General Equation of an Ellipse



University of Minnesota General Equation of an Ellipse

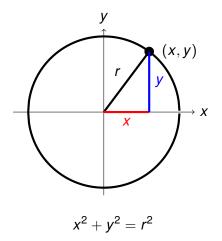
Preliminaries

- Equation of a circle
- Transformation of graphs (shifting and stretching)

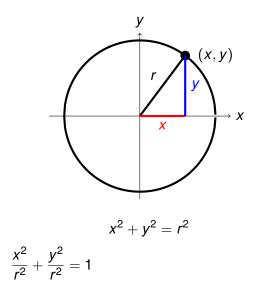
Objectives

• Find the equation of an ellipse, given the graph.

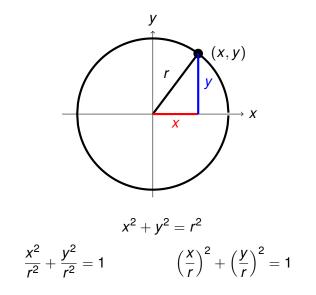
Circle centered at the origin



Circle centered at the origin



Circle centered at the origin



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 $y = \sin(Bx)$

The sine wave is B times thinner. Period (wavelength) is divided by B. Frequency is multiplied by B.

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The sine wave is *B* times thinner. Period (wavelength) is divided by *B*. Frequency is multiplied by *B*.

$$y = \sin\left(\frac{x}{b}\right)$$

The sine wave is *b* times wider. Period (wavelength) is multiplied by *b*. Frequency is divided by *b*.

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The sine wave is *B* times thinner. Period (wavelength) is divided by *B*. Frequency is multiplied by *B*.

$$y = \sin\left(\frac{x}{b}\right)$$

The sine wave is *b* times wider. Period (wavelength) is multiplied by *b*. Frequency is divided by *b*.

$$\left(\frac{x}{r}\right)^2 + \left(\frac{y}{r}\right)^2 = 1$$

The unit circle is stretched *r* times wider and *r* times taller.

$$\left(\frac{x}{r}\right)^2 + \left(\frac{y}{r}\right)^2 = 1$$

The unit circle is stretched *r* times wider and *r* times taller.

$$\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1$$

The unit circle is stretched *a* times wider and *b* times taller.

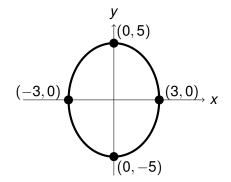
$$\left(\frac{x}{r}\right)^2 + \left(\frac{y}{r}\right)^2 = 1$$

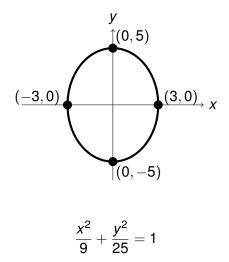
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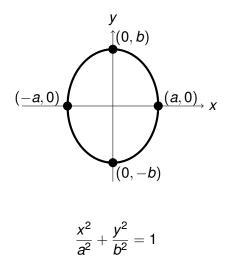
$$\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1$$

The unit circle is stretched *a* times wider and *b* times taller.

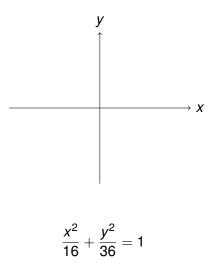
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

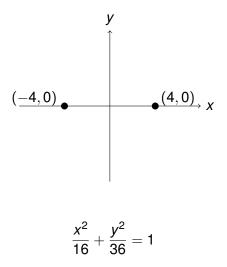


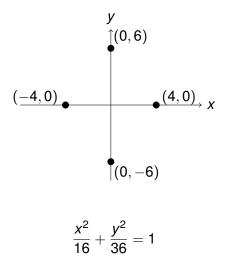


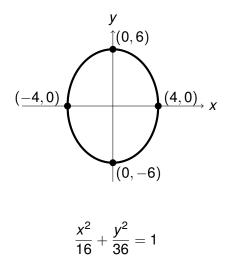


$$\frac{x^2}{16} + \frac{y^2}{36} = 1$$







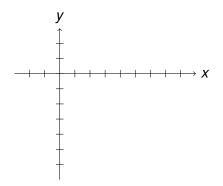


$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

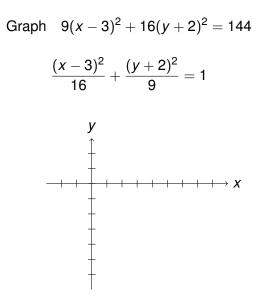
Center at (h, k)

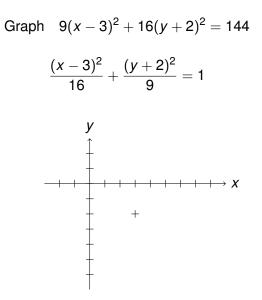
Vertices at (h + a, k), (h - a, k), (h, k + b), (h, k - b)

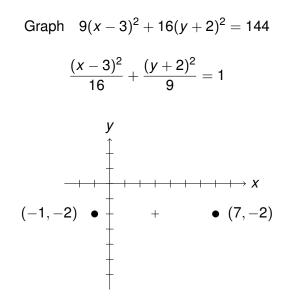
Graph
$$9(x-3)^2 + 16(y+2)^2 = 144$$

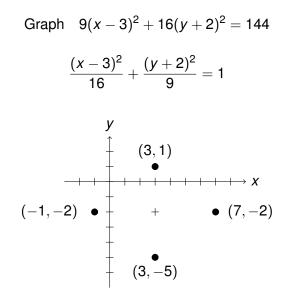


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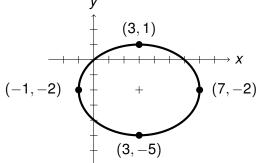


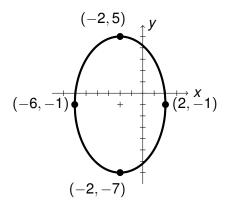




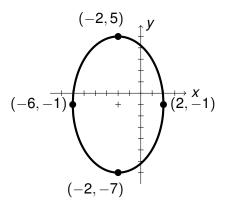
Graph
$$9(x-3)^2 + 16(y+2)^2 = 144$$

 $\frac{(x-3)^2}{16} + \frac{(y+2)^2}{9} = 1$

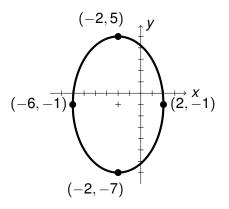




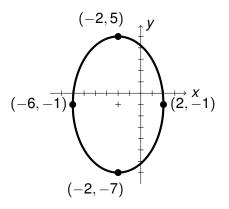
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$$\frac{(x+2)^2}{a^2} + \frac{(y+1)^2}{b^2} = 1$$



$$\frac{(x+2)^2}{16} + \frac{(y+1)^2}{b^2} = 1$$



$$\frac{(x+2)^2}{16} + \frac{(y+1)^2}{36} = 1$$

General Equation of an Ellipse

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

Center at (h, k)

Vertices at (h + a, k), (h - a, k), (h, k + b), (h, k - b)

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