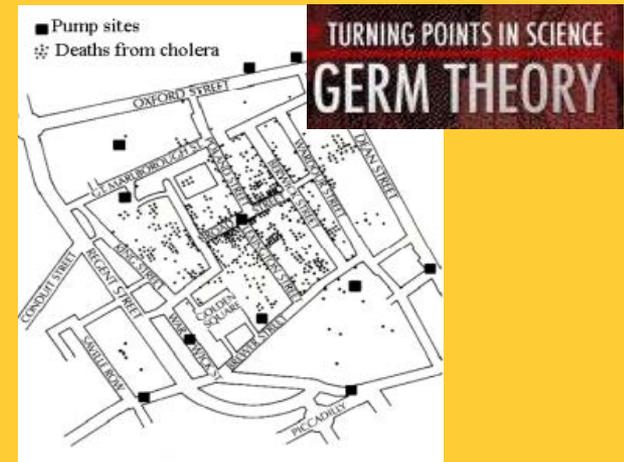
Pattern Family 3: Predictive Models

- Location Prediction:
 - Predict Bird Habitat Prediction
 - Using environmental variables



Family 4: Co-location, Co-occurrence

- Co-location (Cholera Deaths, Water Pump)
 - Hypothesis: Cholera is water-borne (1854)
 - Miasma theory => Germ Theory
- Co-location (Liver Cancer, HBV infection)
- Which exposures and cancers are co-located?
 - **Challenge: Large number of candidate pairs!**

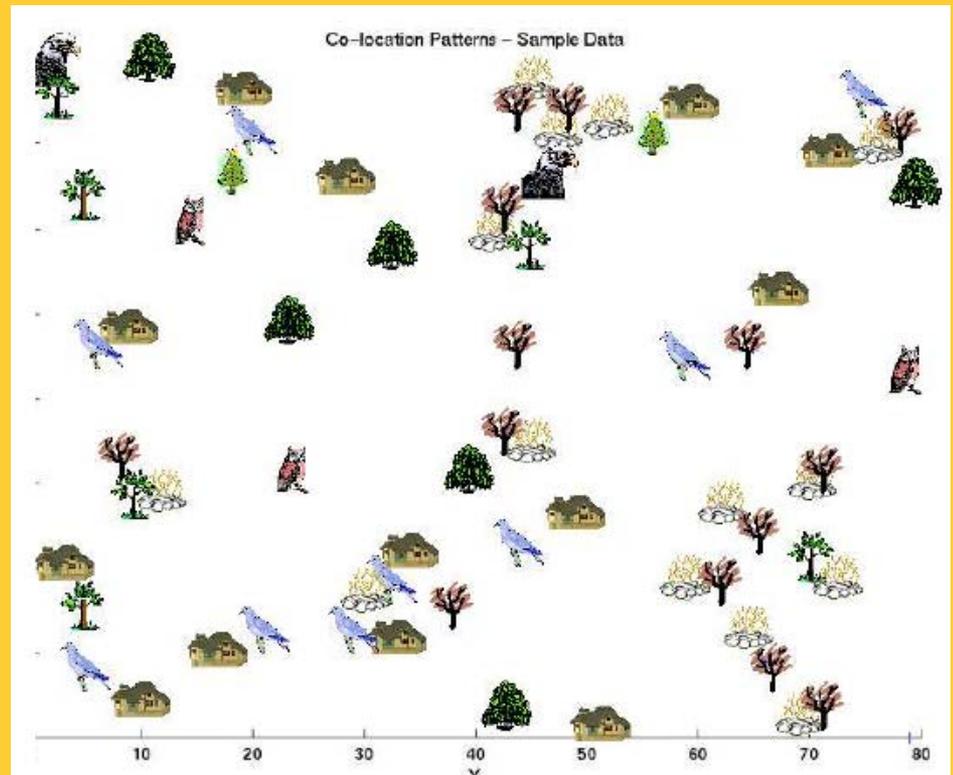


Source: CDC

Family 4: Co-locations/Co-occurrence

- Given: A collection of different types of spatial events
- Find: Co-located subsets of event types

Answers:   and  



Source: Discovering Spatial Co-location Patterns: A General Approach, IEEE Transactions on Knowledge and Data Eng., 16(12), December 2004 (w/ H.Yan, H.Xiong).

What's NOT Spatial Data Mining (SDM)

- Simple Querying of Spatial Data
 - Find neighbors of Canada, or shortest path from Boston to Houston
- Testing **a** hypothesis via a primary data analysis
 - Ex. Is cancer rate inside Hinkley, CA higher than outside ?
 - SDM: Which places have significantly higher cancer rates?
- Uninteresting, **obvious** or well-known patterns
 - Ex. (Warmer winter in St. Paul, MN) => (warmer winter in Minneapolis, MN)
 - SDM: (Pacific warming, e.g. El Nino) => (warmer winter in Minneapolis, MN)
- Non-spatial data or pattern
 - Ex. Diaper and beer sales are correlated
 - SDM: Diaper and beer sales are correlated in **blue-collar areas** (weekday evening)



Review Quiz: Spatial Data Mining

- Categorize following into queries, hotspots, spatial outlier, colocation, location prediction:
 - (a) Which countries are very different from their neighbors?
 - (b) Which highway-stretches have abnormally high accident rates ?
 - (c) Forecast landfall location for a Hurricane brewing over an ocean?
 - (d) Which retail-store-types often co-locate in shopping malls?
 - (e) What is the distance between Beijing and Chicago?

Outline

- Motivation
- Spatial Data
 - Spatial Data Types & Relationships
 - OGIS Simple Feature Types
- Spatial Statistical Foundations
- Spatial Data Mining
- Conclusions

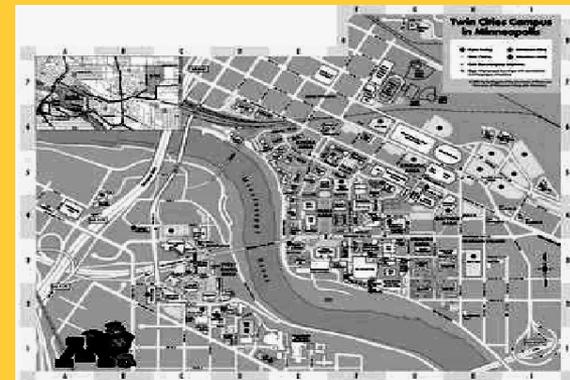


Data-Types: Non-Spatial vs. Spatial

- Non-spatial
 - Numbers, text-string, ...
 - e.g., city name, population
- Spatial (Geographically referenced)
 - Location, e.g., longitude, latitude, elevation
 - Neighborhood and extent
- Spatial Data-types
 - Raster: gridded space
 - Vector: point, line, polygon, ...
 - Graph: node, edge, path



Raster (Courtesy: UMN)



Vector (Courtesy: MapQuest)

Relationships: Non-spatial vs. Spatial

- Non-spatial Relationships
 - **Explicitly** stored in a database
 - Ex. New Delhi **is the capital of** India

- Spatial Relationships
 - **Implicit**, computed on demand
 - Topological: meet, within, overlap, ...
 - Directional: North, NE, left, above, behind, ...
 - Metric: distance, area, perimeter
 - Focal: slope
 - Zonal: highest point in a country
 - ...



OGC Simple Features

- Open GIS Consortium: Simple Feature Types
 - Vector data types: e.g. point, line, polygons
 - Spatial operations :

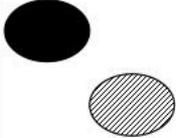
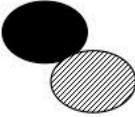
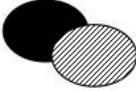
Operator Type	Operator Name
Basic Function	SpatialReference, Envelope, Boundary, Export, IsEmpty, IsSimple
Topological/Set Operations	Equal, Disjoint, Intersect, Touch, Cross, Within, Contains, Overlap
Spatial Analysis	Distance, Buffer, ConvexHull, Intersection, Union, Difference, SymmDiff

Examples of Operations in OGC Model

OGIS - Topological Operations

- Topology: 9-intersections
 - interior
 - boundary
 - exterior

Interior(B)	Boundary(B)	Exterior(B)	
$(A^\circ \cap B^\circ)$	$(A^\circ \cap \partial B)$	$(A^\circ \cap B^-)$	Interior(A) Boundary(A) Exterior(A)
$(\partial A \cap B^\circ)$	$(\partial A \cap \partial B)$	$(\partial A \cap B^-)$	
$(A^- \cap B^\circ)$	$(A^- \cap \partial B)$	$(A^- \cap B^-)$	

Topological Relationship				
	disjoint	meet	overlap	equal
9-intersection model	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 1 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$



Research Needs for Data

- Limitations of OGC Model
 - Direction predicates - e.g. absolute, ego-centric
 - 3D and visibility, Network analysis, Raster operations
 - Spatio-temporal
- Needs for New Standards & Research
 - Modeling richer spatial properties listed above
 - Spatio-temporal data, e.g., moving objects



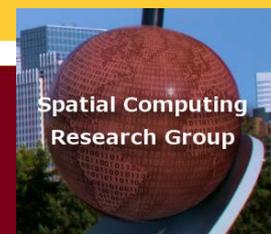
Outline

- Motivation
- Spatial Data Types
- **Spatial Statistical Foundations**
 - Spatial Auto-correlation
 - Heterogeneity
 - Edge Effect
- Spatial Data Mining
- Conclusions



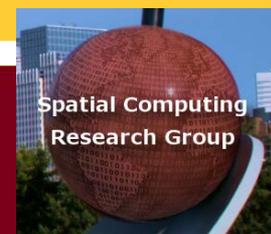
Limitations of Traditional Statistics

- Classical Statistics
 - Data samples: independent and identically distributed (i.i.d)
 - Simplifies mathematics underlying statistical methods, e.g., Linear Regression
- Spatial data samples are not independent
 - Spatial Autocorrelation metrics
 - distance-based (e.g., K-function), neighbor-based (e.g., Moran's I)
 - Spatial Cross-Correlation metrics
- Spatial Heterogeneity
 - Spatial data samples may not be identically distributed!
 - No two places on Earth are exactly alike!
- ...



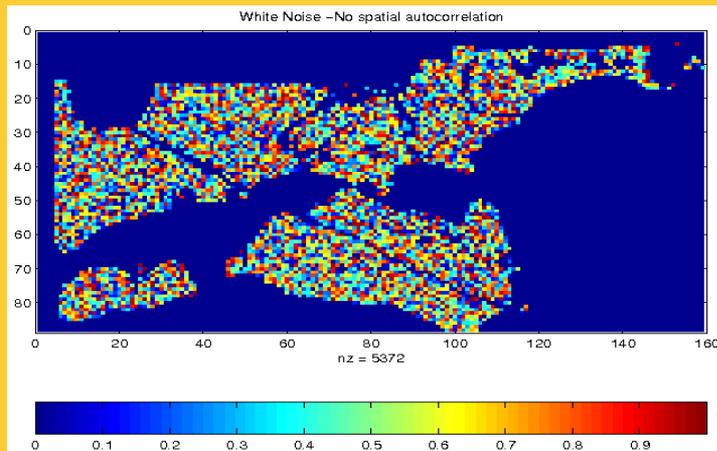
Spatial Statistics: An Overview

- Point process
 - Discrete points, e.g., locations of trees, accidents, crimes, ...
 - Complete spatial randomness (CSR): Poisson process in space
 - K-function: test of CSR
- Geostatistics
 - Continuous phenomena, e.g., rainfall, snow depth, ...
 - Methods: Variogram measure how similarity decreases with distance
 - Spatial interpolation, e.g., Kriging
- Lattice-based statistics
 - Polygonal aggregate data, e.g., census, disease rates, pixels in a raster
 - Spatial Gaussian models, Markov Random Fields, Spatial Autoregressive Model

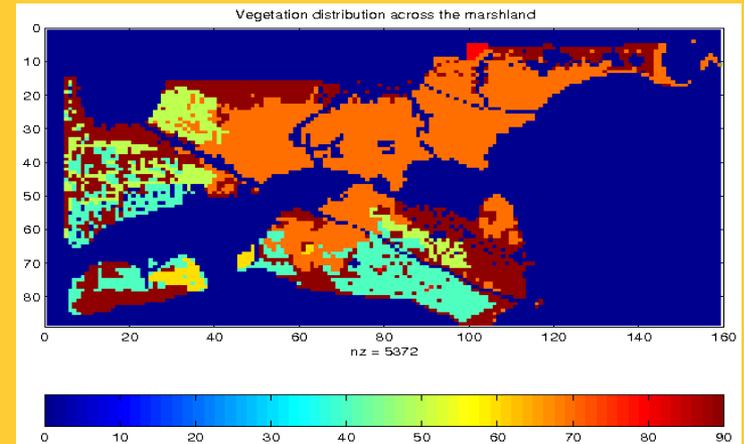


Spatial Autocorrelation (SA)

- First Law of Geography
 - All things are related, but nearby things are more related than distant things. [Tobler70]
- Spatial autocorrelation
 - Traditional i.i.d. assumption is not valid
 - Measures: K-function, Moran's I, Variogram, ...



Independent, Identically Distributed pixel property



Vegetation Durability with SA

Spatial Autocorrelation: K-Function

- **Purpose:** Compare a point dataset with a complete spatial random (CSR) data

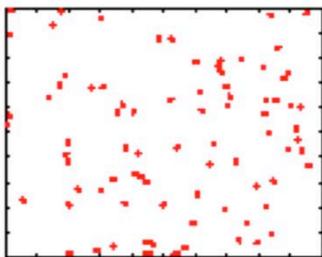
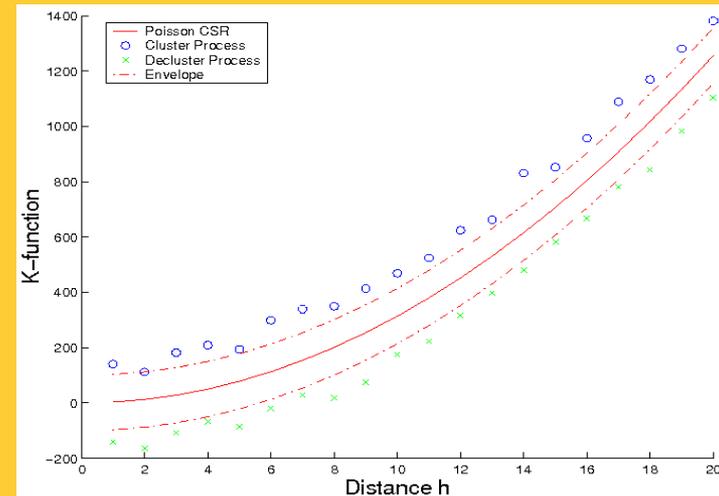
- **Input:** A set of points

$$K(h, data) = \lambda^{-1} E [\text{number of events within distance } h \text{ of an arbitrary event}]$$

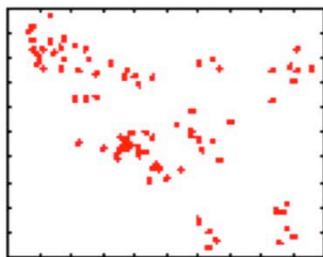
- where λ is intensity of event

- **Interpretation:** Compare $k(h, data)$ with $K(h, CSR)$

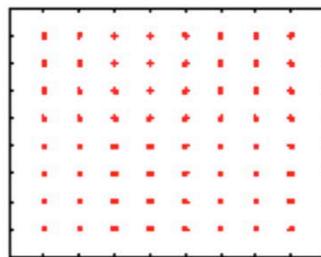
- $K(h, data) = k(h, CSR)$: Points are CSR
 - > means Points are clustered
 - < means Points are de-clustered



CSR



Clustered



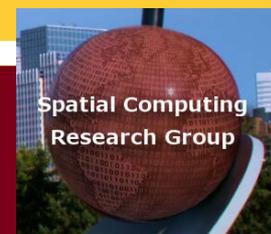
De-clustered

Cross-Correlation

- Cross K-Function Definition

$K_{ij}(h) = \lambda_j^{-1} E$ [number of type j event within distance h
of a randomly chosen type i event]

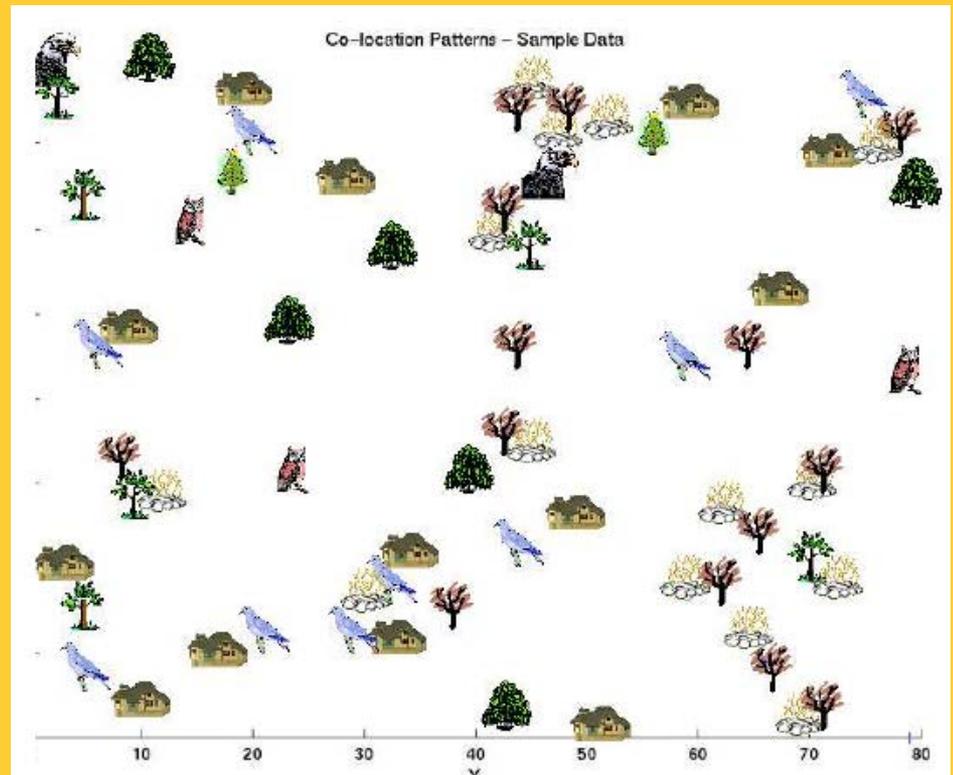
- Cross K-function of some pair of spatial feature types
- Example
 - Which pairs are frequently co-located
 - Statistical significance



Recall Pattern Family 4: Co-locations

- Given: A collection of different types of spatial events
- Find: Co-located subsets of event types

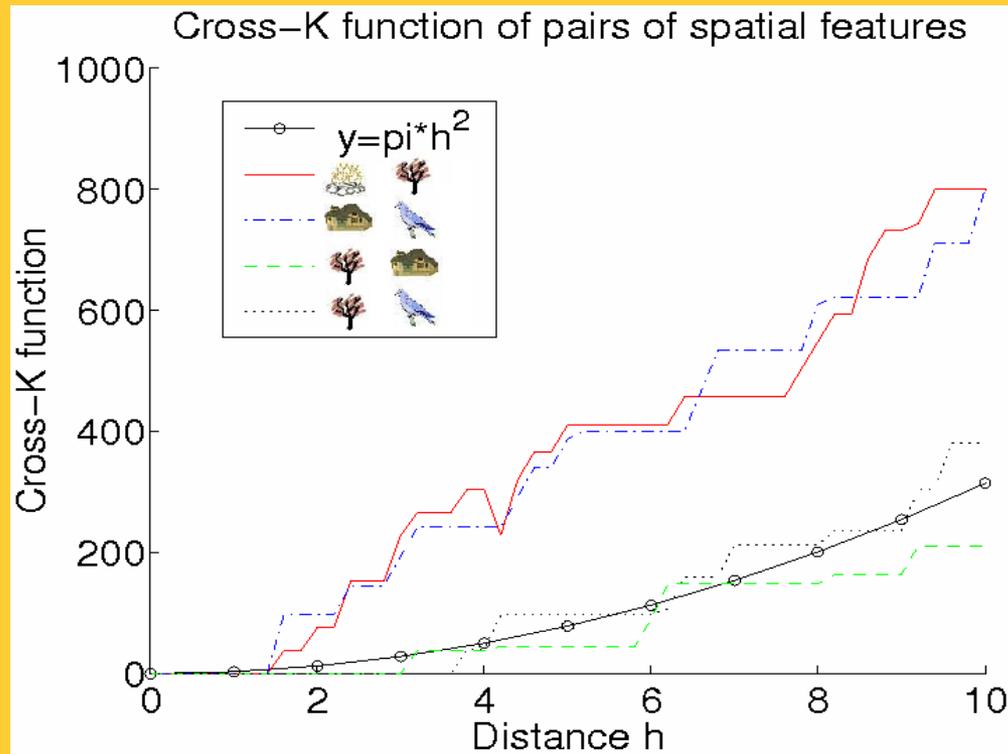
Answers:   and  



Source: Discovering Spatial Co-location Patterns: A General Approach, IEEE Transactions on Knowledge and Data Eng., 16(12), December 2004 (w/ H.Yan, H.Xiong).

Illustration of Cross-Correlation

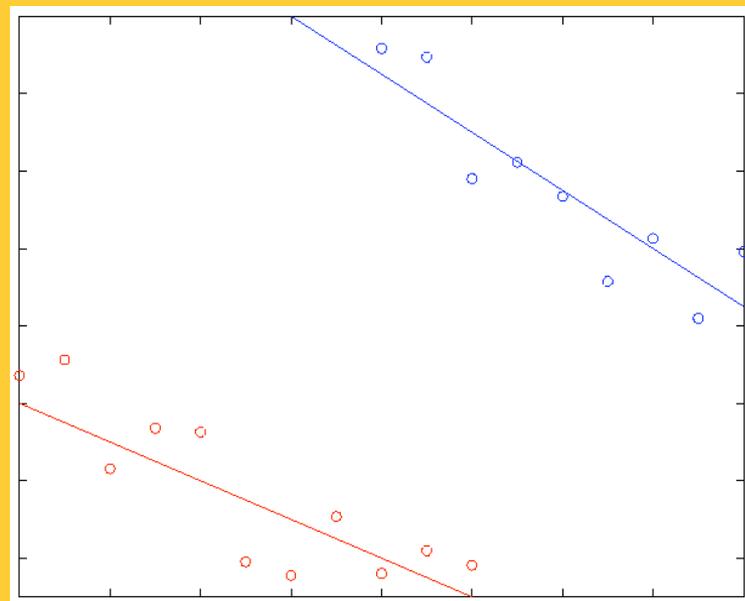
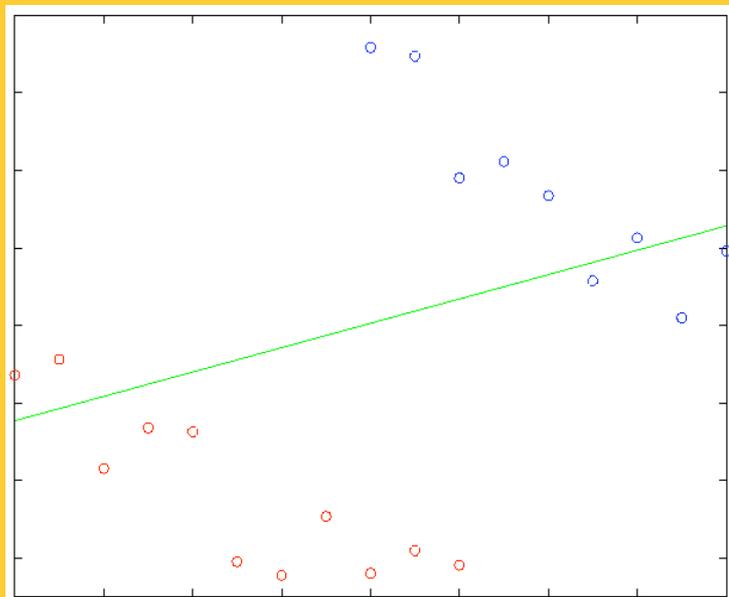
- Illustration of Cross K-function for Example Data



Cross-K Function for Example Data

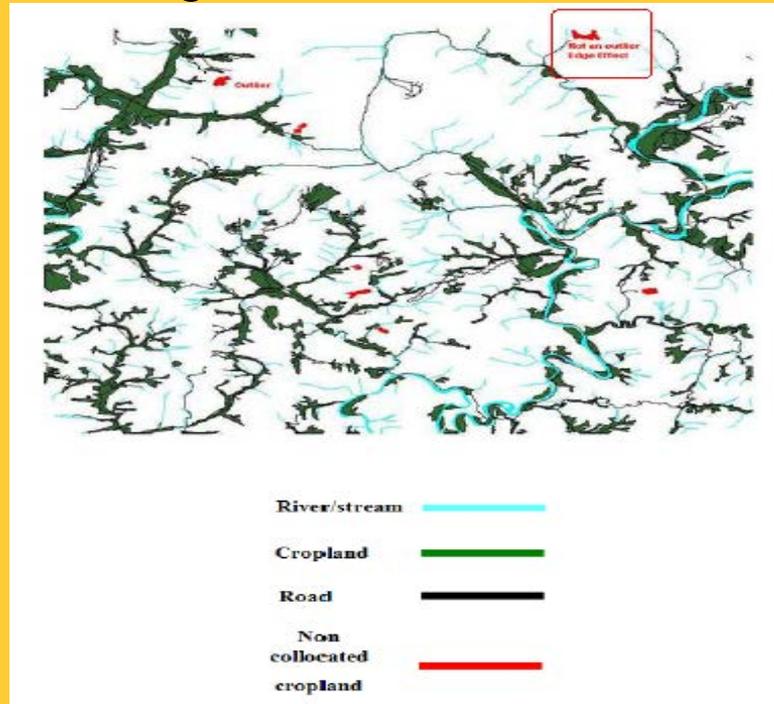
Spatial Heterogeneity

- “Second law of geography” [M. Goodchild, UCGIS 2003]
- Global model might be inconsistent with regional models
 - Spatial Simpson’s Paradox
- May improve the effectiveness of SDM, show support regions of a pattern



Edge Effect

- Cropland on edges may not be classified as outliers
- No concept of spatial edges in classical data mining



Korea Dataset, Courtesy:
Architecture Technology
Corporation

Research Challenges of Spatial Statistics

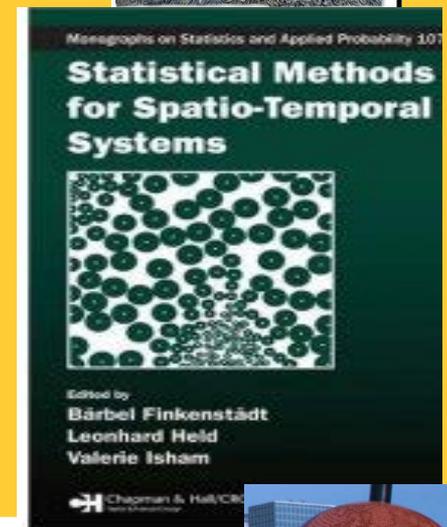
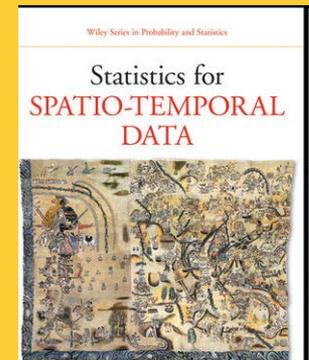
- State-of-the-art of Spatial Statistics

		Point Process	Lattice	Geostatistics
raster			√	√
Vector	Point	√	√	√
	Line			√
	Polygon		√	√
graph				

Data Types and Statistical Models

- Research Needs

- Correlating extended features, road, rivers, cropland
- Spatio-temporal statistics
- Spatial graphs, e.g., reports with street address

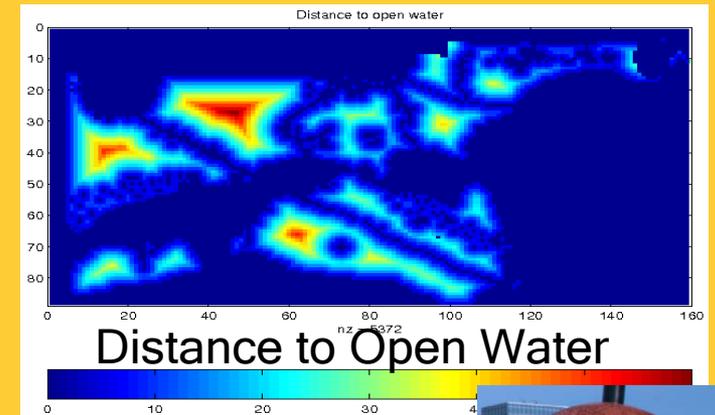
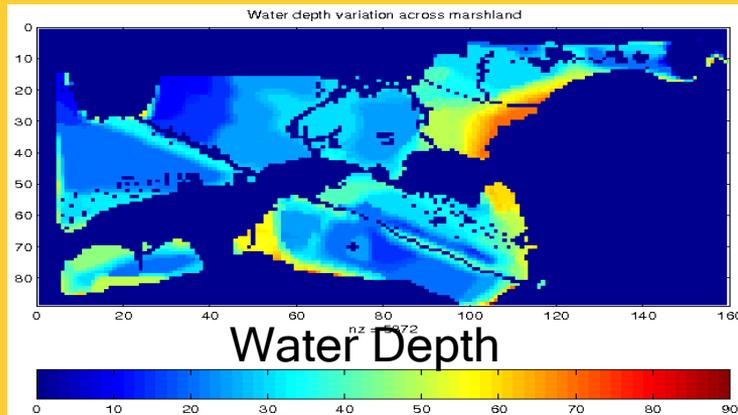
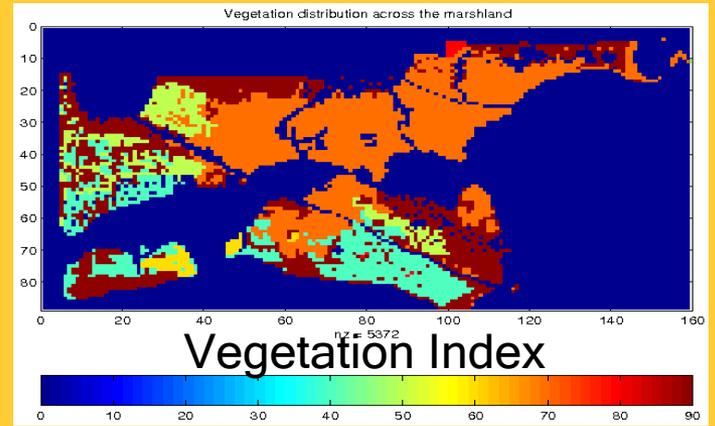
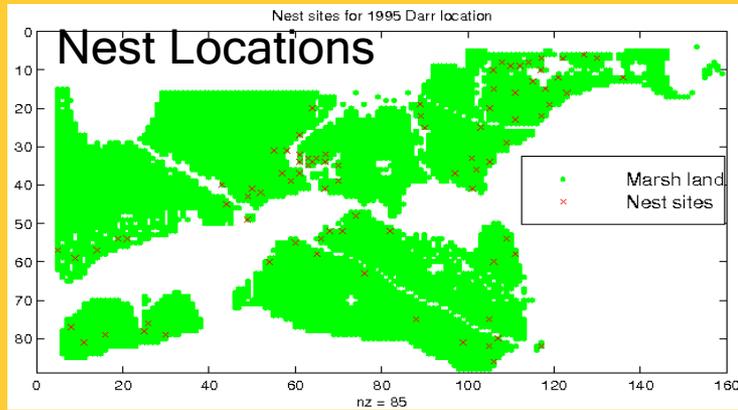


Outline

- Motivation
- Spatial Data Types
- Spatial Statistical Foundations
- **Spatial Data Mining**
 - Location Prediction
 - Hotspots
 - Spatial Outliers
 - Colocations
- Conclusions



Illustration of Location Prediction Problem



Decision Tree

vs. Spatial Decision Tree

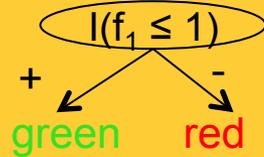
Inputs: table of records

Output: Decision Tree

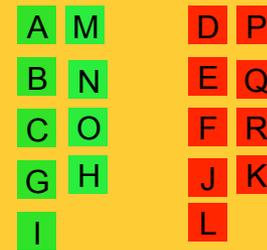
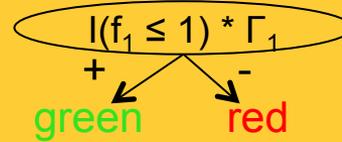
Inputs: feature n class maps, (root) neighborhood

Output: Spatial Decision Tree

ID	f_1	f_2	class
A	1	1	green
B	1	1	green
C	1	3	green
G	1	1	green
I	1	3	green
K	1	2	red
M	1	1	green
N	1	1	green
O	1	3	green
D	3	2	red
E	3	2	red
F	3	2	red
H	3	1	green
J	3	2	red
L	3	2	red
P	3	2	red
Q	3	2	red
R	3	2	red



Predicted map



Predicted map



Focal function Γ_1

1	.3	.3	.3	.3	1
.3	-1	0	0	-1	.3
1	.3	.3	.3	.3	1

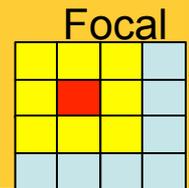
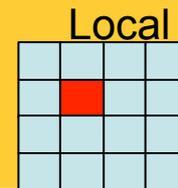
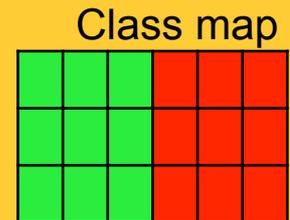
feature test	information gain
$f_1 \leq 1$	0.50
$f_2 \leq 1$	0.46
$f_2 \leq 2$	0.19

Feature f_1

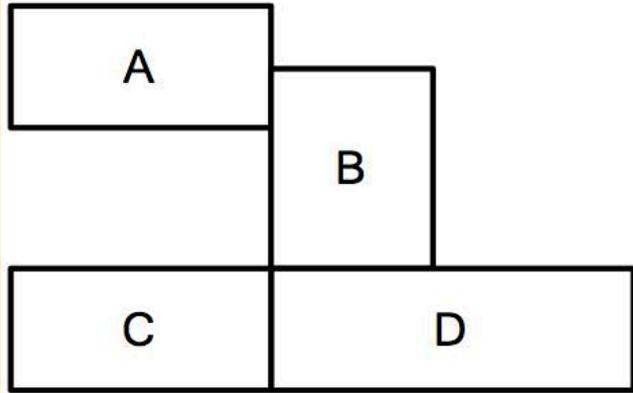
1	1	1	3	3	3
1	3	1	3	1	3
1	1	1	3	3	3

Feature f_2

1	1	3	2	2	2
1	1	3	2	2	2
1	1	3	2	2	2



Neighbor Relationship: W Matrix



(a) Map

	A	B	C	D
A	0	1	0	0
B	1	0	1	1
C	0	1	0	1
D	0	1	1	0

(b) Boolean W

	A	B	C	D
A	0	1	0	0
B	0.3	0	0.3	0.3
C	0	0.5	0	0.5
D	0	0.5	0.5	0

(c) Row-normalized W

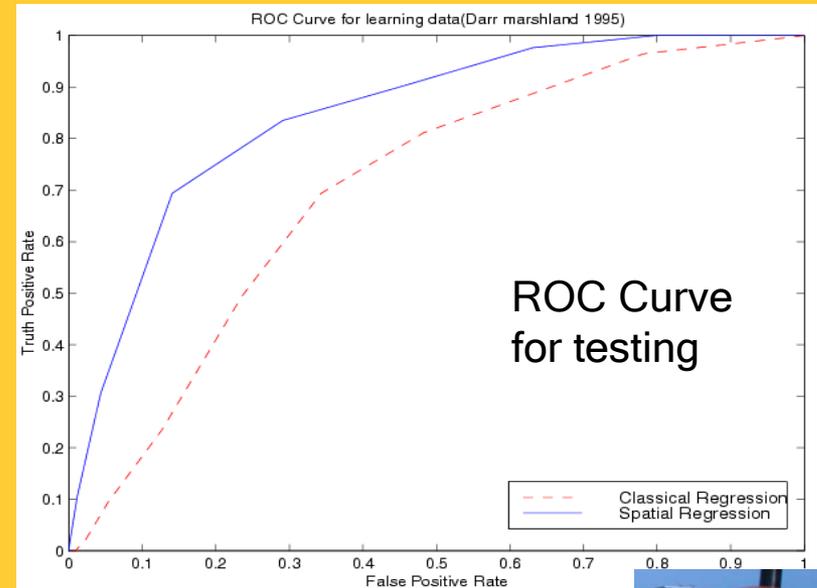
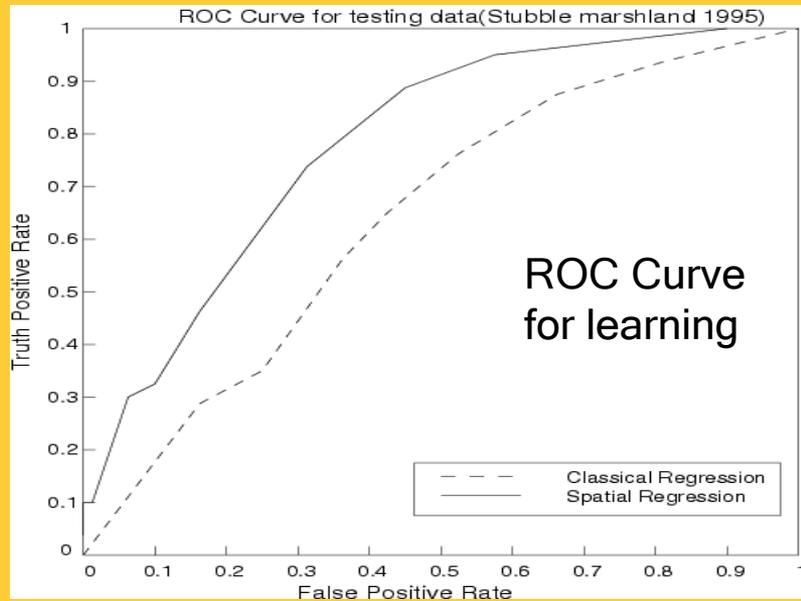
Location Prediction Models

- Traditional Models, e.g., Regression (with Logit or Probit),
 - Bayes Classifier, ...
- Spatial Models
 - Spatial autoregressive model (SAR)
 - Markov random field (MRF) based Bayesian Classifier

Classical	Spatial
$y = X\beta + \varepsilon$	$y = \rho W y + X\beta + \varepsilon$
$\Pr(C_i X) = \frac{\Pr(X C_i) \Pr(C_i)}{\Pr(X)}$	$\Pr(c_i X, C_N) = \frac{\Pr(C_i) \Pr(X, C_N c_i)}{\Pr(X, C_N)}$

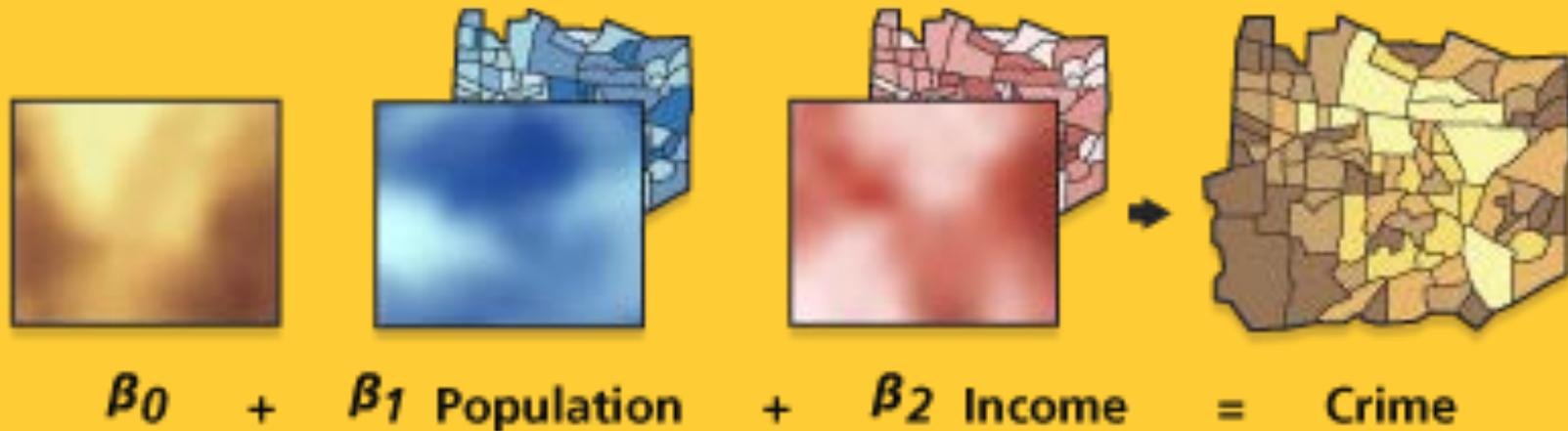
Comparing Traditional and Spatial Models

- Dataset: Bird Nest prediction
- Linear Regression
 - Lower prediction accuracy, coefficient of determination,
 - Residual error with spatial auto-correlation
- Spatial Auto-regression outperformed linear regression



Modeling Spatial Heterogeneity: GWR

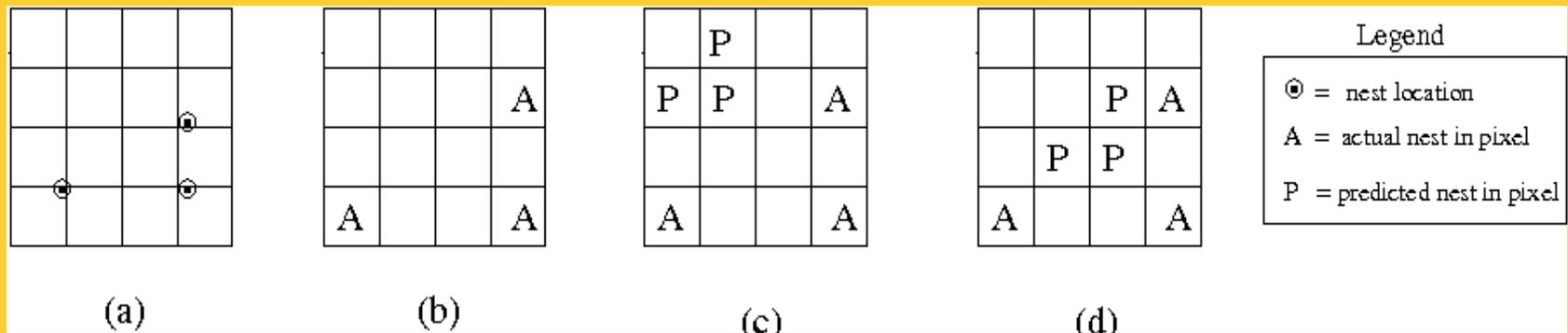
- Geographically Weighted Regression (GWR)
 - Goal: Model spatially varying relationships
 - Example: $y = X\beta' + \varepsilon'$
Where β' and ε' are location dependent



Source: resources.arcgis.com

Research Needs for Location Prediction

- Spatial Auto-Regression
 - Estimate W
 - Scaling issue $\rho W y$ vs. $X\beta$
- Spatial interest measure
 - e.g., distance(actual, predicted)



(a) Actual Sites

(b) Pixels with actual sites

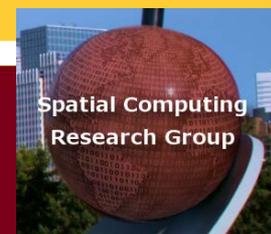
(c) Prediction 1

(d) Prediction 2.

Spatially more interesting than Prediction 1

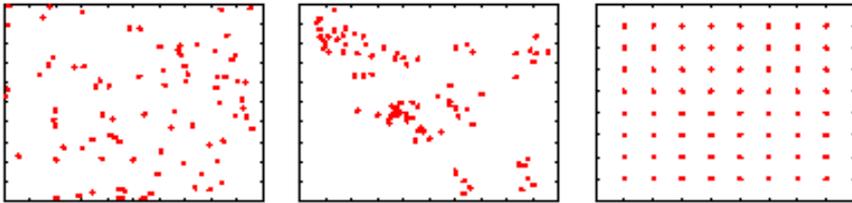
Outline

- Motivation
- Spatial Data Types
- Spatial Statistical Foundations
- **Spatial Data Mining**
 - Location Prediction
 - **Hotspots**
 - Spatial Outliers
 - Colocations
- Conclusions



Limitations of K-Means

- K-Means does test Statistical Significance
 - Finds chance clusters in complete spatial randomness (CSR)



Classical
Clustering



Spatial
Clustering



SaTScan™

Software for the spatial, temporal, and space-time scan statistics

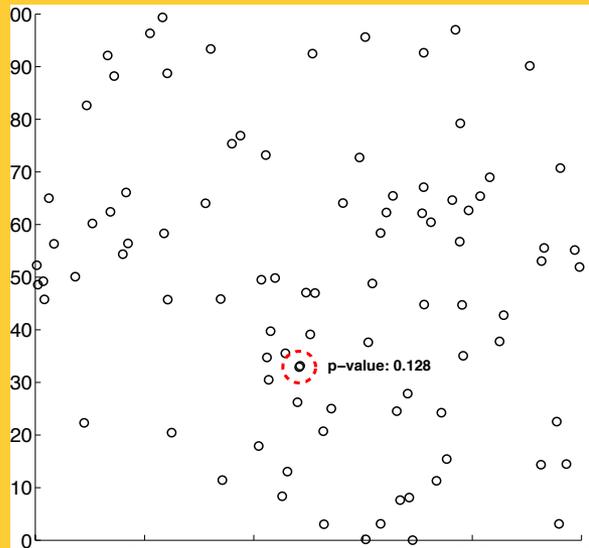


Spatial Scan Statistics (SatScan)

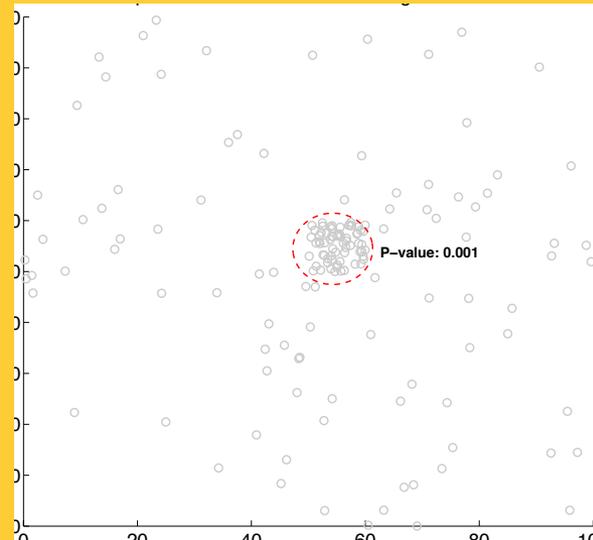
- Goal: Omit chance clusters
- Ideas: Likelihood Ratio, Statistical Significance
- Steps
 - Enumerate candidate zones & choose zone X with highest likelihood ratio (LR)
 - $LR(X) = p(H1|data) / p(H0|data)$
 - $H0$: points in zone X show complete spatial randomness (CSR)
 - $H1$: points in zone X are clustered
 - If $LR(Z) \gg 1$ then test statistical significance
 - Check how often is $LR(CSR) > LR(Z)$
using 1000 Monte Carlo simulations

SatScan Examples

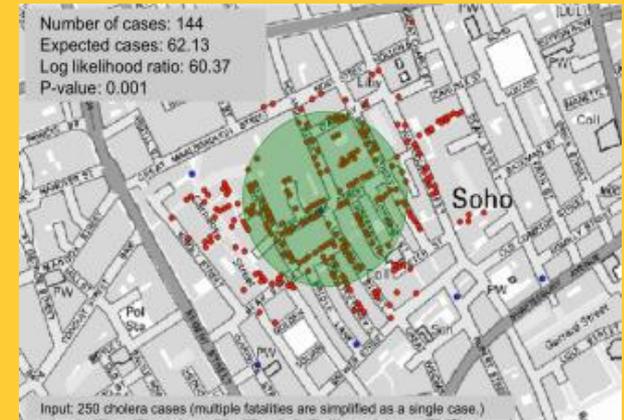
Complete Spatial Randomness
Output: No hotspots !
Highest LR circle p-value = 0.128



Data with a hotspot
Output: A hotspot!
p-value = 0.001



1854 London Cholera
Output: A hotspot!
p-value = 0.001

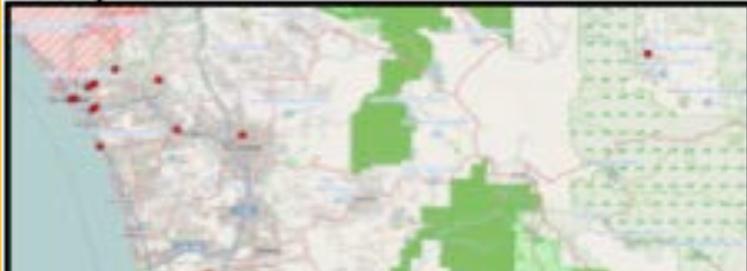


Complex Hotspots

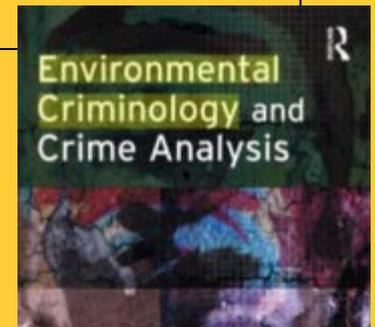
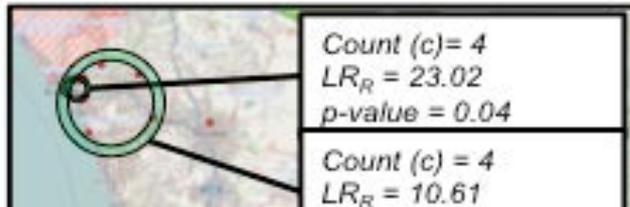
Semantic Gap between Spatial and Machine Learning

- Environmental Criminology
 - Routine Activities Theory, Crime Pattern Theory, Doughnut Hole pattern
- Formulation: **rings**, where **inside** density is significantly higher than **outside** ...

Input



Output: Ring Shaped Hotspot Detection (RHD)



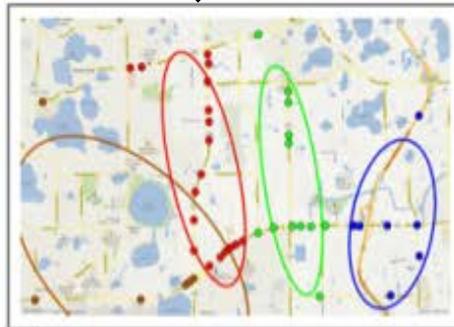
Mathematics	Concepts	Relationships
Sets	Set Theory	Member, set-union, set-difference, ...
Vector Space	Linear Algebra	Matrix & vector operations
Euclidean Spaces	Geometry	Circle, Ring , Polygon, Line_String, Convex hull, ...
Boundaries, Graphs, Spatial Graphs	Topology, Graph Theory, Spatial graphs, ...	Interior, boundary, Neighbor, inside , surrounds , ..., Nodes, edges, paths, trees, ... Path with turns, dynamic segmentation, ...

Spatial-Concept/Theory-Aware Clusters

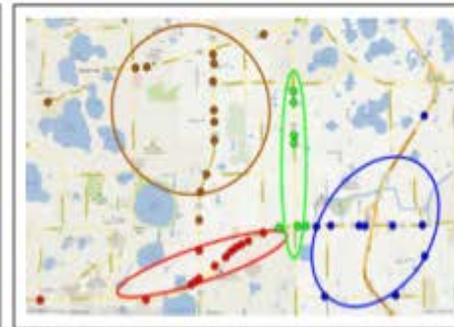
- Spatial Theories, e.g., environmental criminology
 - Circles \rightarrow Doughnut holes
- Geographic features, e.g., rivers, streams, roads, ...
 - Hot-spots \Rightarrow Hot Geographic-features



(a) Input



(b) Crimestat K-means with Euclidean Distance



(c) Crimestat K-means with Network Distance



(d) KMR

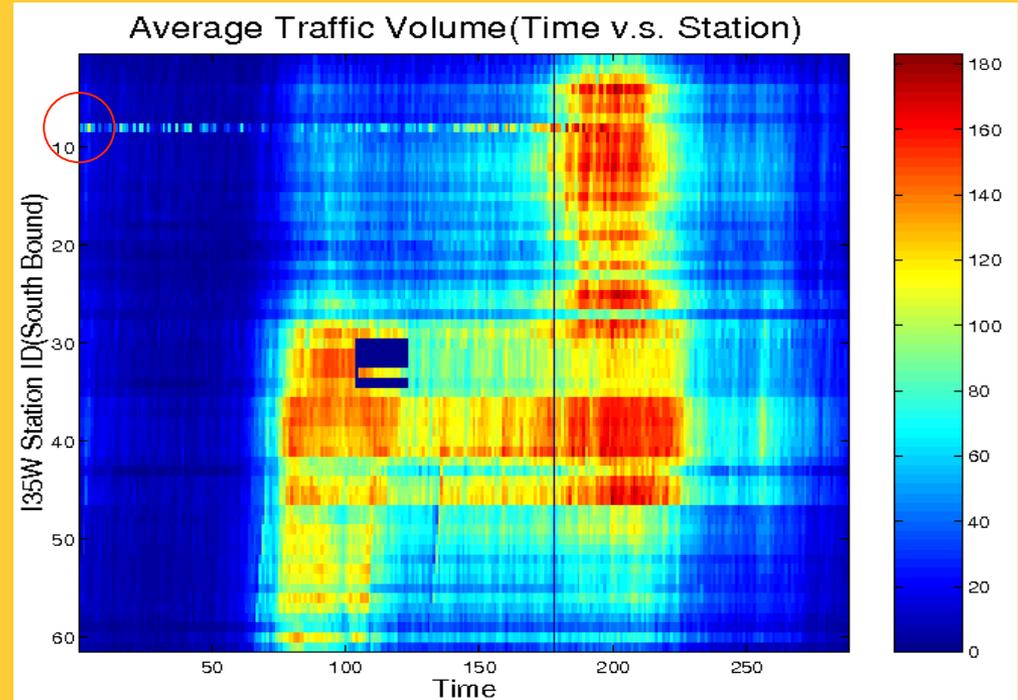
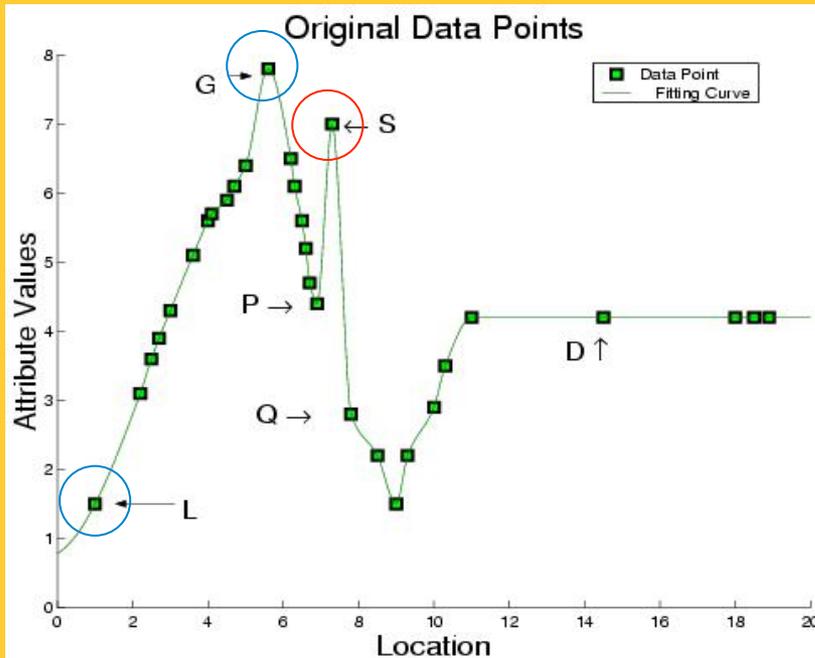
Source: A K-Main Routes Approach to Spatial Network Activity Summarization, IEEE Transactions on Knowledge and Data Eng., 26(6), 2014.)

Outline

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- Spatial Data Types
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- **Spatial Data Mining**
 - Location Prediction
 - Hotspots
 - **Spatial Outliers**
 - Colocations
- Conclusions

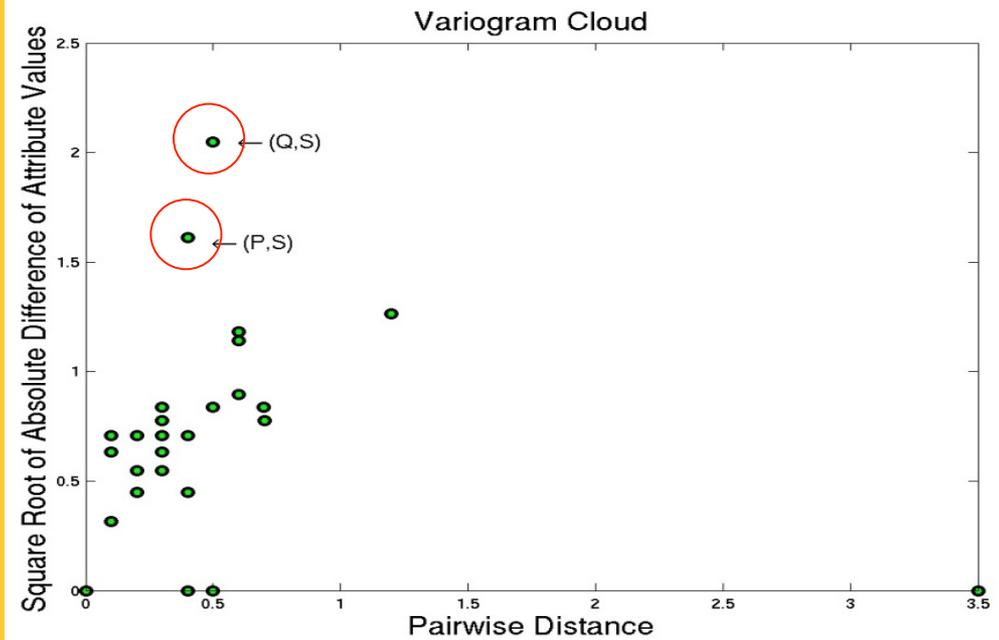
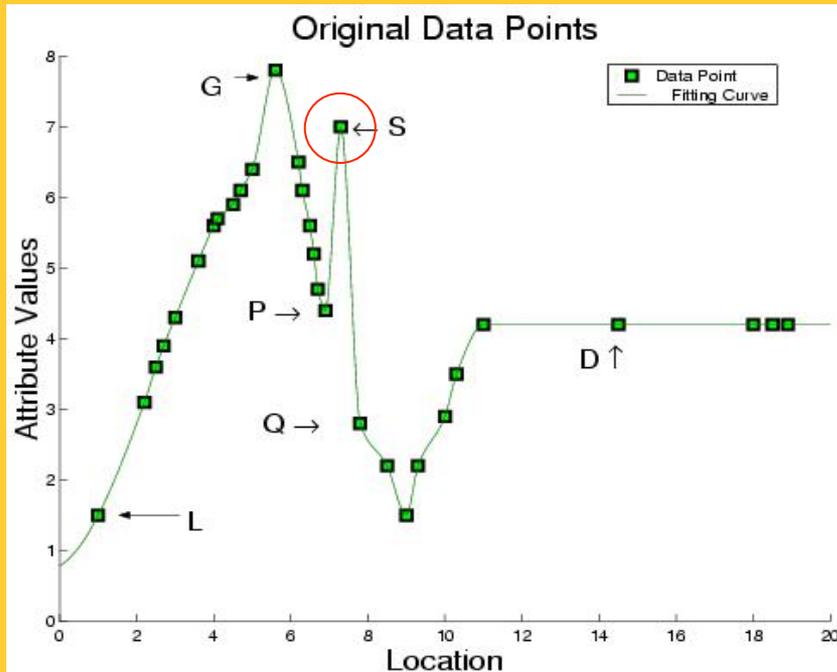


Outliers: Global (G) vs. Spatial (S)



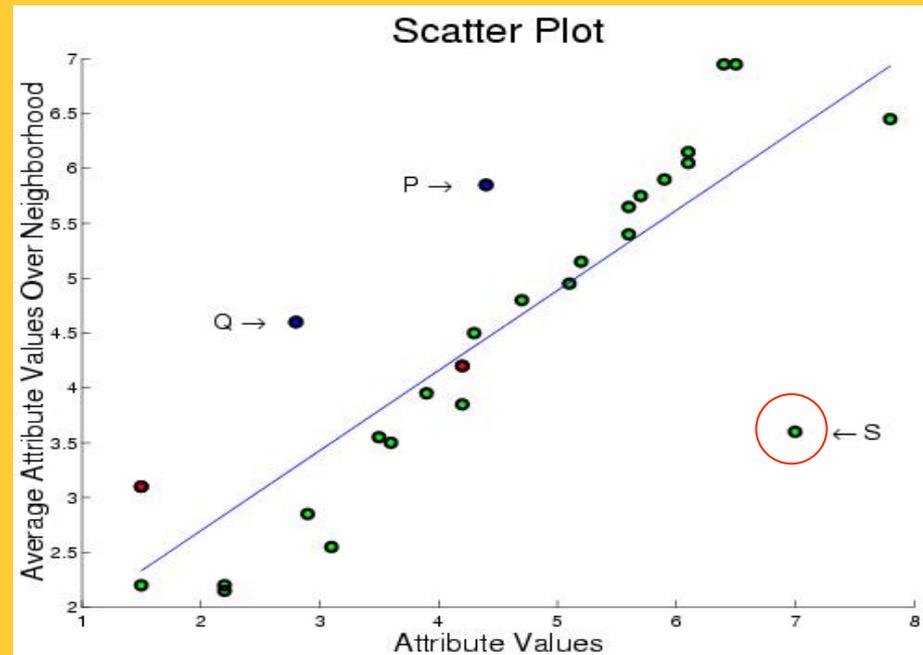
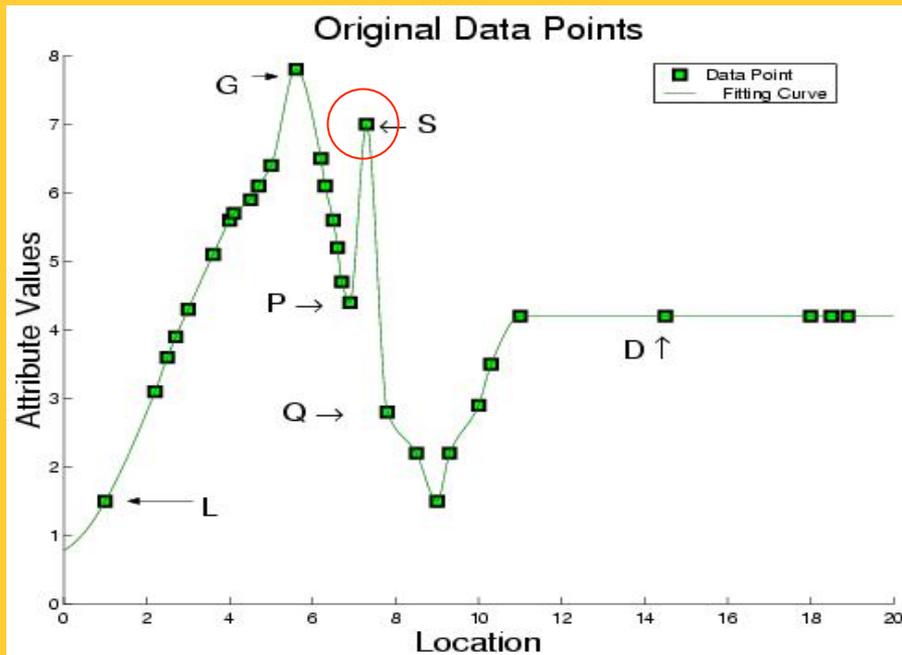
Outlier Detection Tests: Variogram Cloud

- Graphical Test: Variogram Cloud



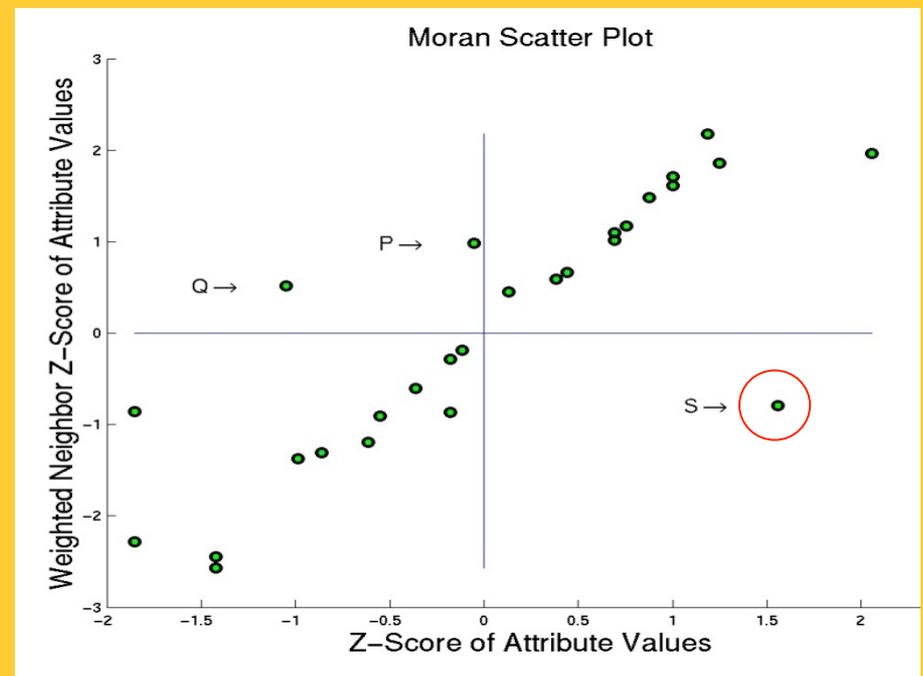
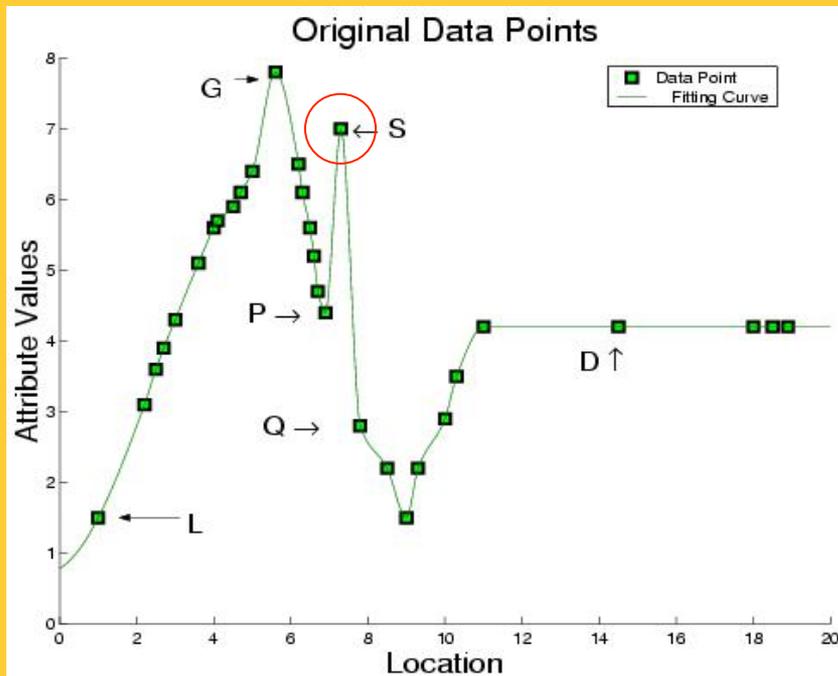
Outlier Detection - Scatterplot

- Quantitative Tests: Scatter Plot



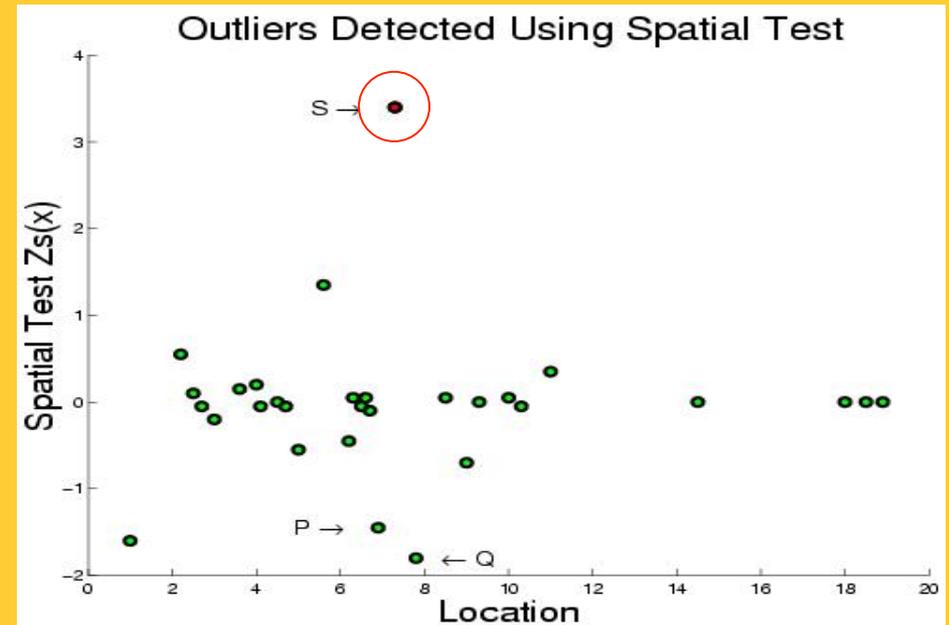
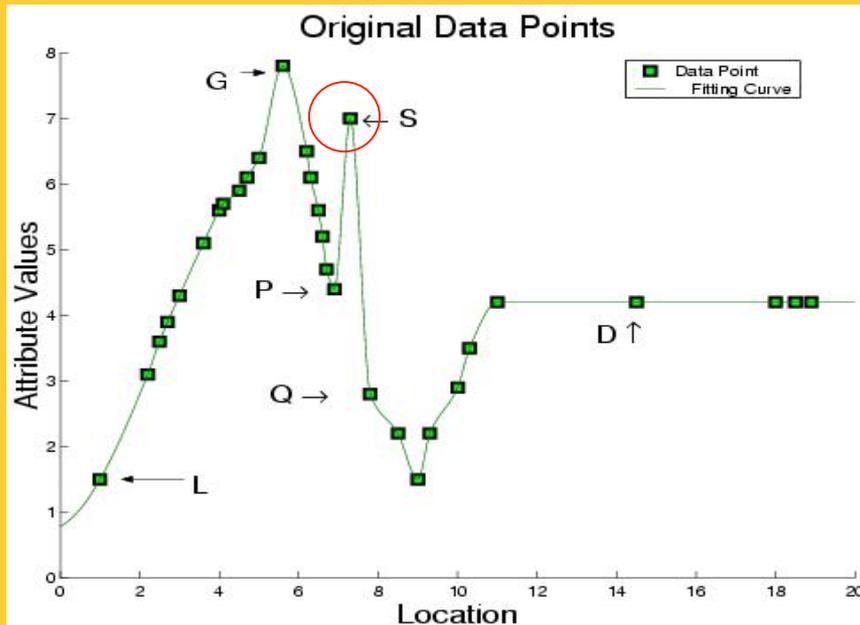
Outlier Detection Test: Moran Scatterplot

- Graphical Test: Moran Scatter Plot



Outlier Detection Tests: Spatial Z-test

- Quantitative Tests: Spatial Z-test
 - Algorithmic Structure: Spatial Join on neighbor relation



Spatial Outlier Detection: Computation

- Separate two phases
 - Model Building
 - Testing: test a node (or a set of nodes)
- Computation Structure of Model Building
 - Key insights:
 - Spatial self join using $N(x)$ relationship
 - Algebraic aggregate function computed in one scan of spatial join



Trends in Spatial Outlier Detection

- Multiple spatial outlier detection
 - Eliminating the influence of neighboring outliers
- Multi-attribute spatial outlier detection
 - Use multiple attributes as features
- Scale up for large data



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 - **Colocations**
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Learning Objectives

- After this segment, students will be able to
 - Contrast collocations and associations
 - Describe collocation interest measures



Background: Association Rules

- Association rule e.g. (Diaper in T => Beer in T)

Transaction	Items Bought
1	{socks,  , milk,  , beef, egg, ...}
2	{pillow,  , toothbrush, ice-cream, muffin, ...}
3	{  ,  , pacifier, formula, blanket, ...}
...	...
n	{battery, juice, beef, egg, chicken, ...}

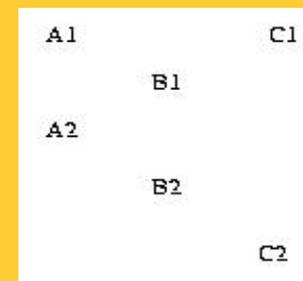
- Support: probability (Diaper and Beer in T) = 2/5
 - Confidence: probability (Beer in T | Diaper in T) = 2/2
- Apriori Algorithm
 - Support based pruning using monotonicity

Association Rules Limitations

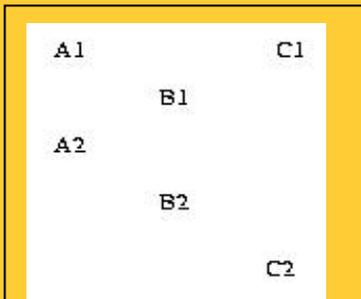
- Transaction is a core concept!
 - Support is defined using **transactions**
 - Apriori algorithm uses **transaction** based Support for pruning

Transaction	Items Bought
1	{socks,  , milk,  , beef, egg, ...}
2	{pillow,  , toothbrush, ice-cream, muffin, ...}
3	{  ,  , pacifier, formula, blanket, ...}
...	...

- However, spatial data is embedded in continuous space
 - Transactionizing continuous space is non-trivial !



Spatial Association Rule vs. Colocation

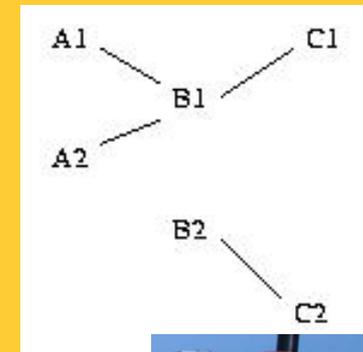
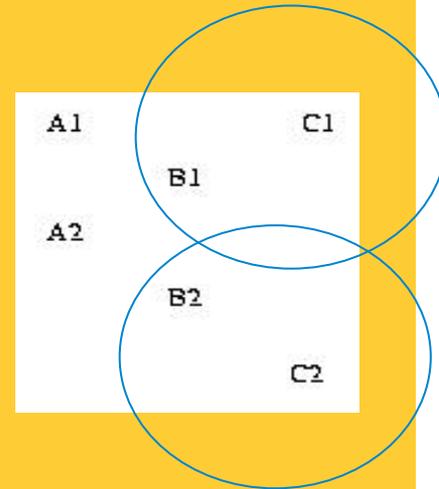


Input = Spatial feature A,B, C, & their instances

- Spatial Association Rule (Han 95)
- **Output = (B,C)**
- **Transactions by Reference feature C**
Transactions: (C1, B1), (C2, B2)
Support (A,B) = \emptyset , Support(B,C) = $2 / 2 = 1$

- **Cross-K Function**
Cross-K (A, B) = $2/4 = 0.5$
Cross-K(B, C) = $2/4 = 0.5$
Output = (A,B), (B, C)

- **Colocation - Neighborhood graph**
Output = (A,B), (B, C)
 $PI(A,B) = \min(2/2, 1/2) = 0.5$
 $PI(B,C) = \min(2/2, 2/2) = 1$

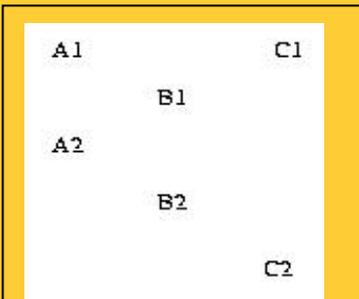


Spatial Association vs. Cross-K Function

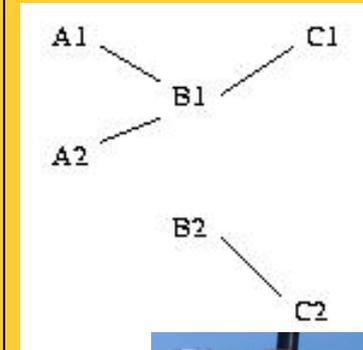
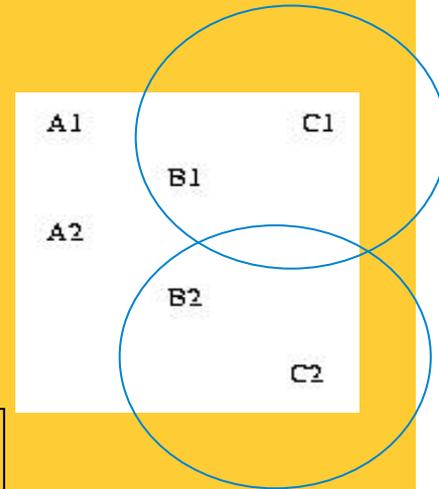
- Spatial Association Rule (Han 95)
- **Output = (B,C)** with threshold 0.5
- **Transactions by Reference feature, e.g. C**
Transactions: (C1, B1), (C2, B2)
Support (A,B) = \emptyset
Support(B,C) = $2 / 2 = 1$

- **Cross-K Function**
Cross-K (A, B) = $2/4 = 0.5$
Cross-K(B, C) = $2/4 = 0.5$
Cross-K(A, C) = 0

Output = (A,B), (B, C) with threshold 0.5



Input = Feature A,B, and, C, & instances A1, A2, B1, B2, C1, C2



Spatial Colocation

Features: A, B, C

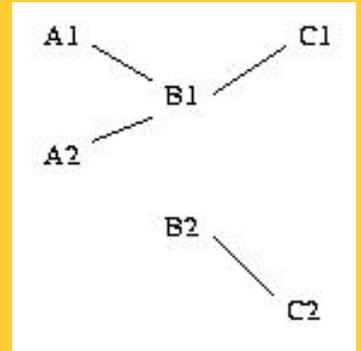
Feature Instances: A1, A2, B1, B2, C1, C2

Feature Subsets: (A,B), (A,C), (B,C), (A,B,C)

Participation ratio (pr):

$\text{pr}(A, (A,B)) = \text{fraction of A instances neighboring feature } \{B\} = 2/2 = 1$

$\text{pr}(B, (A,B)) = 1/2 = 0.5$



Participation index (A,B) = pi(A,B) = min{ pr(A, (A,B)), pr(B, (A,B)) } = min (1, 1/2) = 0.5

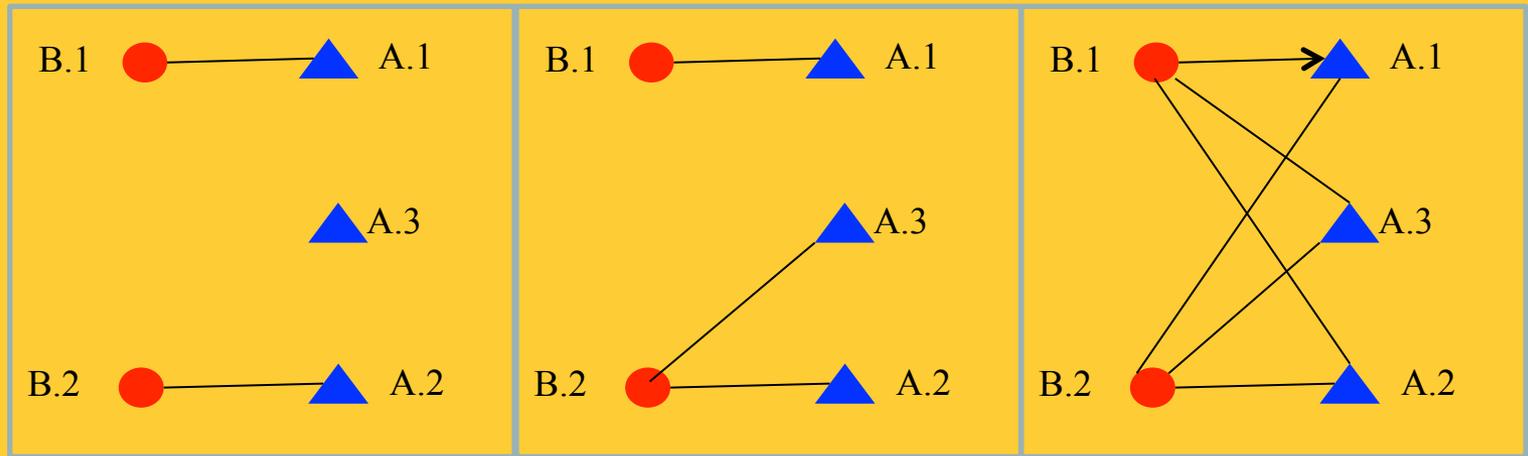
pi(B, C) = min{ pr(B, (B,C)), pr(C, (B,C)) } = min (1,1) = 1

Participation Index Properties:

(1) Computational: Non-monotonically decreasing like support measure

(2) Statistical: Upper bound on Ripley's Cross-K function

Participation Index \geq Cross-K Function



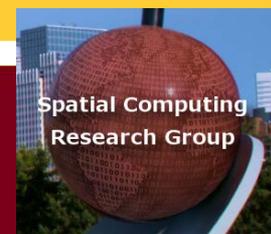
Cross-K (A,B)			
PI (A,B)			

Association Vs. Colocation

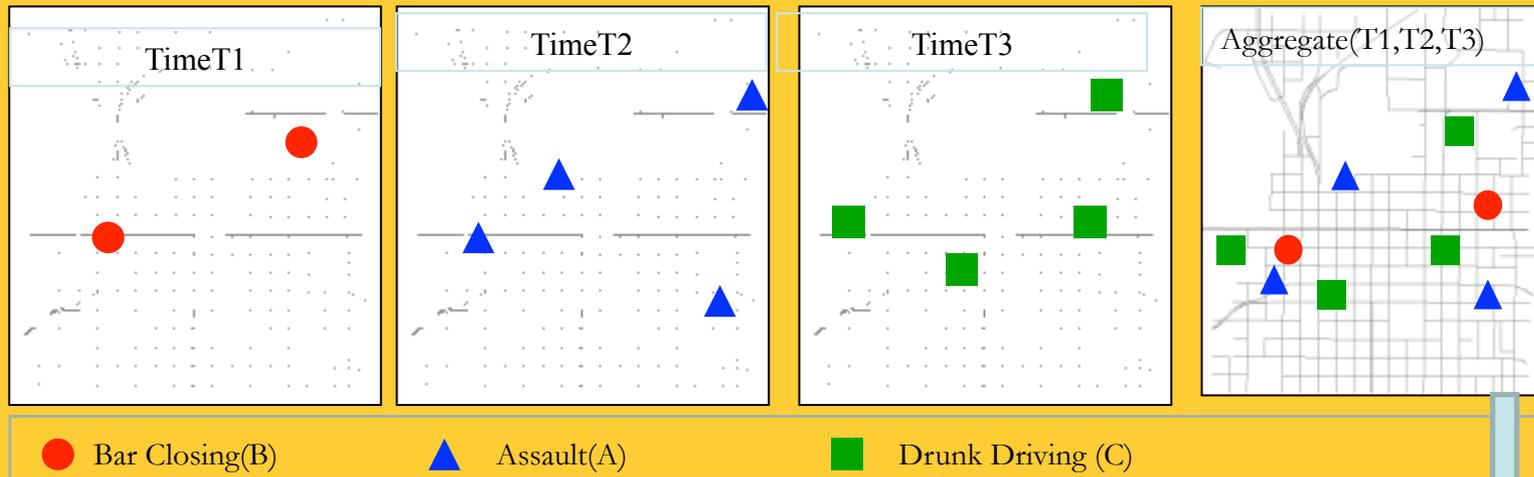
	Associations	Colocations
underlying space	Discrete market baskets	
event-types	item-types, e.g., Beer	
collections	Transaction (T)	
prevalence measure	Support, e.g., Pr.[Beer in T]	
conditional probability measure	Pr.[Beer in T Diaper in T]	

Spatial Colocation: Trends

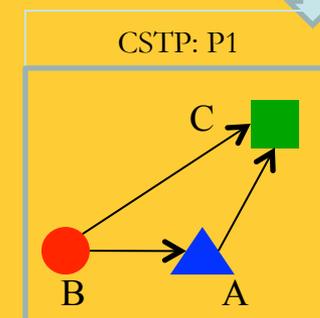
- Algorithms
 - Join-based algorithms
 - One spatial join per candidate colocation
 - Join-less algorithms
- Spatio-temporal
 - Which events co-occur in space and time?
 - (bar-closing, minor offenses, drunk-driving citations)
 - Which types of objects move together?



Cascading spatio-temporal pattern (CSTP)



- ❑ **Input:** Urban Activity Reports
- ❑ **Output: CSTP**
 - ❑ *Partially ordered* subsets of ST event types.
 - ❑ Located together in space.
 - ❑ Occur in *stages* over time.
- ❑ Applications: Public Health, Public Safety, ...

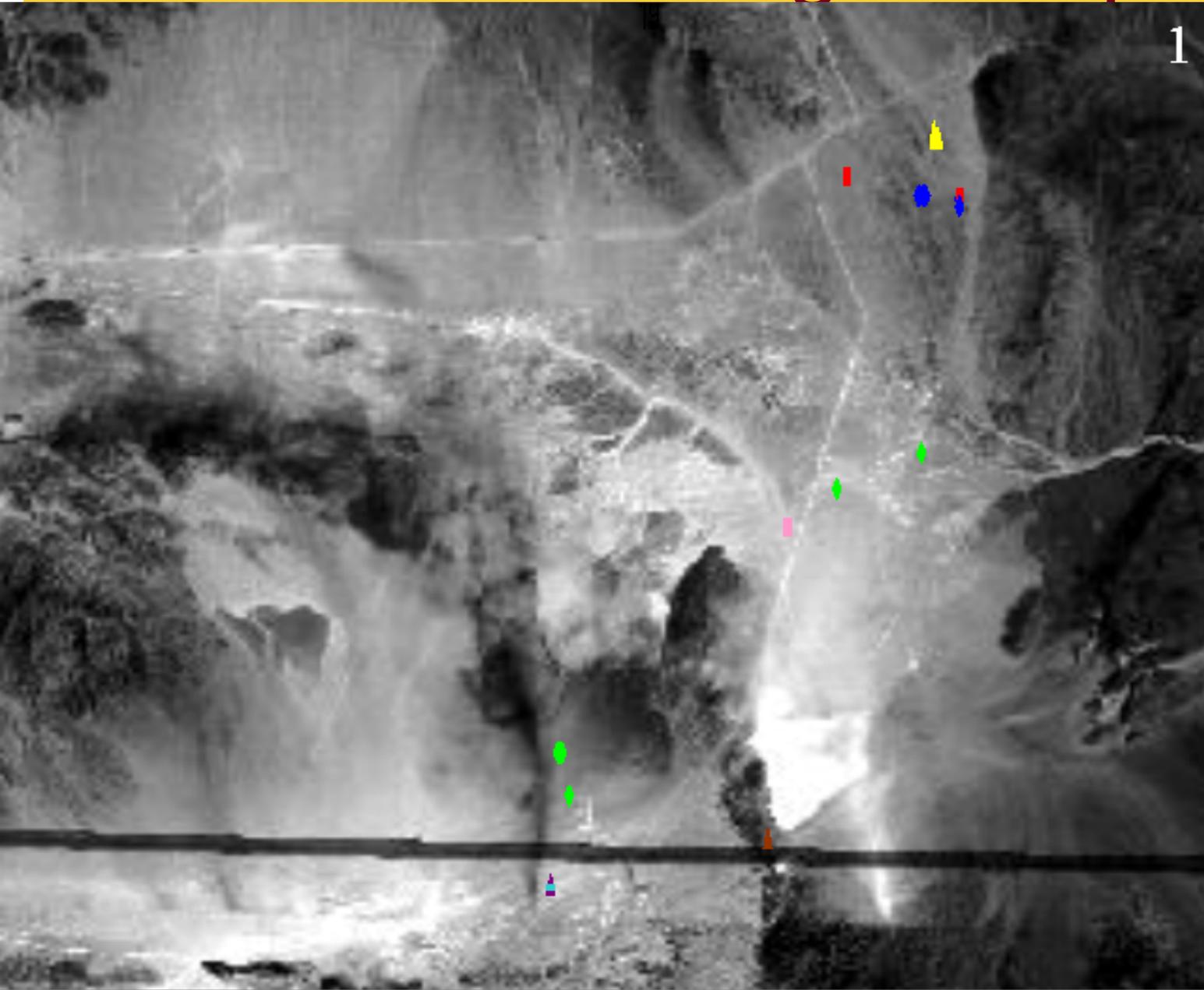


Details: Cascading Spatio-Temporal Pattern Discovery, IEEE Trans. on Know. & Data Eng, 24(11), 2012.

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Driven to DiscoverSM

MDCOP Motivating Example



Manpack stinger
(2 Objects)



M1A1_tank
(3 Objects)



M2_IFV
(3 Objects)



Field_Marker
(6 Objects)

T80_tank
(2 Objects)



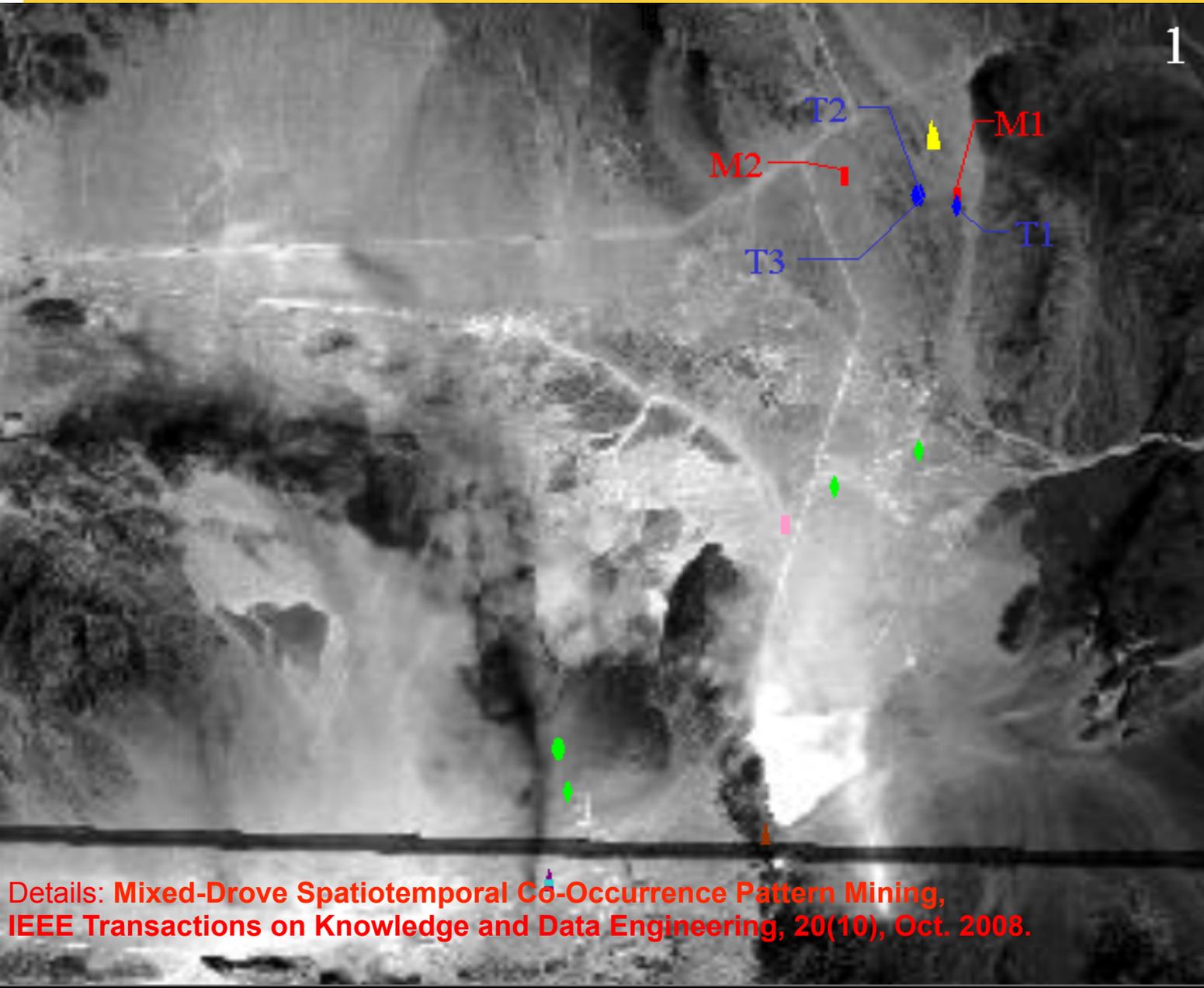
BRDM_AT5
(enemy) (1 Object)



BMP1
(1 Object)



MDCOP Motivating Example : Output



• Manpack stinger
(2 Objects)



• M1A1_tank
(3 Objects)



• M2_IFV
(3 Objects)



• Field_Marker
(6 Objects)

• T80_tank
(2 Objects)



• BRDM_AT5
(enemy) (1 Object)



• BMP1
(1 Object)



Details: Mixed-Drove Spatiotemporal Co-Occurrence Pattern Mining,
IEEE Transactions on Knowledge and Data Engineering, 20(10), Oct. 2008.

Outline

- Motivation
 - Use cases
 - Pattern families
- Spatial Data Types
- Spatial Statistical Foundations
- Spatial Data Mining
- **Conclusions**



Summary

What's Special About Mining Spatial Data ?

		Spatial DM	
Input Data		Often implicit relationships, complex types	
Statistical Foundation			
Output	Association		
	Clusters		
	Outlier		
	Prediction		

Acknowledgements

National Science Foundation (Current Grants)

- 1320580 : III:Investigating Spatial Big Data for Next Generation Routing Services
- 0940818: Expedition: Understanding Climate Change: A Data Driven Approach
- IIS-1218168 : III:Towards Spatial Database Management Systems for Flash Memory Storage
- 1029711 :: Datanet: Terra Populus: A Global Population / Environment Data Network

USDOD (Current Grants)

- HM0210-13-1-0005: Identifying and Analyzing Patterns of Evasion
- SBIR Phase II: Spatio-Temporal Analysis in GIS Environments (STAGE) (with Architecture Technology Corporation)

University of Minnesota (Current Grants)

- Infrastructure Initiative: U-Spatial - Support for Spatial Research
- MOOC Initiative: From GPS and Google Earth to Spatial Computing

- Past Sponsors, e.g., NASA, ARL, AGC/TEC, Mn/DOT, ...

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Driven to DiscoverSM

References

Colocations

- Discovering colocation patterns from spatial data sets: a general approach, *IEEE Transactions on Knowledge and Data Engineering*, 16(12), 2004 (with Y. Huang et al.).
- A join-less approach for mining spatial colocation patterns, *IEEE Transactions on Knowledge and Data Engineering*, 18 (10), 2006. (with J. Yoo).

Spatial Outliers

- Detecting graph-based spatial outliers: algorithms and applications (a summary of results), *Proc.: ACM International Conference on Knowledge Discovery & Data Mining*, 2001 (with Q. Lu et al.)
- A unified approach to detecting spatial outliers, *Springer Geoinformatica*, 7 (2), 2003. (w/ C. T. Lu, et al.)

Hot-Spots

- Discovering personally meaningful places: An interactive clustering approach, *ACM Transactions on Information Systems (TOIS)* 25 (3), 2007. (with C. Zhou et al.)
- A K-Main Routes Approach to Spatial Network Activity Summarization, *IEEE Transactions on Knowledge & Data Engineering*, 26(6), 2014. (with D. Oliver et al.)

Location Prediction

- Spatial contextual classification and prediction models for mining geospatial data, *IEEE Transactions on Multimedia*, 4 (2), 2002. (with P. Schrater et al.)
- Focal-Test-Based Spatial Decision Tree Learning, to appear in *IEEE Transactions on Knowledge and Data Eng.* (a summary in *Proc. IEEE Intl. Conference on Data Mining*, 2013).

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- Spatiotemporal change footprint pattern discovery: an inter-disciplinary survey. *Wiley Interdisc. Rev.: Data Mining and Knowledge Discovery* 4(1), 2014. (with X. Zhou et al.)